

EFSTRATIOS GAVVES

GROUNDING FOUNDATION MODELS IN REALITY PHYSICS- & CAUSALITY-INFORMED WORLD MODELS

WHO AM I?

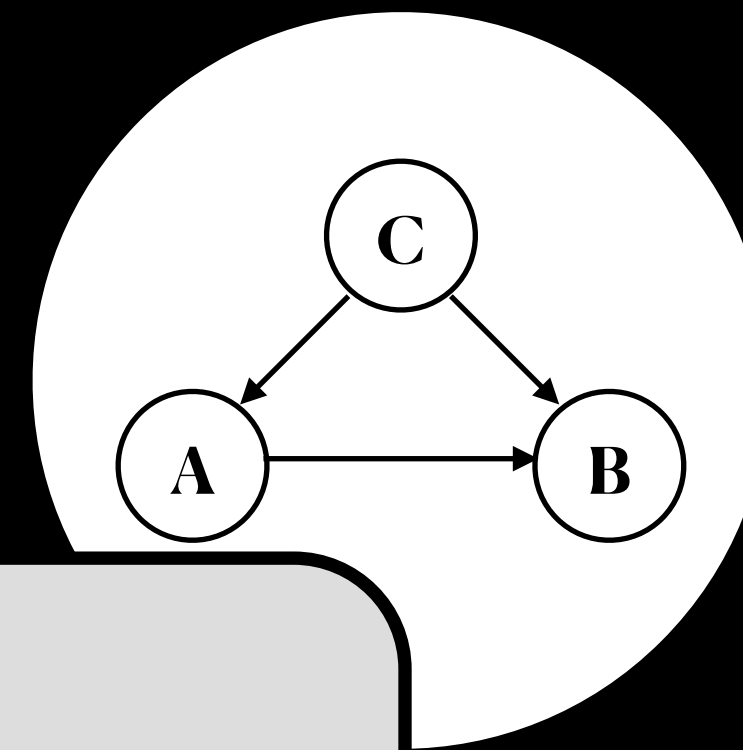
- Associate Professor Deep Learning
- ERC StG & NWO VIDI
- ELLIS Scholar
- Co-director of ICAI QUVA & POP-AART
- Co-founder of Ellogon.AI and LYDS Partners



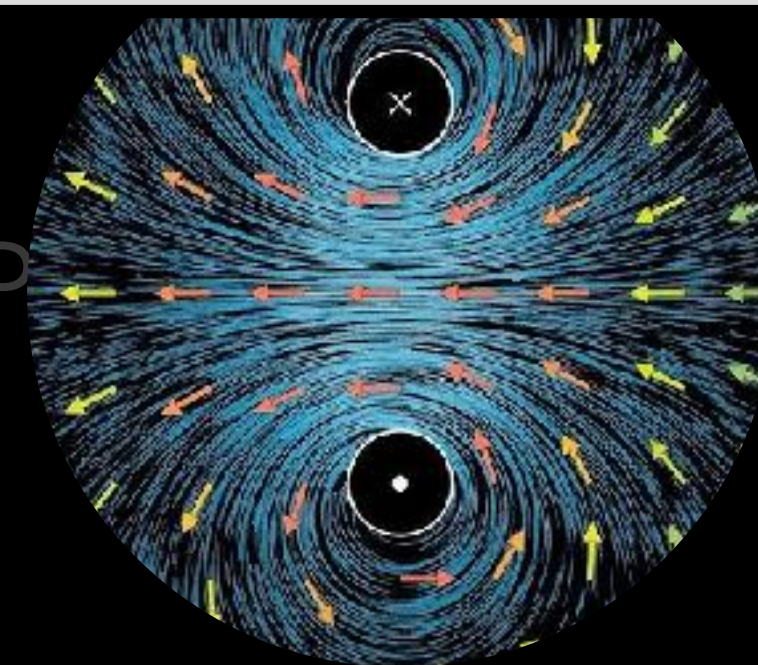
WHO AM I?

Robot Learning

Causal Representation Learning



Dynamical Deep Learning

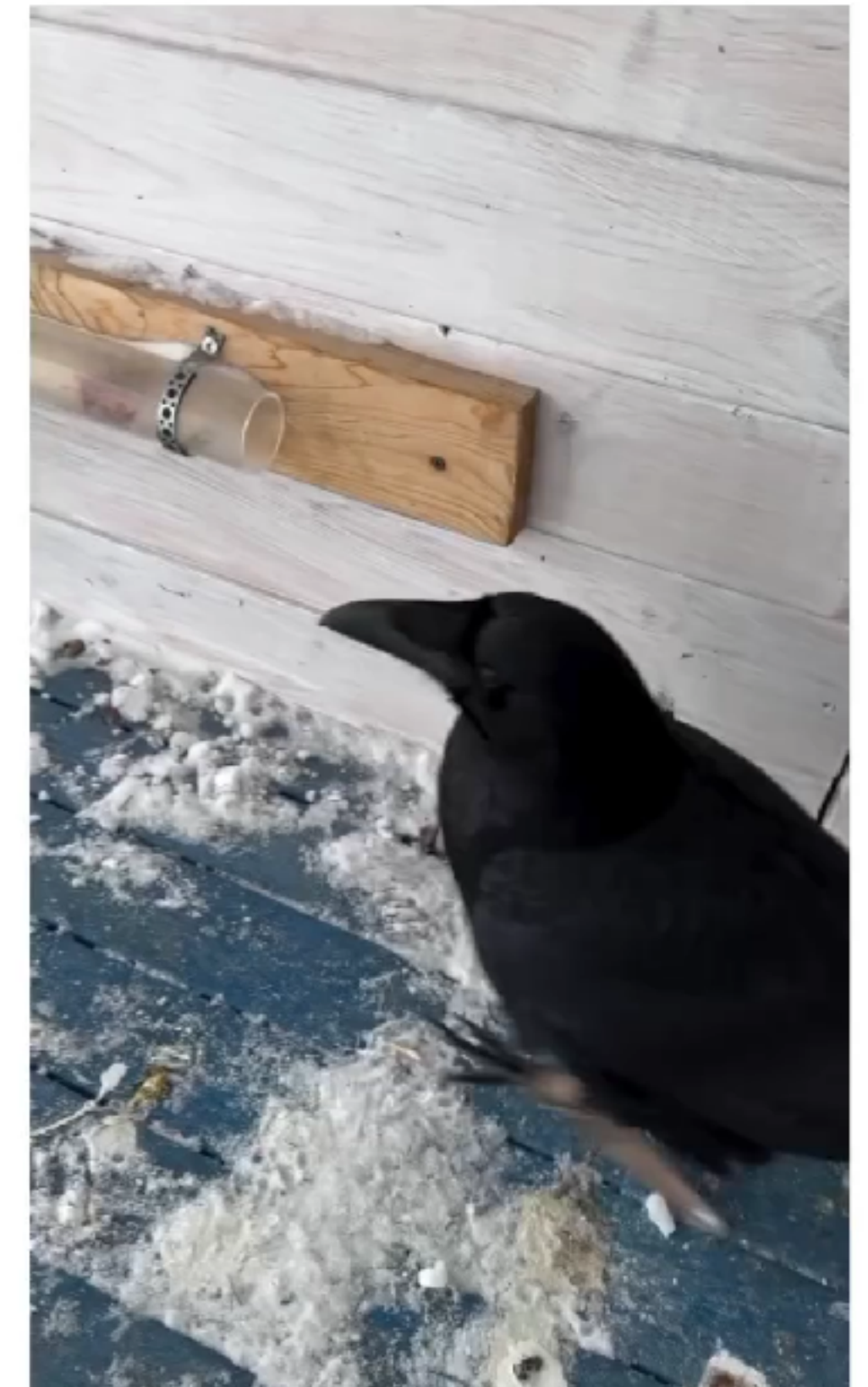


AI & Science


- Associate Professor of Machine Learning
- ERC StG & NWO VIDI
- ELLIS Scholar
- Co-director of ICAI QUVA & POP
- Co-founder of Ellogon.AI

CROW VS FRONTIER MODELS

Problem solving instinct of a crow is just incredible.



ChatGPT 4o >



You are on a bench, and I throw red cubes of sugar inside a transparent cylinder like in the picture. You really wanna get them, what do you do?

🌀 To reach the red cubes of sugar inside the transparent cylinder, a few options come to mind:

1. **Unscrewing the Clamp:** The metal strip holding the cylinder in place is secured with a screw. You could use a screwdriver or a similar tool to remove the screw, loosen the clamp, and slide the cylinder out to get the cubes.
2. **Tilting or Lifting the Cylinder:** If possible, try tilting or lifting the cylinder by loosening it or shifting the pipe without removing the clamp entirely. This might allow the cubes to slide out.
3. **Using a Tool:** If you cannot easily remove the cylinder or shift it, you could use a long tool like a stick or a piece of wire to push the cubes out of the cylinder from one end.

Which approach seems most viable to you depends on your surroundings and the tools available!

📄 🗣️ 🔊 🔄 ⌵

Ok, these are general possibilities. What will you do in this situation. Assume you are a bird and you can only use your beak.

🌀 As a bird, with only my beak to rely on, I would likely use a more creative approach:

1. **Peck at the Clamp or Screw:** I would first try pecking at the metal clamp or the screw, attempting to loosen it. While I might not be able to fully remove the screw, pecking repeatedly could loosen the connection enough for me to shift the cylinder.
2. **Tilt the Cylinder:** If I can't remove the screw, I would attempt to peck at the bottom or side of the transparent cylinder to tilt or knock it slightly, hoping to shake the red cubes loose and make them move towards the opening.
3. **Insert Beak Inside:** If part of the cylinder is open or if I can tilt it enough, I would insert my beak inside and try to push the cubes towards the opening by nudging them, or even pulling one of the cubes out with the tip of my beak.



Claude 3 vs ChatGPT vs Gemini

QUO VADIS AI?

FROM SEEING TO

→ INDUCING PHYSICS & CAUSALITY

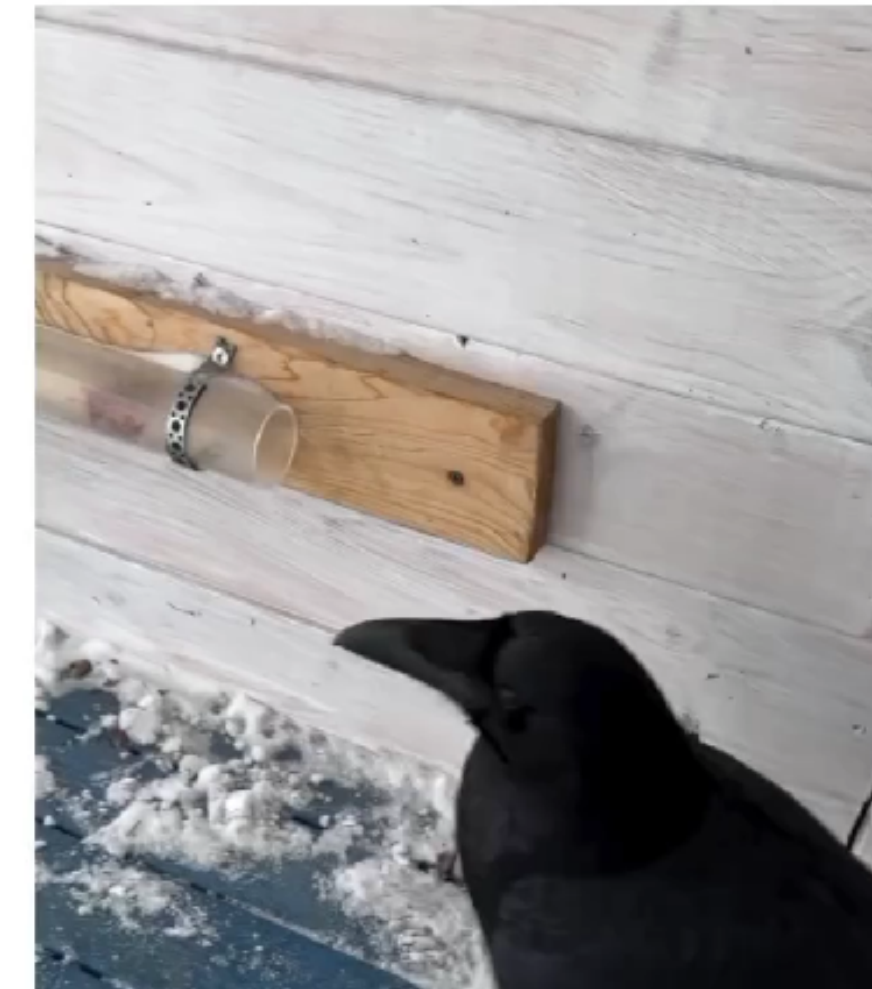
→ SPATIAL MEMORY & NAVIGATION

→ REASONING

→ PLANNING

⇒ INTERACTING WITH REALITY

Problem solving instinct of a crow is just incredible.



Yann LeCun · Following
VP & Chief AI Scientist at Meta
35m · 🌐

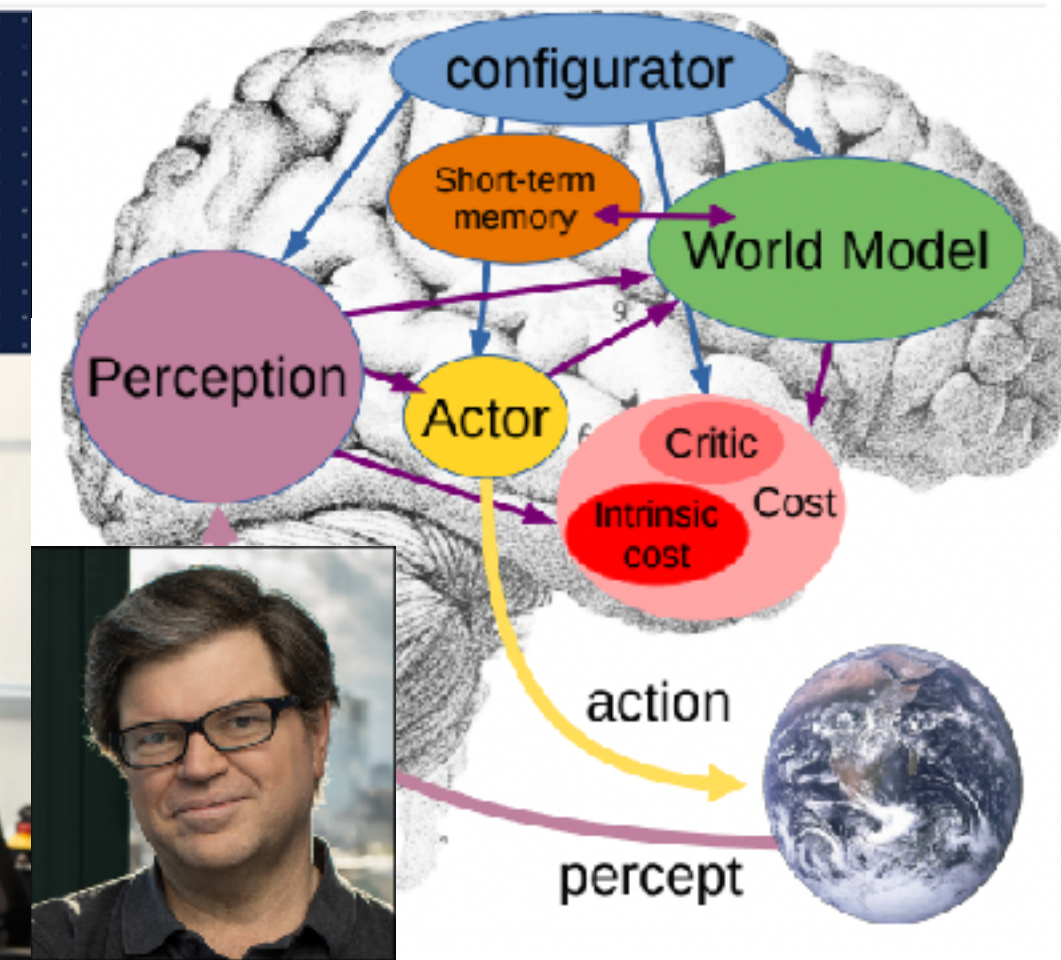
An article in the Wall Street Journal in which I express my opinion on the limitations of LLMs and on the potential power of new architectures capable of understanding the physical world, have persistent memory, can reason and can plan: four features of intelligent behavior that LLMs are incapable of, but that your cat possesses

<https://lnkd.in/e48QigKN>

You and 818 others

37 comments · 33 reposts

ARTIFICIAL INTELLIGENCE
AI is at an inflection point, Fei-Fei Li says
The renowned AI researcher shares her thoughts on the hard problems that lie ahead for the field.
By Melissa Heikkilä November 14, 2023



WITH PHYSICS AND CAUSALITY

GROUNDING ROBOT WORLD MODELS

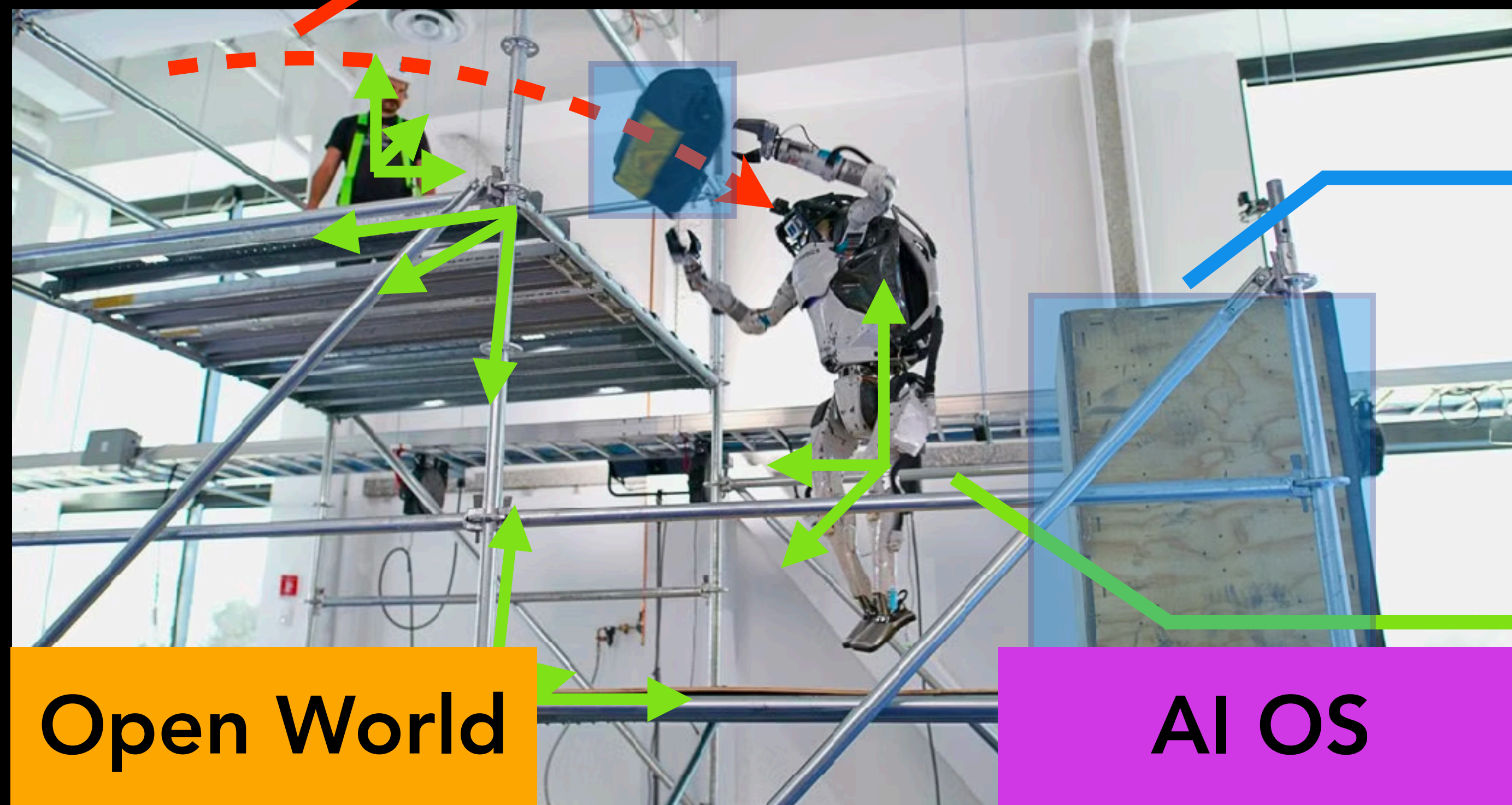
Dynamics/Physics inductive biases

Causal inductive biases

Embodied inductive biases

Open World

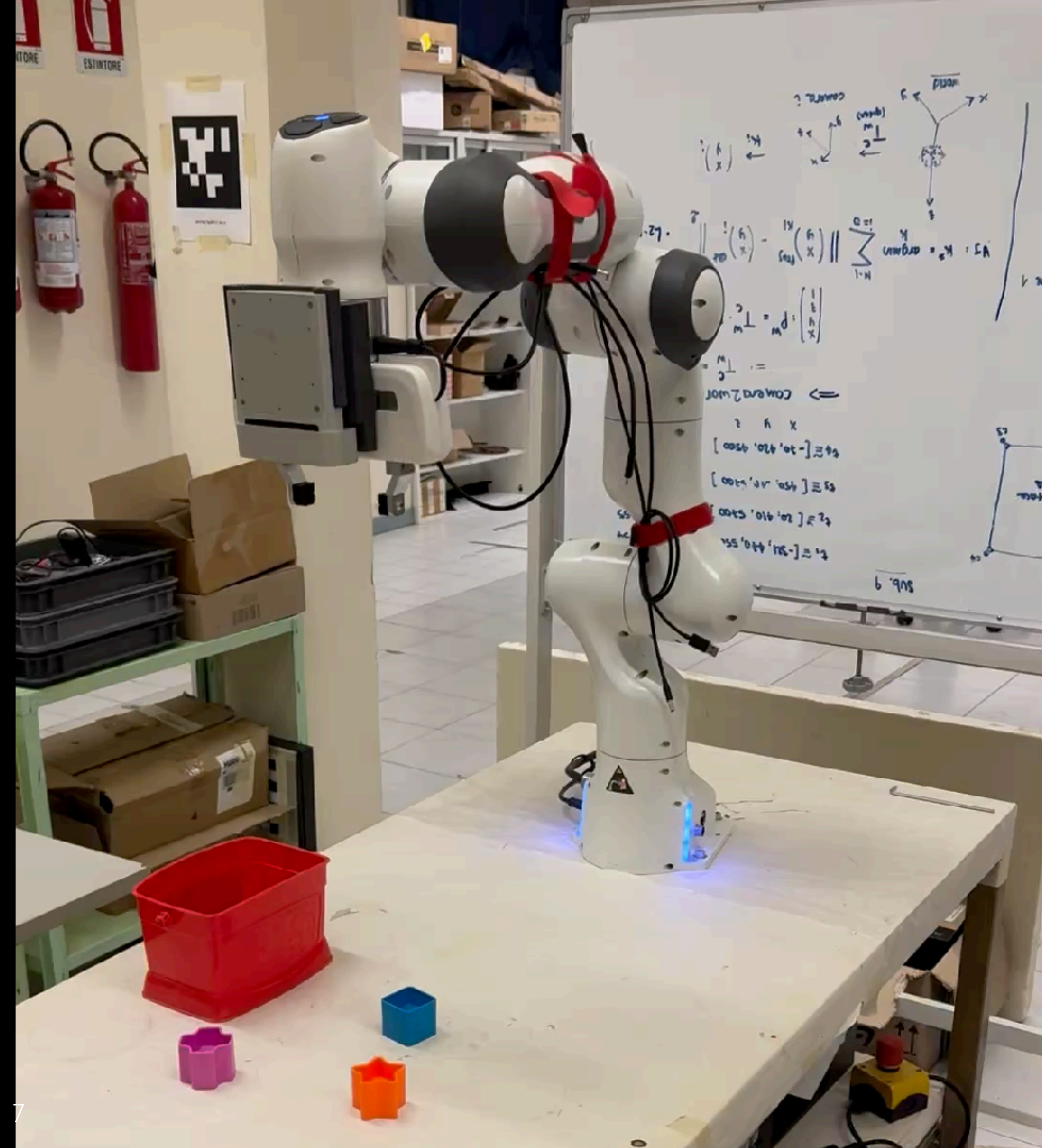
AI OS



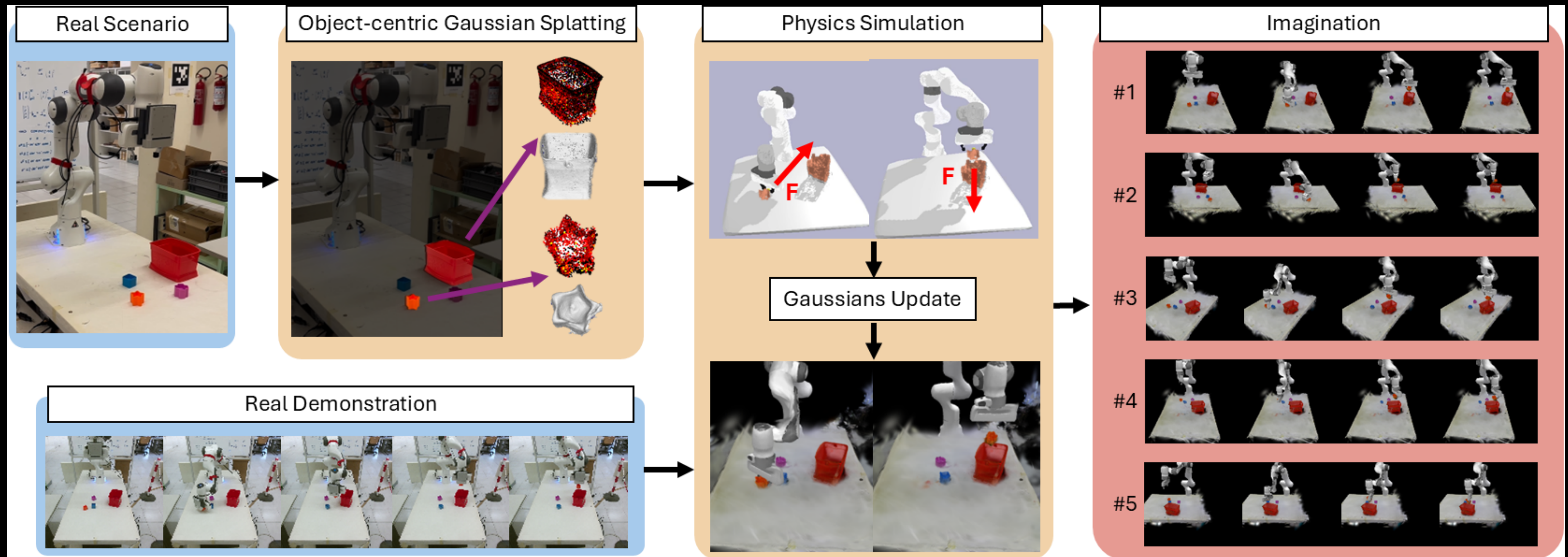
DREAM TO MANIPULATE

COMPOSITIONAL MANIPULATION WORLD MODELS

<https://dreamtomanipulate.github.io/DreMa/>
w. L. Barcellona, A. Zadaianchuk, D. Allegro, S. Papa, S. Ghidoni



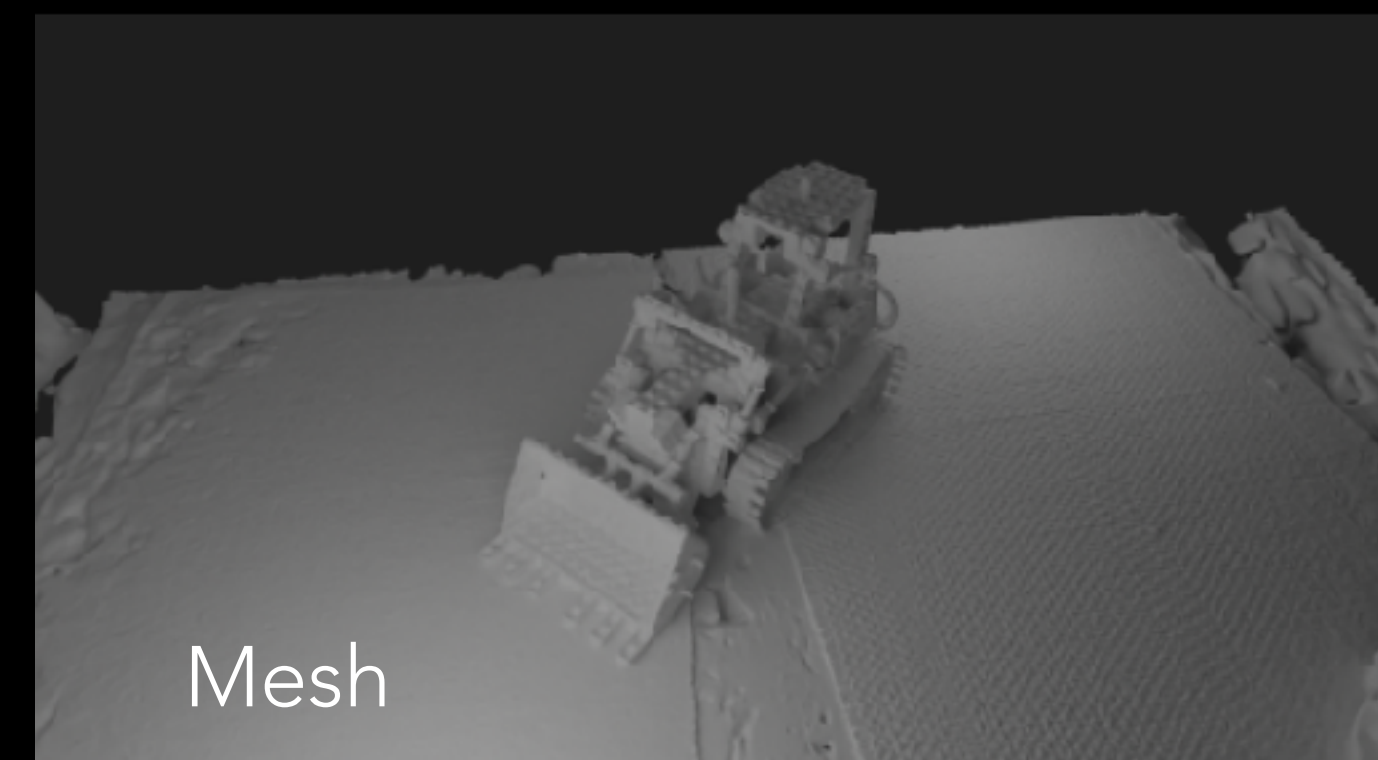
OUR INDUCTIVE BIASES



EXPLICIT GROUNDING == PHOTOREALISTIC RECON@OBJECT-CENTRIC+ EXPLICIT PHYSICS
⇒ COMPOSITIONAL MANIPULATION WORLD MODELS ⇒ IMAGINATION
⇒↑ ROBOT IMITATION LEARNING

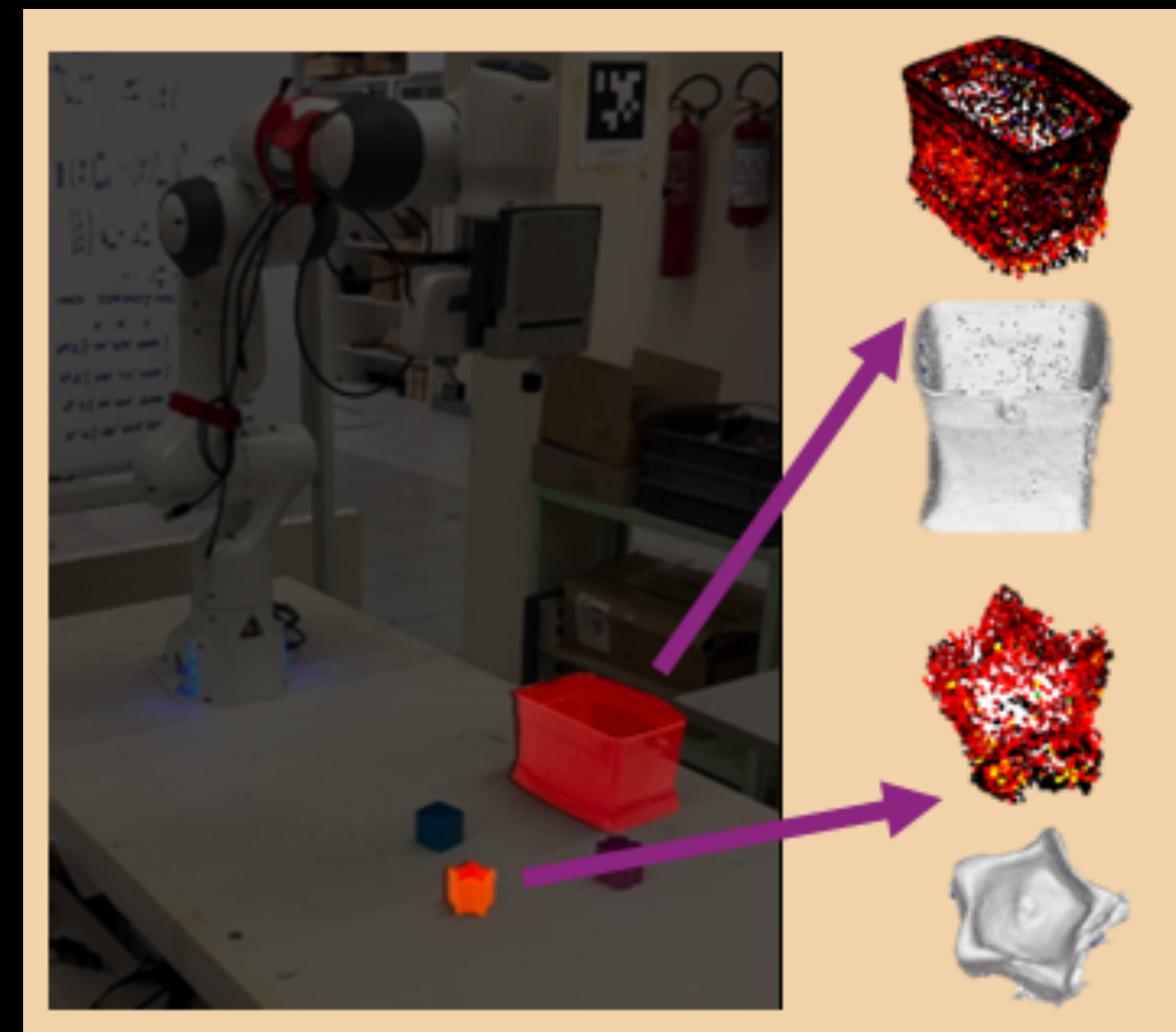
PHOTOREALISTIC RECONSTRUCTION ...

- Gaussian Splatting is like 'sparse 3D pixels'
- Real-time rendering
- High-quality
- Good depth rendering
- Fast training
- Explicitly grounded representation



... MADE OBJECT-CENTRIC WITH OBJECT ASSETS...

- Zero-shot object localization
- Grounded SAM, DEVA, or our VISA¹ & LV-VIS²
- Prompts: "object" & "table"
- Segment and group objects across views

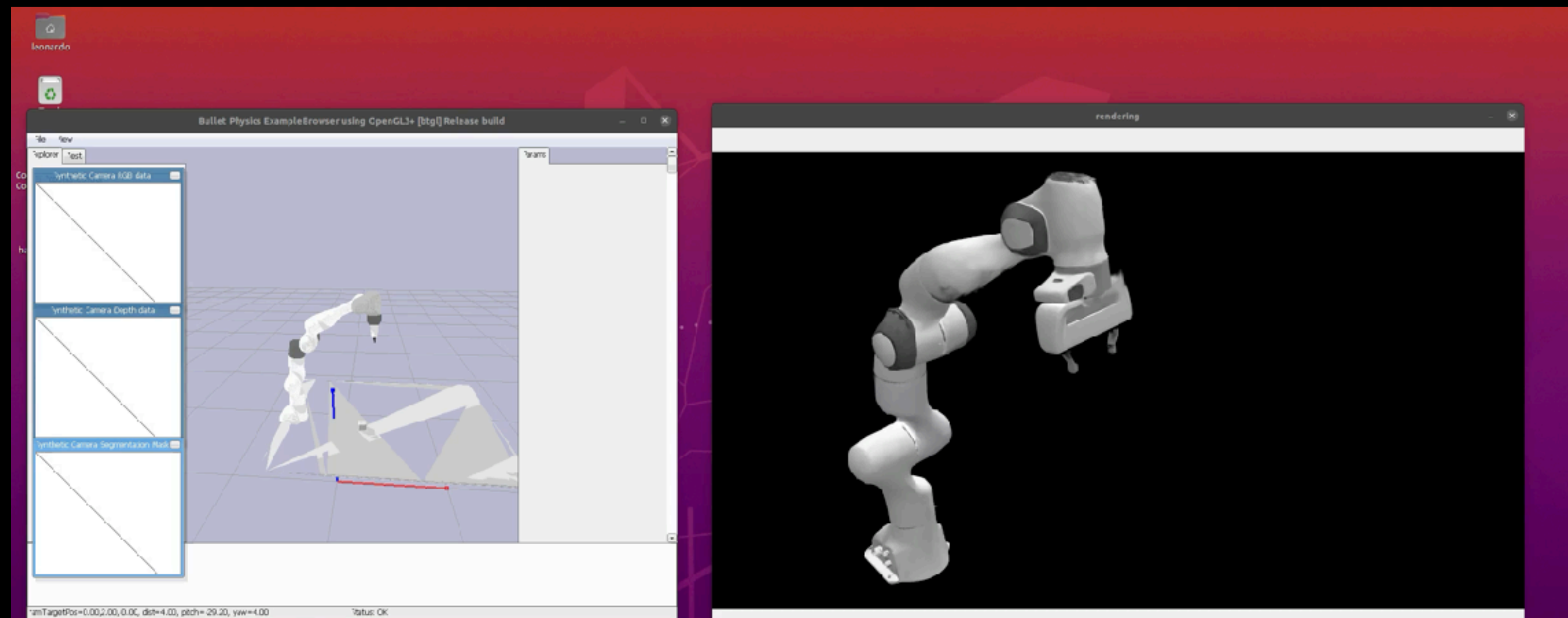


[1] Wang, Gavves et al., Towards Open-Vocabulary Video Instance Segmentation, ICCV 2023

[2] Yan, Wang, Gavves et al., VISA: Reasoning Video Object Segmentation via Large Language Models, ECCV 2024

... WITH "SELF-AWARENESS" ...

- The robot is also an object asset
- Articulated but with known joints
- Movement given by the URDF file, no need to estimate



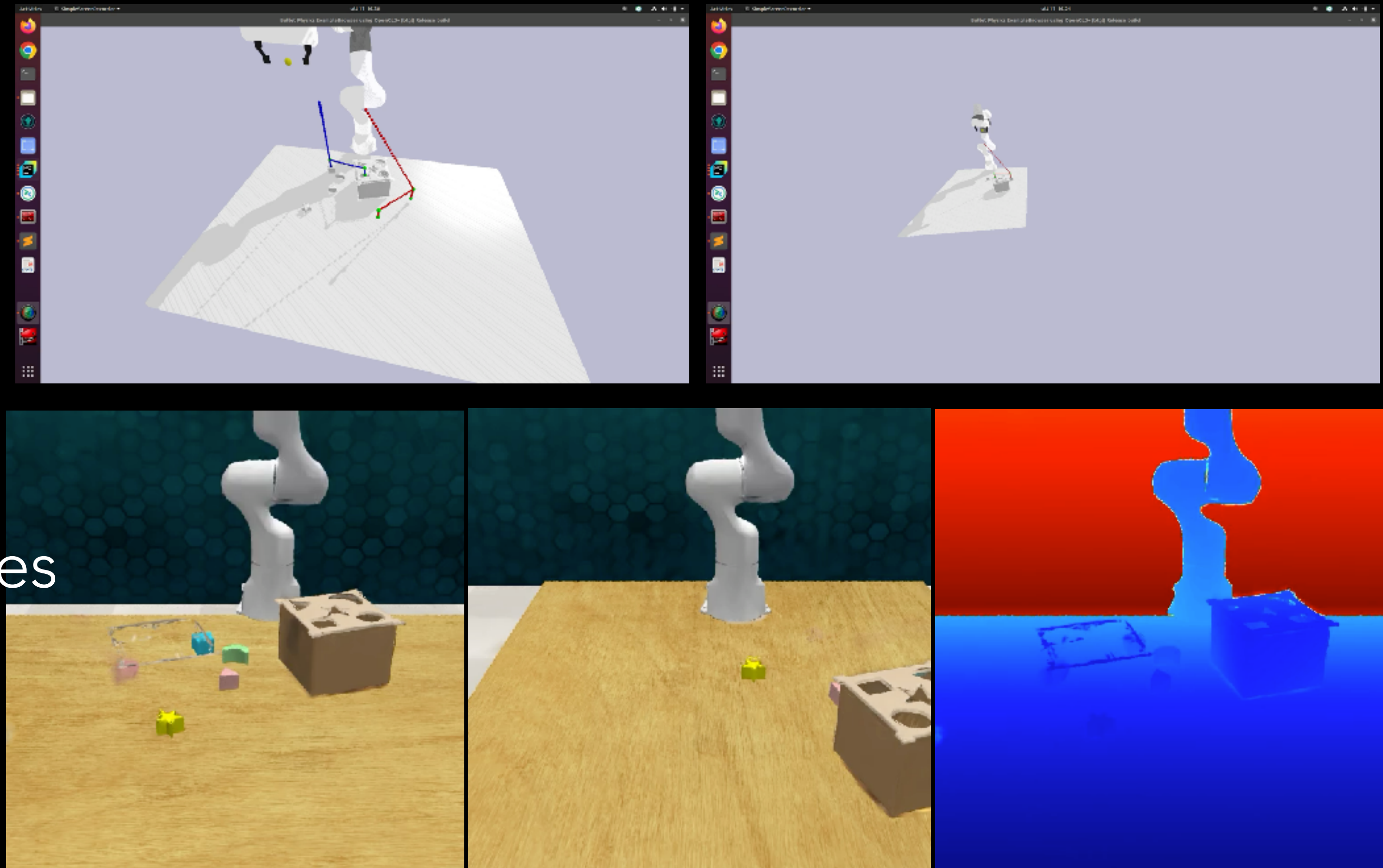
... AND MANIPULABLE WITH PYBULLET ...

- Integrate explicit physics engines
- Manipulate object assets by exerting forces on them
- PyBullet requires mesh grids
- Convert Gaussian Splats to Meshes
- “Decode” effect of manipulations with Gaussian Splatting



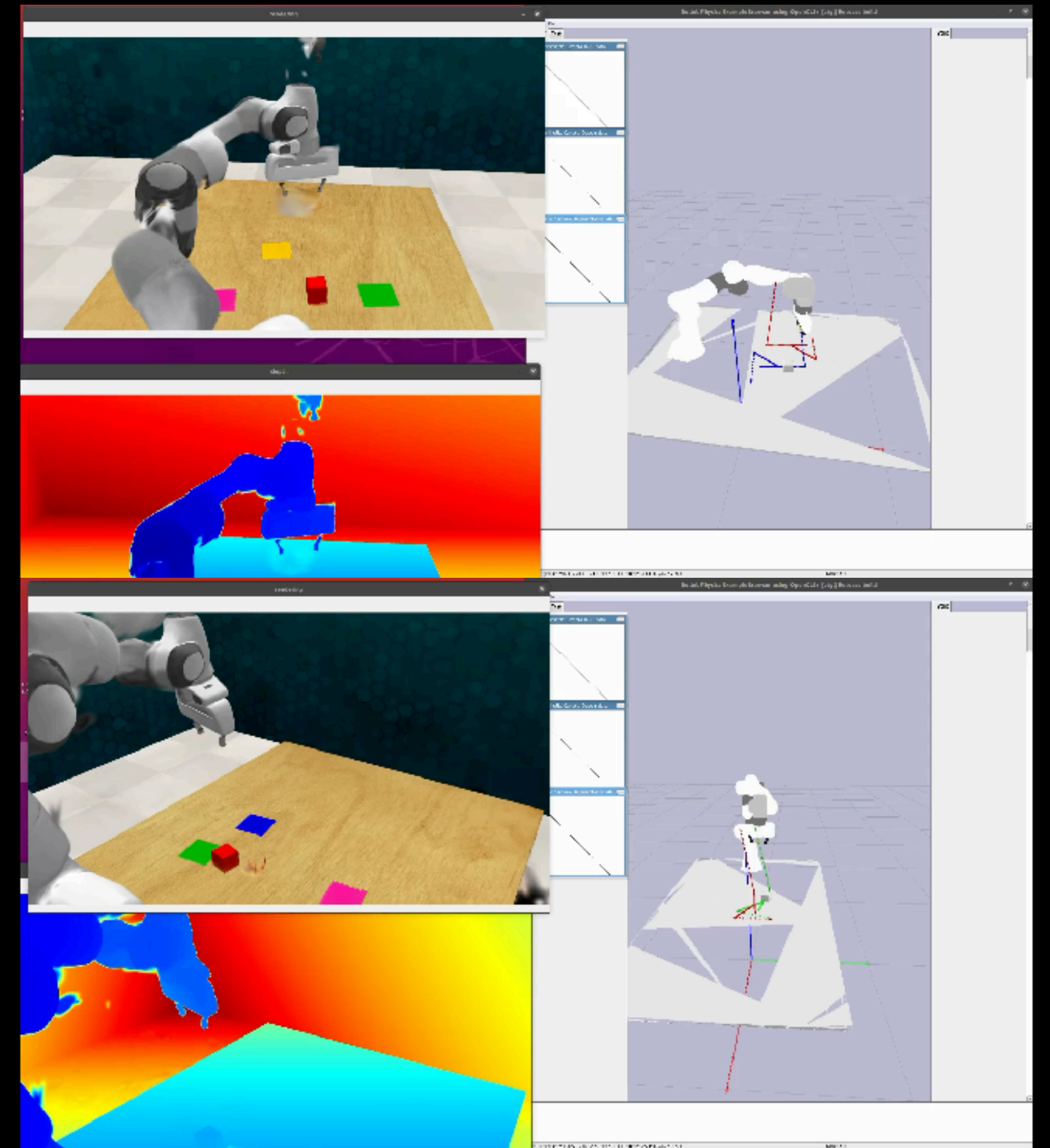
... TO RECONSTRUCT PAST TRAJECTORIES ...

- Play seen trajectories
- And render it from any angle
- “Re-imagining” past experiences



... AND IMAGINE NEW ONES ...

- Since we have a 'digital twin'
- That reconstructs photorealistically
- Understands physics
- And can be intervened with
- We can "imagine" novel trajectories



EQUIVARIANT OBJECT-ROBOT TRANSFORMATIONS

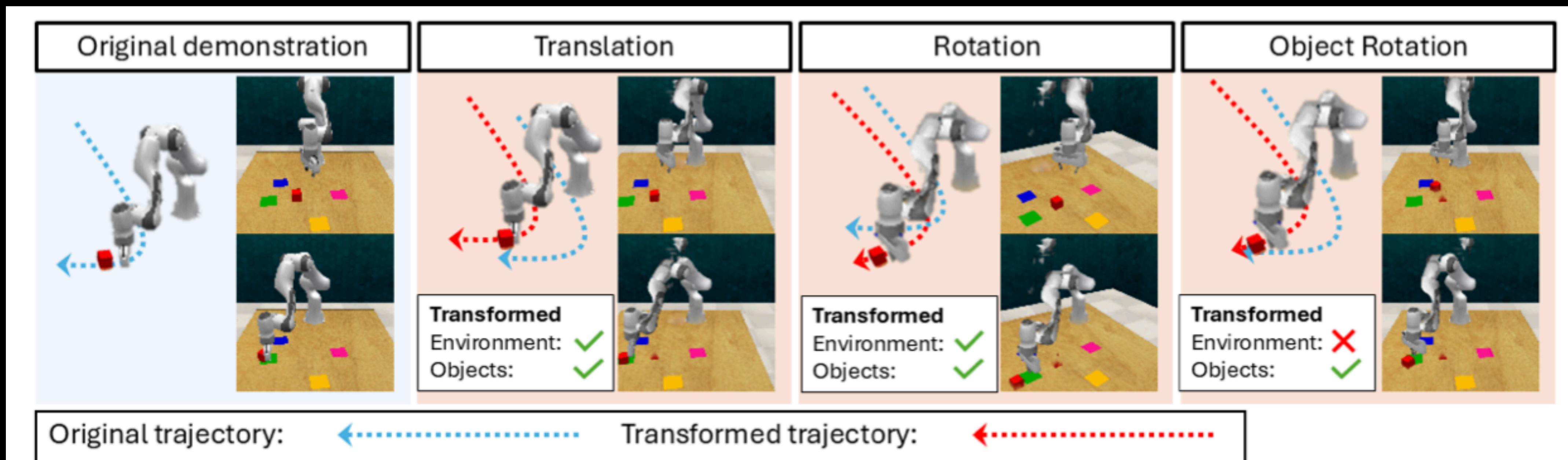


Figure 3: The effect of equivariant translation, equivariant rotation, and the object rotation transformations. Top row: start of demonstration. Bottom row: target of demonstration.

... FOR ONE-SHOT IMITATION LEARNING ...

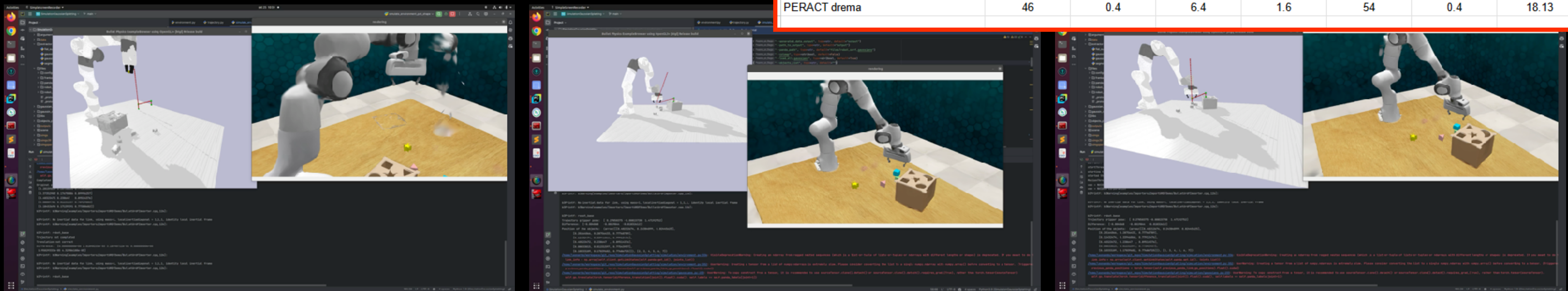
- Single demonstration per variant
- Excluding tasks with articulation
- 60-110 imaginations generated
- Works even with pure imagination

Table 1: Comparison of PerAct (Shridhar et al., 2023) trained on original demonstrations to DREMA trained on only imagination demonstrations and the combination of both. The table reports the mean \pm std and maximum success rate over 5 test runs.

	Single-task							
	<i>close jar</i>		<i>place shape</i>		<i>slide block</i>		<i>avg single-task</i>	
	mean \pm std	max	mean \pm std	max	mean \pm std	max	mean	max
PerAct (<i>Original data</i>)	38.4 \pm 0.80	40	6.4 \pm 1.50	8	48.4 \pm 3.20	50	31.1	32.7
DREMA (<i>Imagined data</i>)	41.2 \pm 2.40	46	9.6 \pm 1.50	12	54.4 \pm 2.15	62	35.1	40.0
DREMA (<i>All data</i>)	51.2 \pm 1.60	54	11.2 \pm 1.60	12	62.0 \pm 2.19	66	41.5	44.0

	Multi-task							
	<i>close jar</i>		<i>place shape</i>		<i>slide block</i>		<i>avg multi-task</i>	
	mean \pm std	max	mean \pm std	max	mean \pm std	max	mean	max
PerAct (<i>Original data</i>)	26.0 \pm 3.10	28	7.2 \pm 1.60	10	34.0 \pm 5.06	38	22.4	25.3
DREMA (<i>Imagined data</i>)	28.0 \pm 3.35	32	18.0 \pm 2.83	22	48.0 \pm 1.79	50	31.3	34.7
DREMA (<i>All data</i>)	46.0 \pm 3.58	52	6.4 \pm 3.20	12	54.0 \pm 2.19	58	35.5	40.7

	close jar	place cups	place shape	put groceries	slide blocks	stack block	AVERAGE
RVT2 original four cameras	62	0.4	2.4	8.8	41.2	3.2	19.67
RVT2 original three cameras (val results)	17.5	2.5	7.5	5	50	2.5	14.17
RVT2 drema three cameras (val results)	25	0	15	10	50	10	18.33
PERACT original	26	1.6	7.2	1.2	34	3.6	12.27
PERACT drema	46	0.4	6.4	1.6	54	0.4	18.13



... THAT WORKS EVEN WITH REAL ROBOTS

Table 3: Localization errors.

Task	Error (m)
<i>pick block</i>	0.010
<i>pick shape</i>	0.050
<i>push</i>	0.049
Average	0.038

Table 4: In- and out-of-distribution evaluation with real robots.

	<i>pick block</i>		<i>pick shape</i>		<i>push</i>	
	In distr.	OOD	In distr.	OOD	In distr.	OOD
PerAct	55	50	30	10	40	10
DREMA (All)	90	90	35	30	80	60

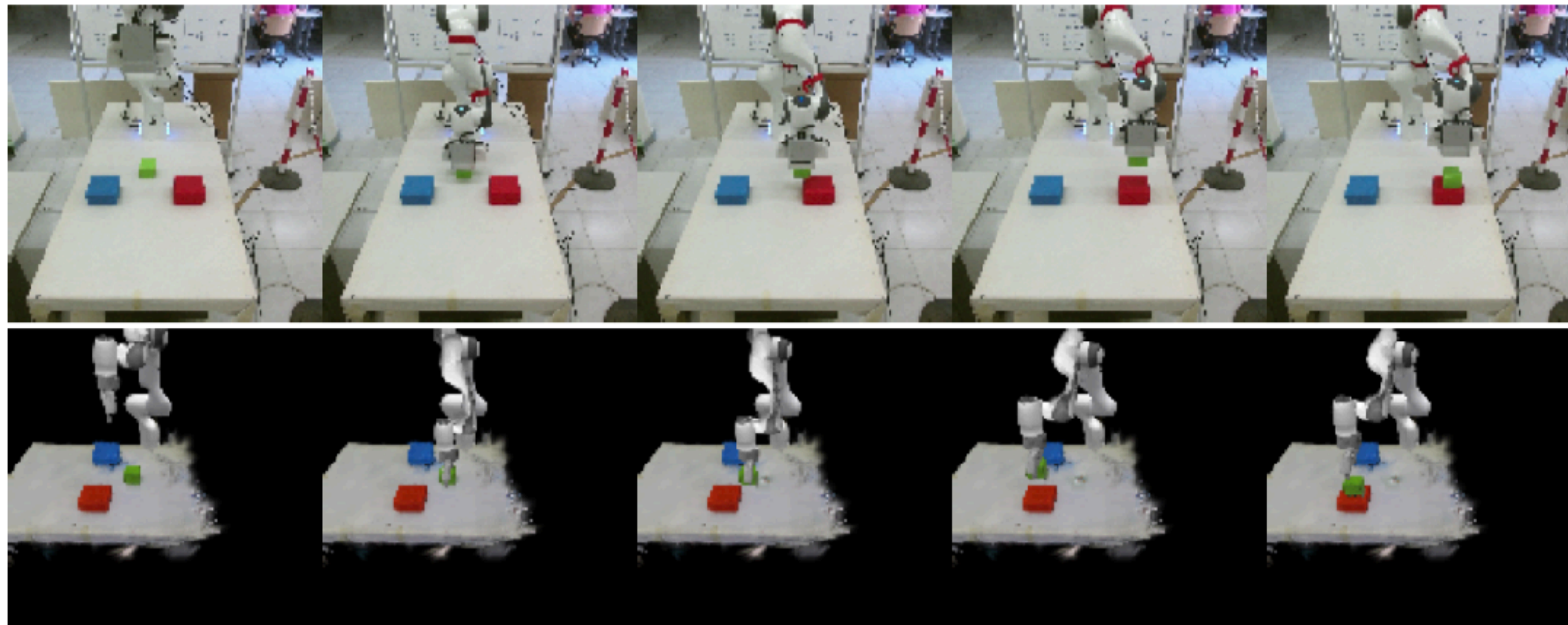
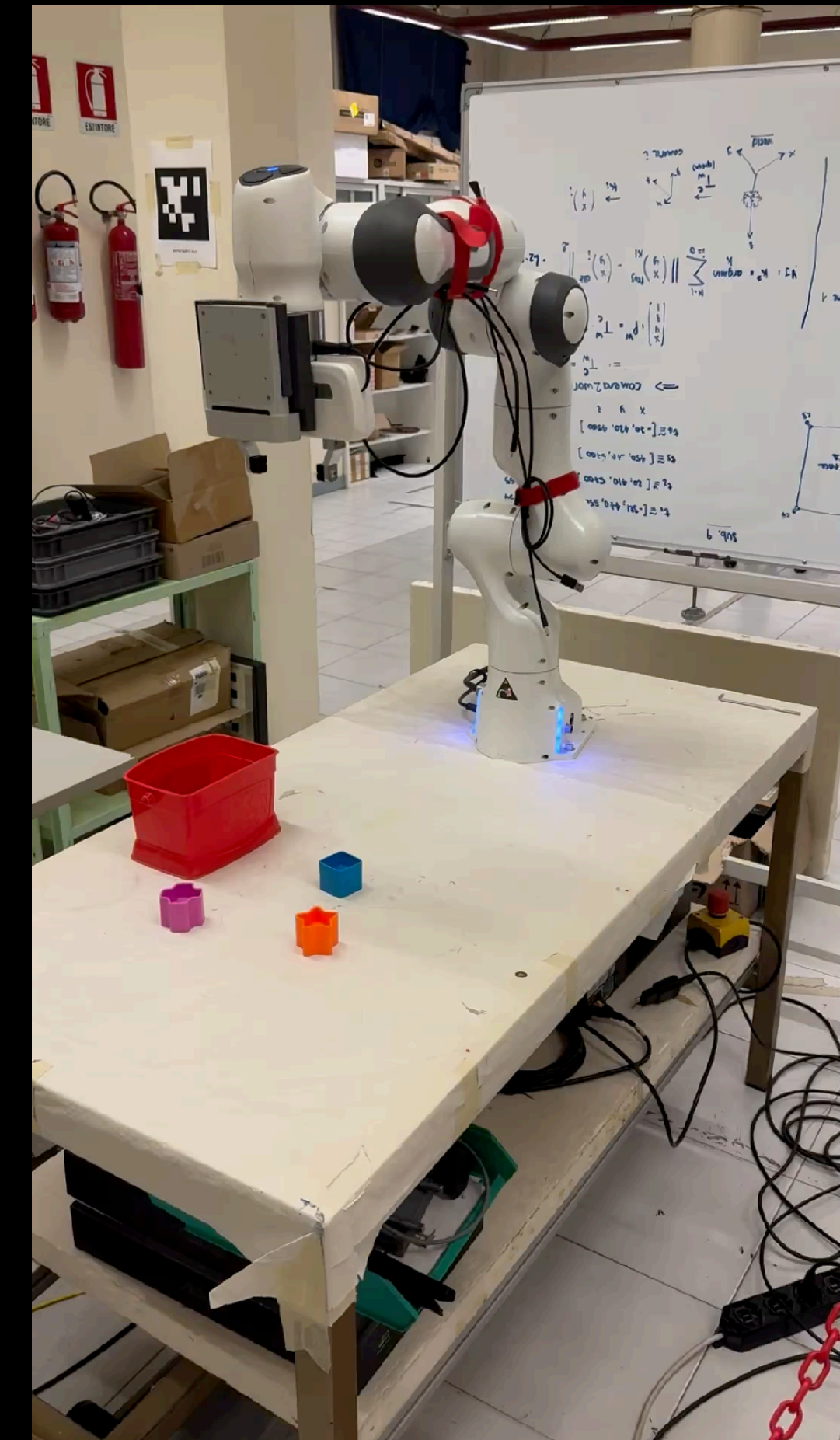


Figure 5: Original (top) and imagined demonstration (bottom) after a 90° rotation transformation.



MORE IMAGINED AUGMENTATIONS HELP

- Simple transformations for now
- Main challenge: make sure demonstrations are valid
- Lower efficacy but better scalability

Table 2: Performance of DREMA trained on single-task demonstrations from different types of transformations. The table reports the mean \pm std and maximum success rate over 5 test runs.

	<i>close jar</i>		<i>place shape</i>		<i>slide block</i>	
	mean \pm std	max	mean \pm std	max	mean \pm std	max
Replay	10.0 \pm 3.10	16	1.2 \pm 0.98	2	26.0 \pm 0.00	26
Object Rotation	25.2 \pm 0.98	26	10.4 \pm 2.65	14	42.0 \pm 0.00	42
Roto-translation	41.2 \pm 2.40	44	10.0 \pm 2.53	14	50.4 \pm 1.50	52
DREMA (<i>All data</i>)	51.2 \pm 1.60	54	11.2 \pm 1.60	12	62.0 \pm 2.19	66

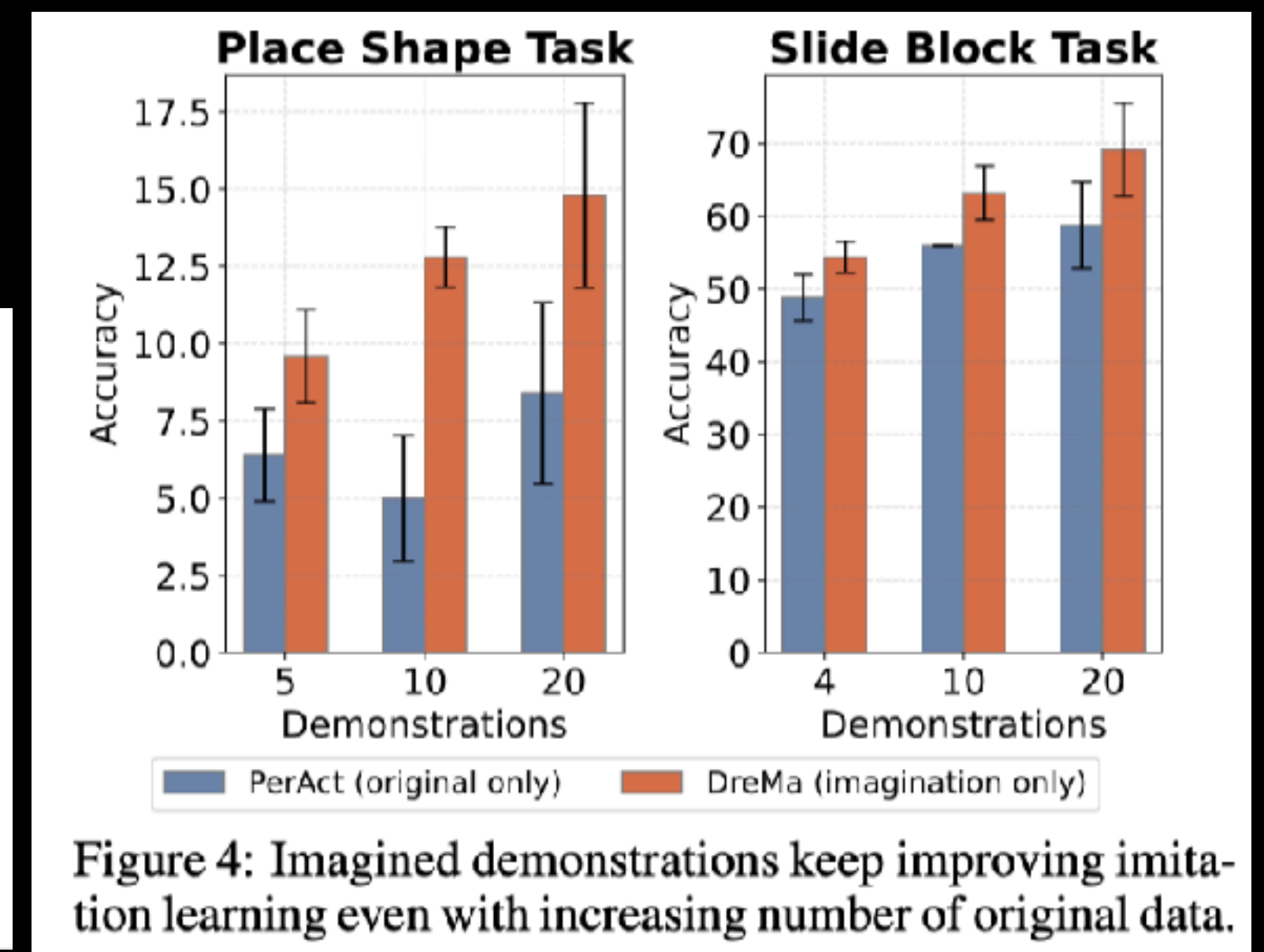


Figure 4: Imagined demonstrations keep improving imitation learning even with increasing number of original data.

Equivariant transformations are complementary ...

... and scale

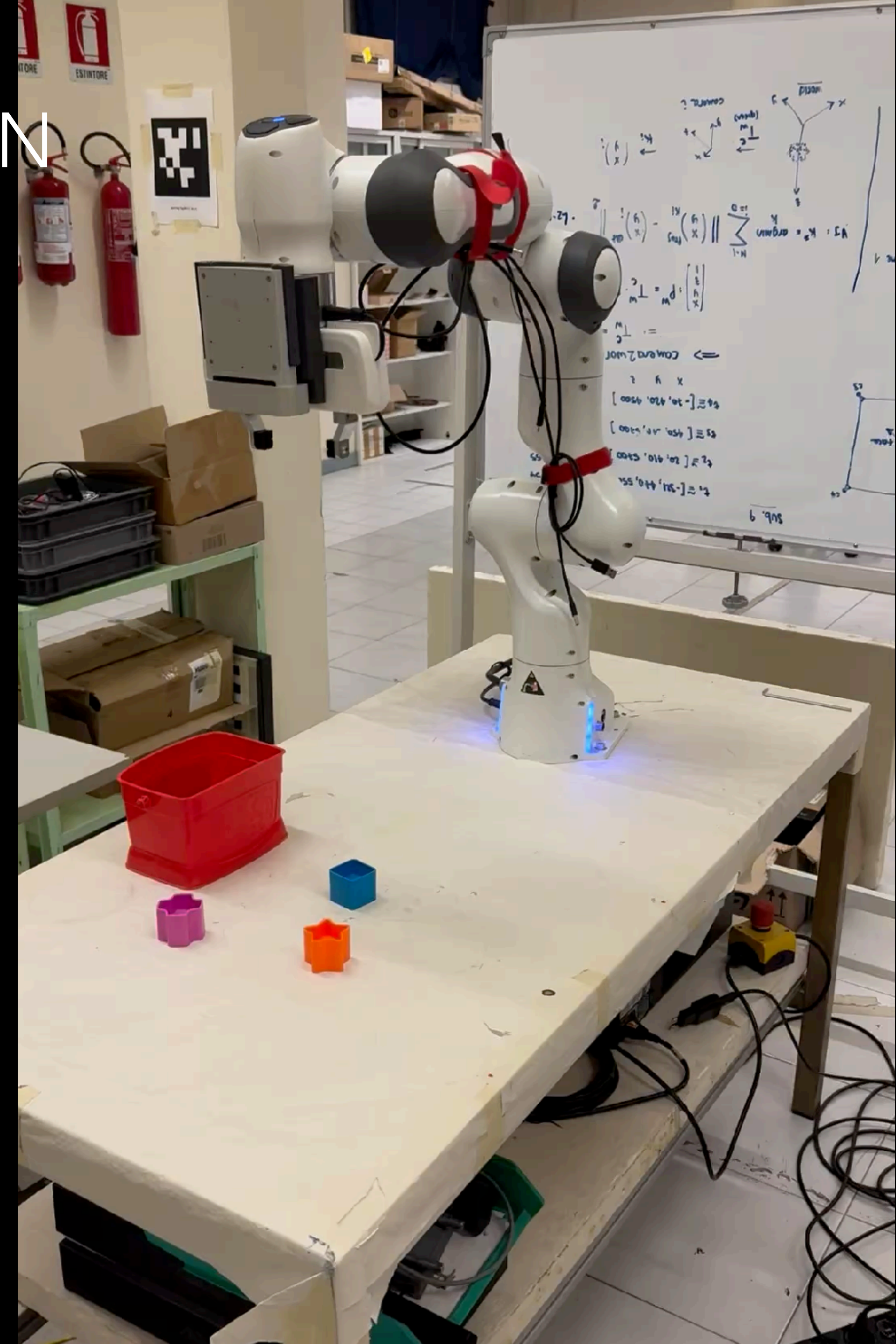
WHAT MAKES IT **NOT** A WORLD MODEL?

- Not end-to-end yet
- Dynamics are not learned
- In fact, not much learning (from us) yet
- BUT, the idea is not to return to feature engineering
- Start with grounding explicitly
- Then everything else neural

The image illustrates the UniSim framework through a collage of various scenes and diagrams. At the top, a grid of images shows diverse environments, with a globe in the center labeled "UniSim". Below this, three diagrams illustrate the learning process: "World Model Learning" (a sequence of states), "Learning Value and Actor Networks" (a robot interacting with a goal), and "Environment Interaction" (a stack of environment states). At the bottom, four photographs show robots performing tasks: "A1 Quadruped Walking", "UR5 Multi-Object Visual Pick Place", "XArm Visual Pick and Place", and "Sphero Ollie Visual Navigation".

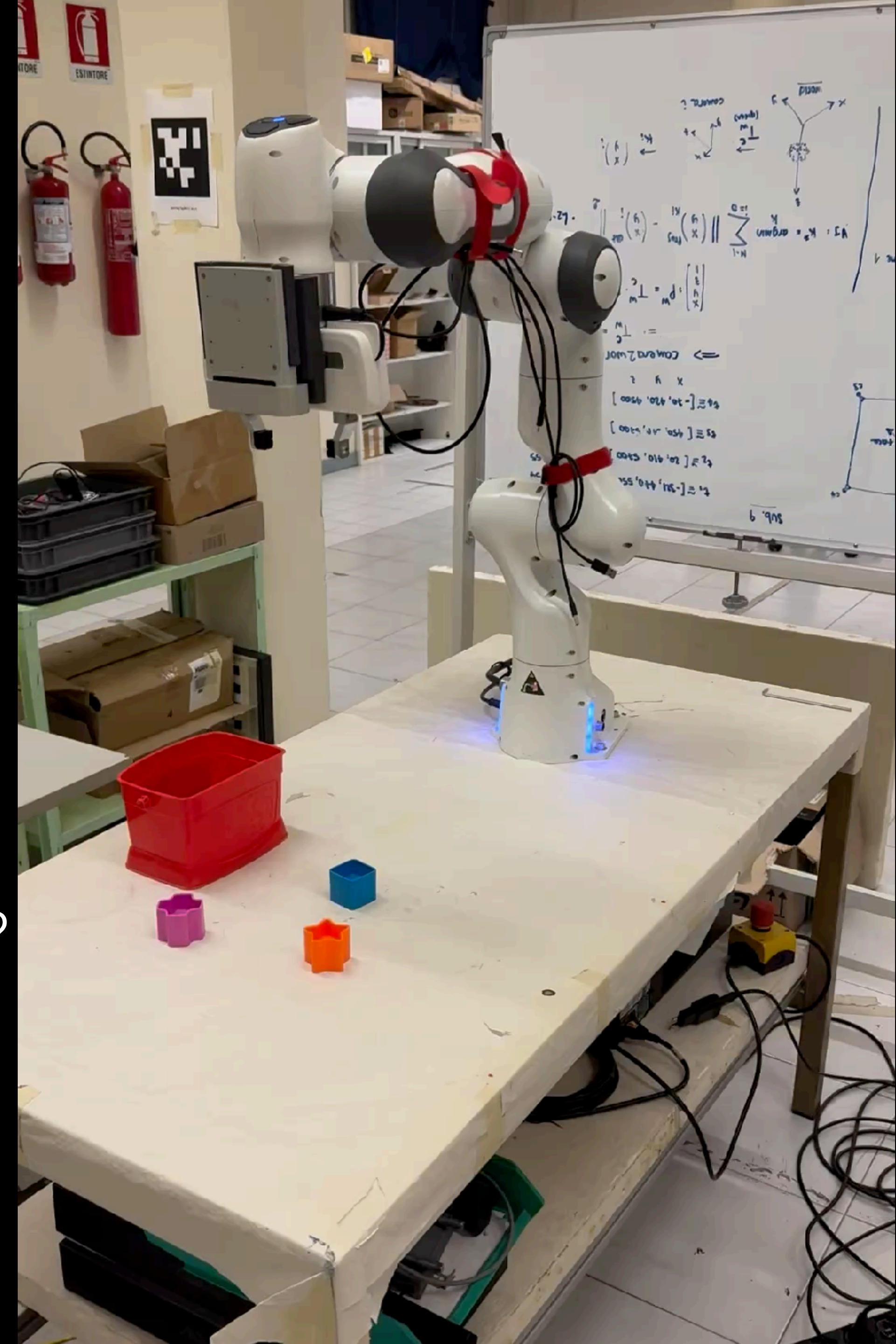
LEARNING & GENERALIZATION

- For one, add representations to object assets
- Learn (fine-tune) on observed trajectories
- Learn with differentiable physics
- Learn with partial observability
- Learn with manipulations
- Learn dynamics beyond physics (eg, causality, third-person actors, theory of mind, ...)
- Learn with dynamic scenes



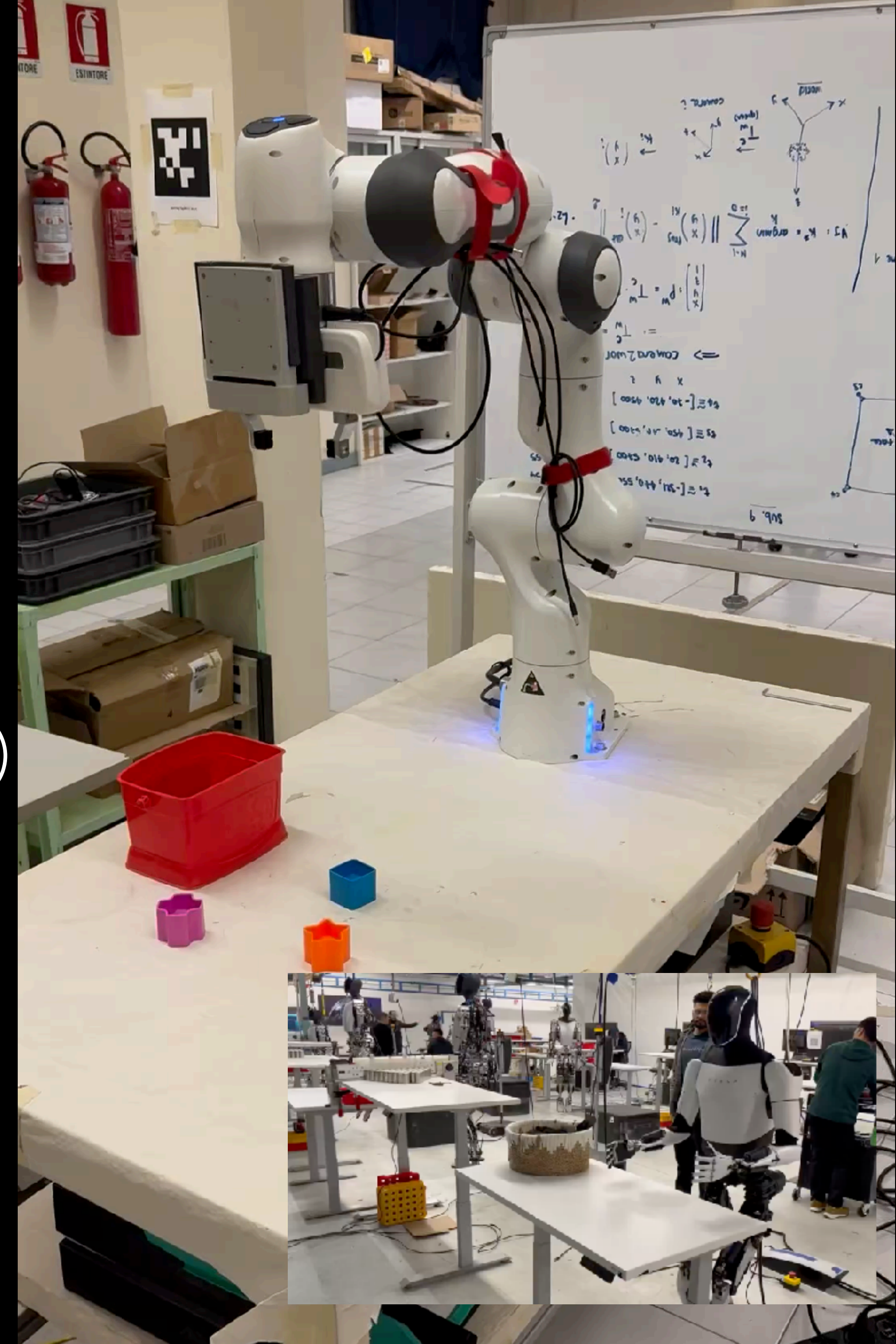
BEYOND IMITATION: LEARNING RL POLICIES

- Why stop with imitation learning?
- Grounded imagination & reasoning opens up lots of exciting possibilities
- Maximizing future reward in future imagination?
- ...



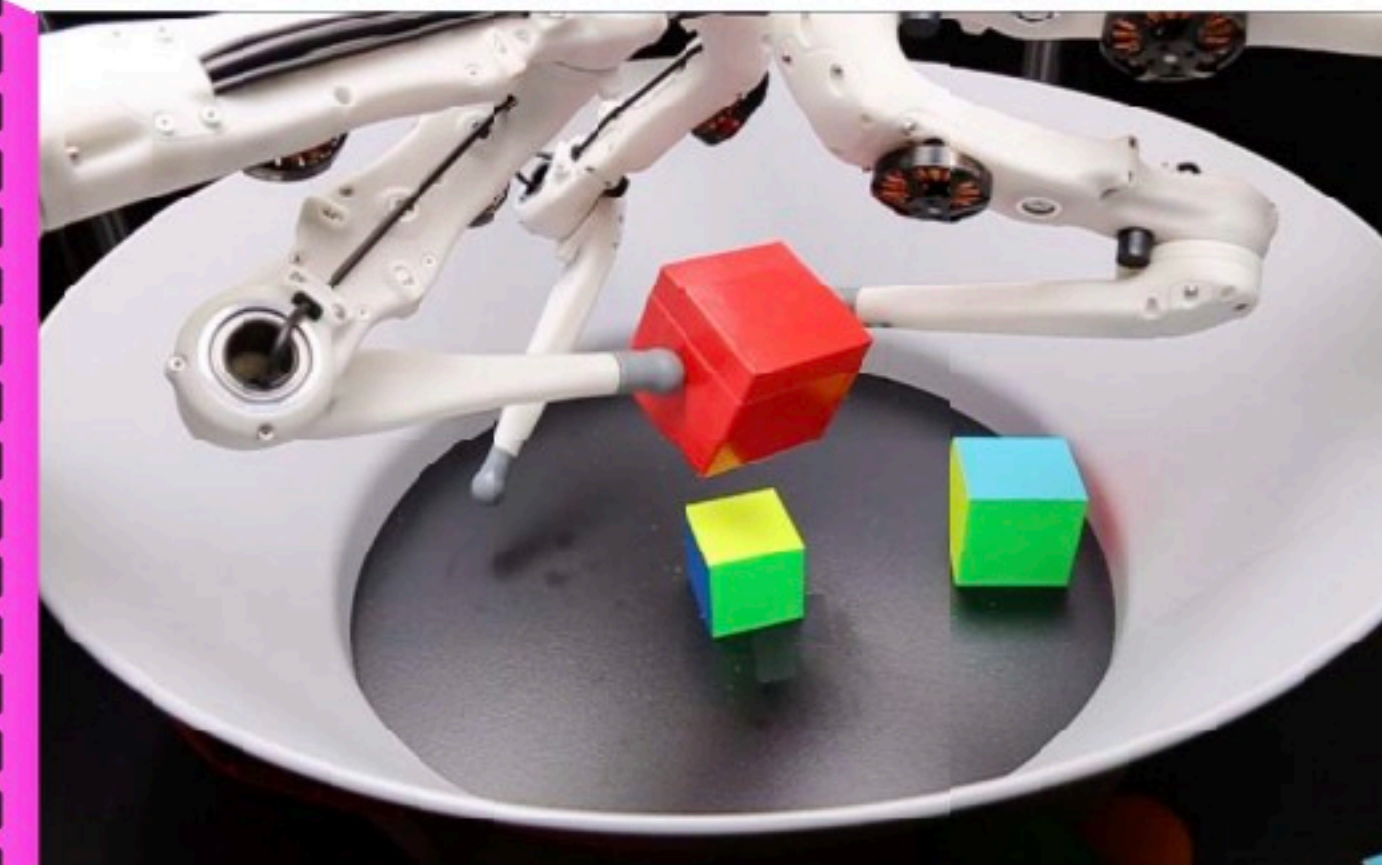
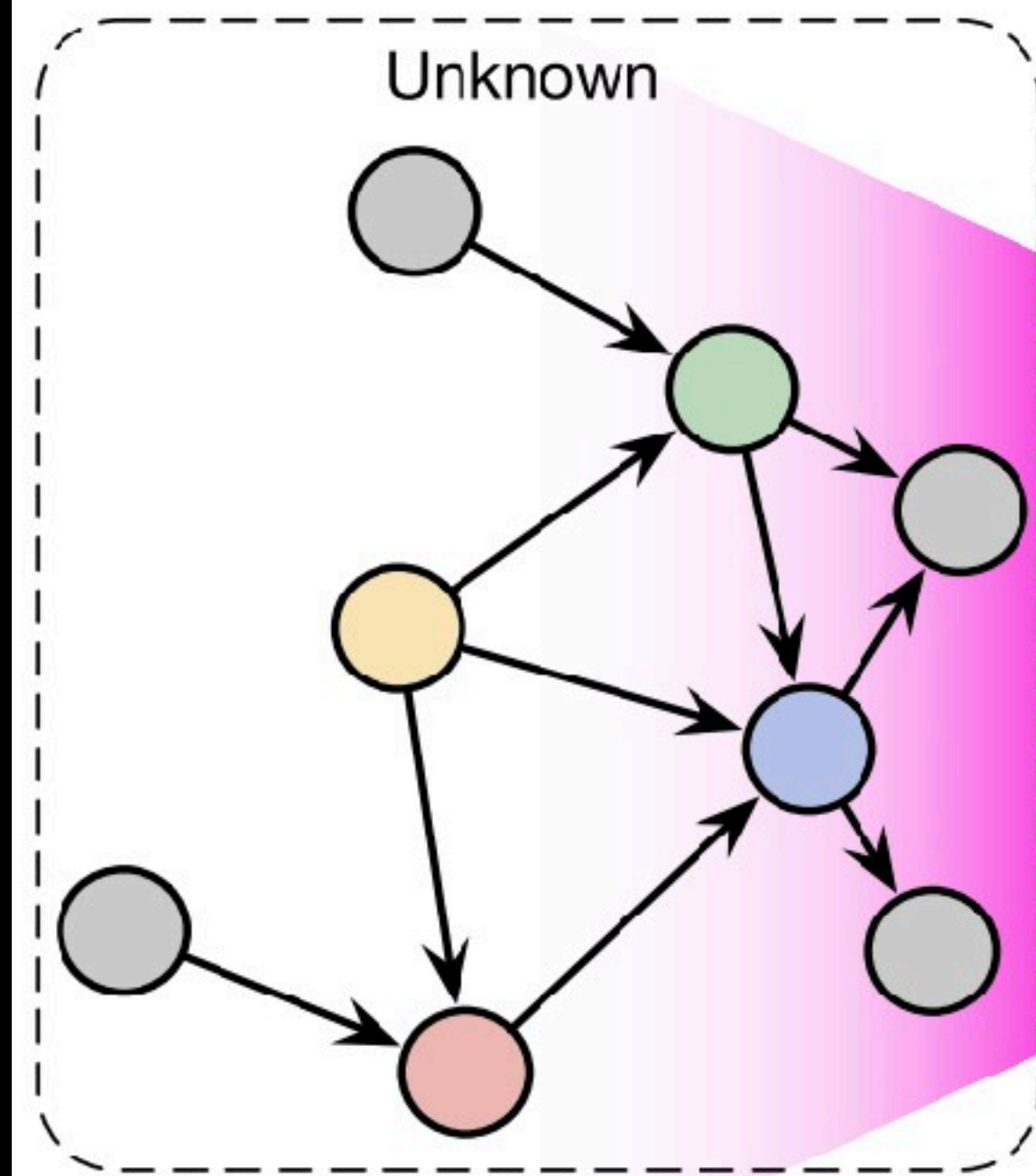
SKY IS THE LIMIT

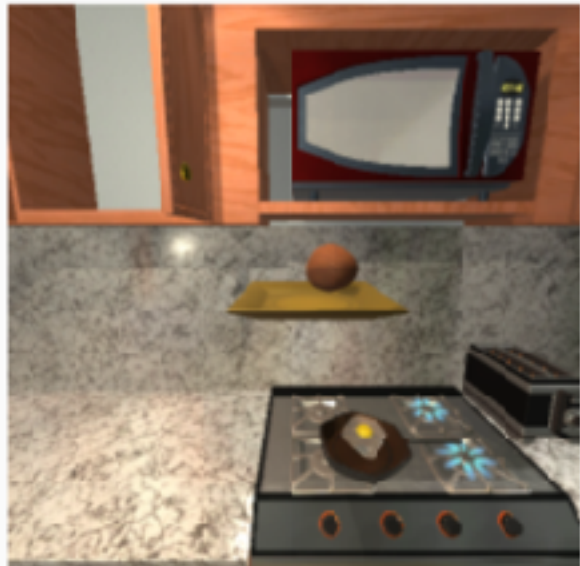


- Articulated objects (identifying joints)
- Deformable objects (with complex physics engines)
- Closed feedback loop ('eye-hand coordination')
- Physical parameter identification (friction, etc)
- Safety and interpretability
- Stochasticity (many possible futures)



LIPPE ET AL, ICLR, ICML, UAI, 2022-23

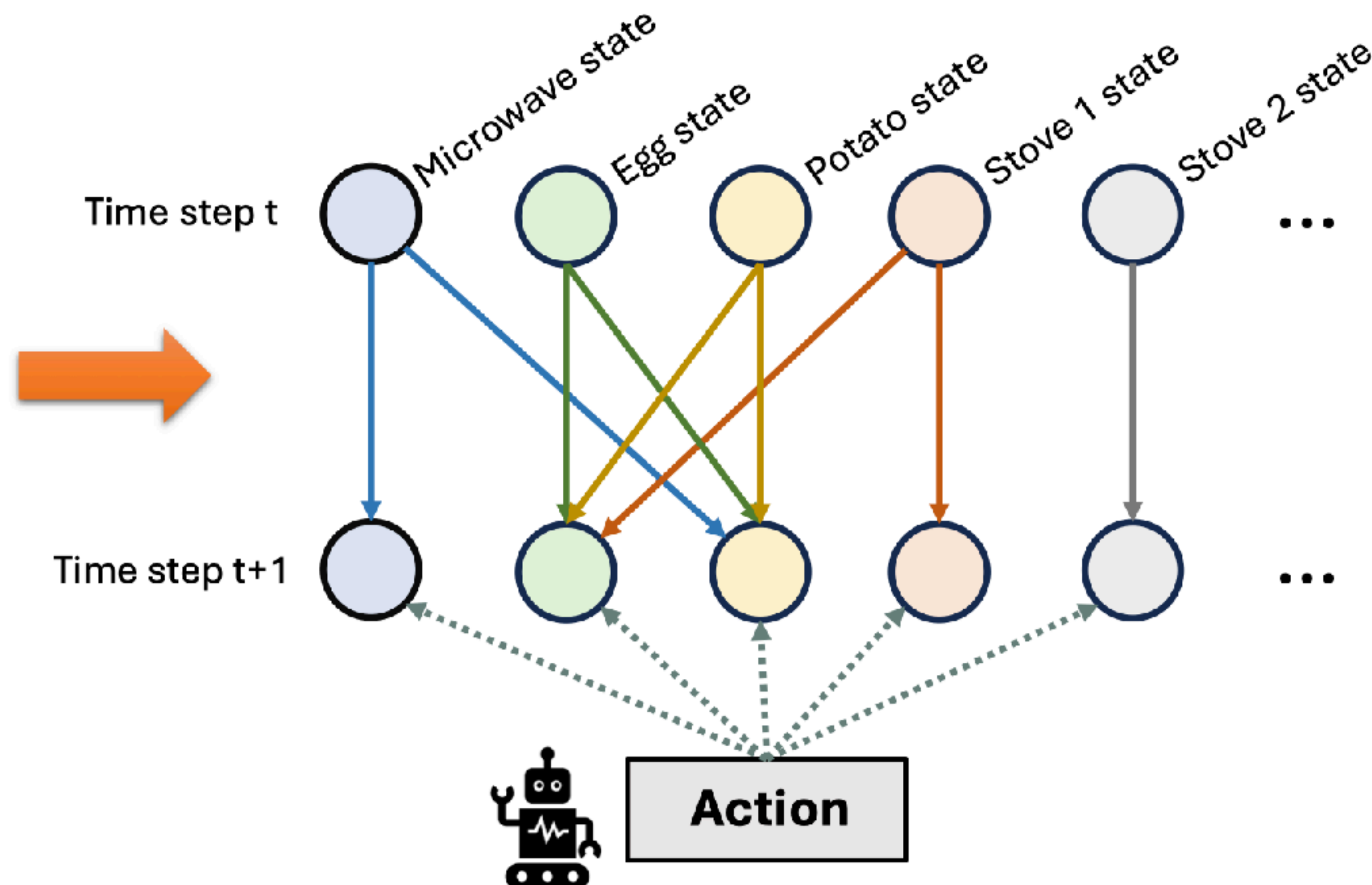
CAUSAL INDUCTIVE BIASES



Input image 1	Input image 2	Generated Output	Latents from image 2
			Microwave Active Stove (front-left)

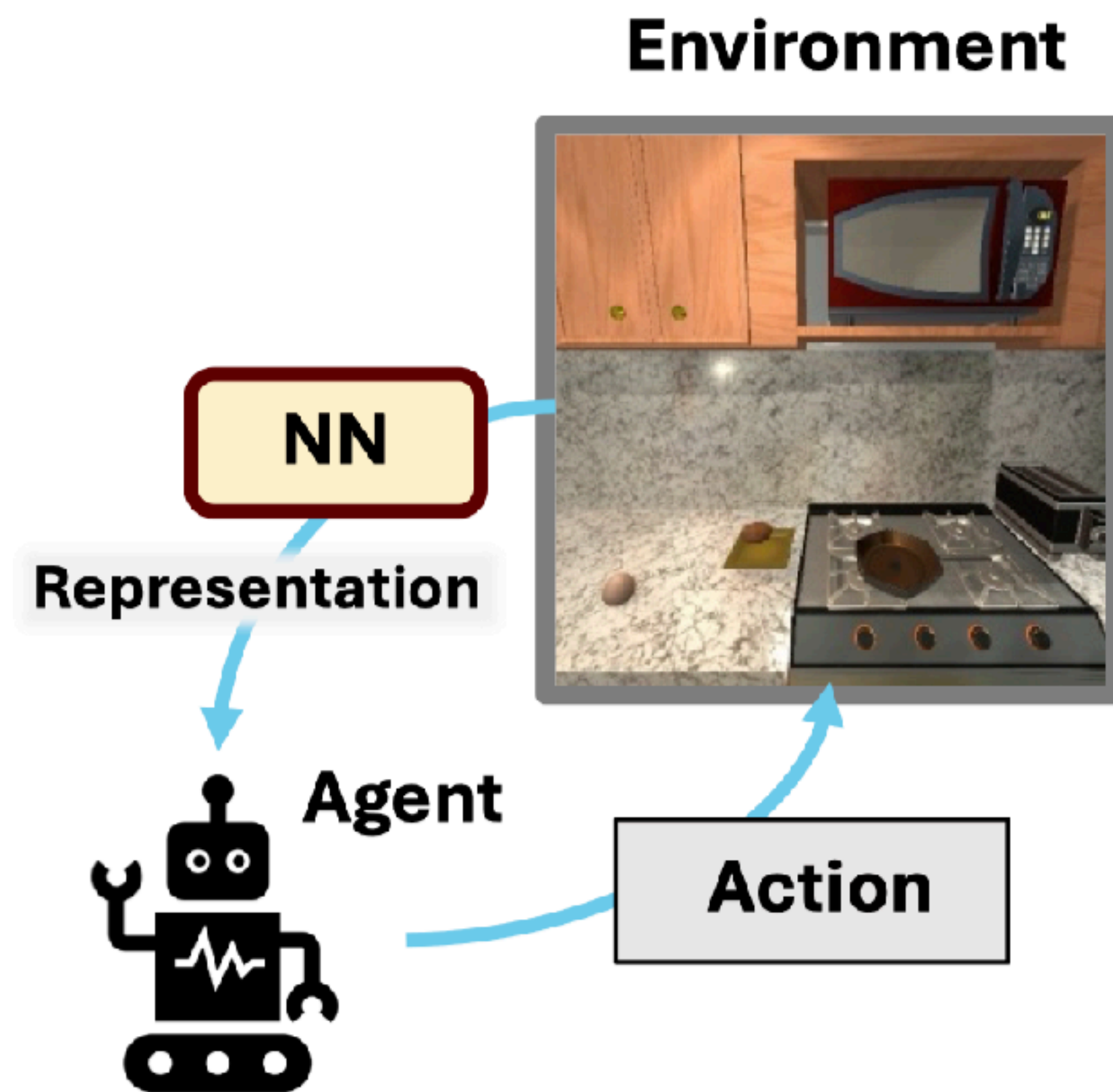
Manipulating Image 1 by turning on the Microwave and the front-left Stove. Note the egg staying uncooked despite the stove being turned on, which the model has never seen in training and shows BISCUIT's ability to perform novel interventions.

TEMPORAL CAUSAL REPRESENTATION LEARNING



<https://philippe.github.io/>

TEMPORAL CAUSAL REPRESENTATION LEARNING



Representation Learning Tasks

What are the causal variables of the environment?

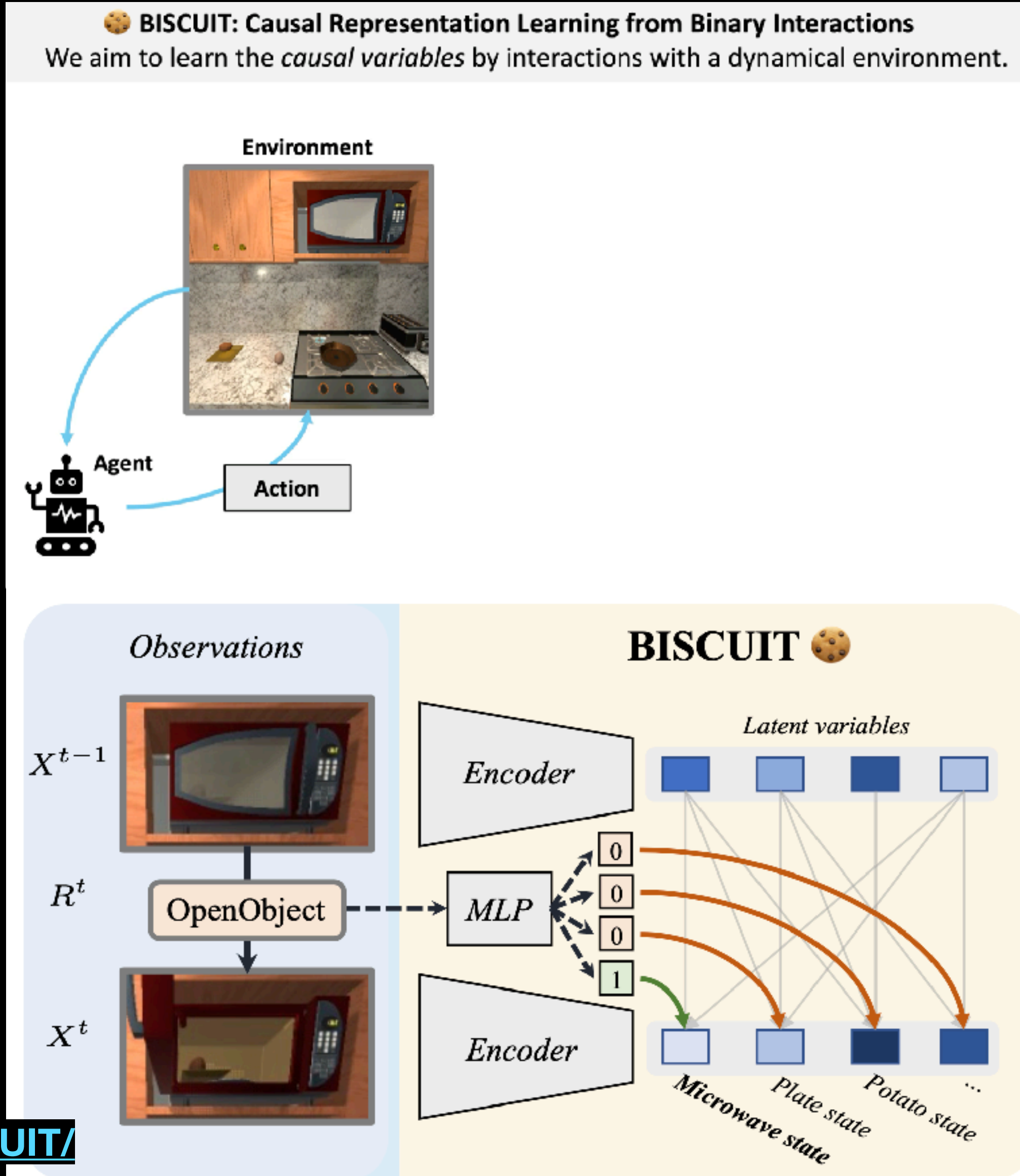
How do they interact with each other?

How can the robot agent intervene on causal variables?

<https://philippe.github.io/>

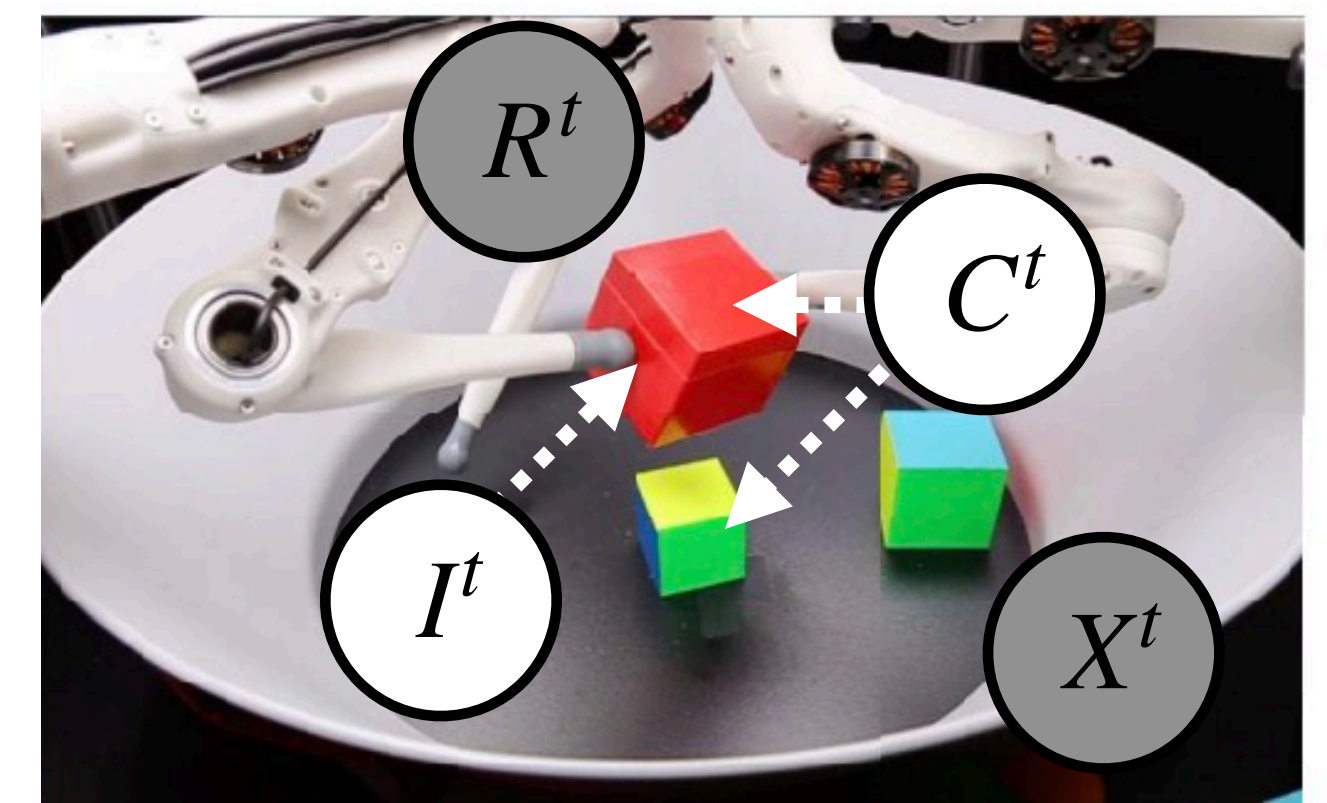
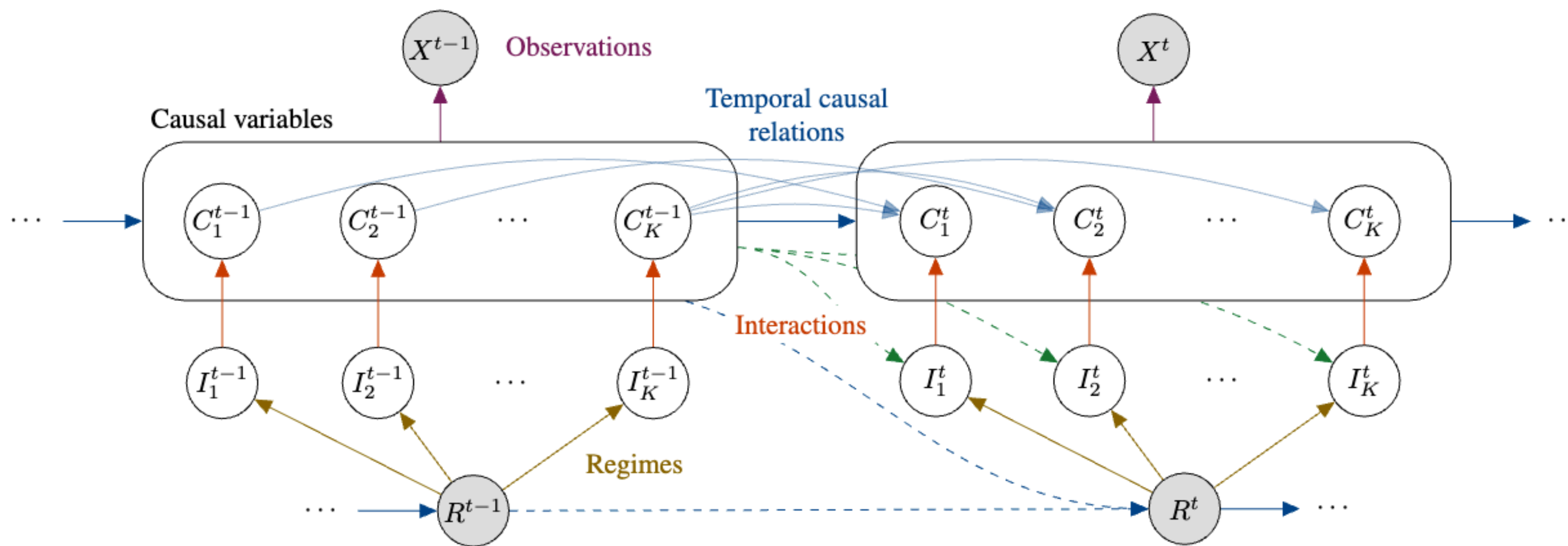
CAUSAL LEARNING FROM BINARY INTERACTIONS

- Many interactions are binary
(Turn lights on/off, open/close door ...)
- Learn latents to reflect change
- Provable & manipulable causal factors
- By integrating probabilistic causal priors



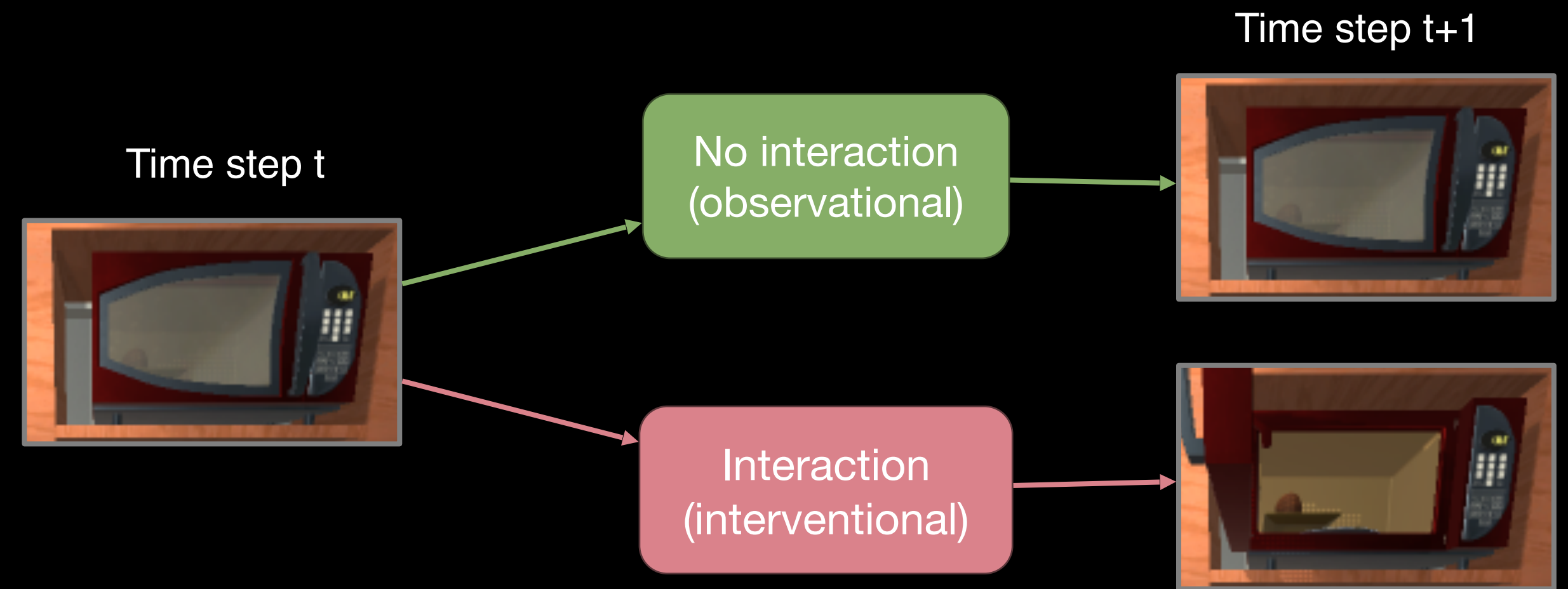
CAUSAL LEARNING FROM BINARY INTERACTIONS

- Causal model: a temporal DAG
- Observed: images X^t and "regime" variables R^t
- Latents: causal C^{t-1} and interactions $I^t = f(R^t, C^{t-1})$



BINARY INTERACTIONS FOR IDENTIFIABILITY

- Assumption #1: interactions described by a binary variable
- Assumption #2: distinct interaction patterns → interactions not functions of other interactions
- Assumption #3: mechanisms vary sufficiently with interactions or time



A. **(Dynamics Variability)** Each variable's log-likelihood difference is twice differentiable and not always zero:

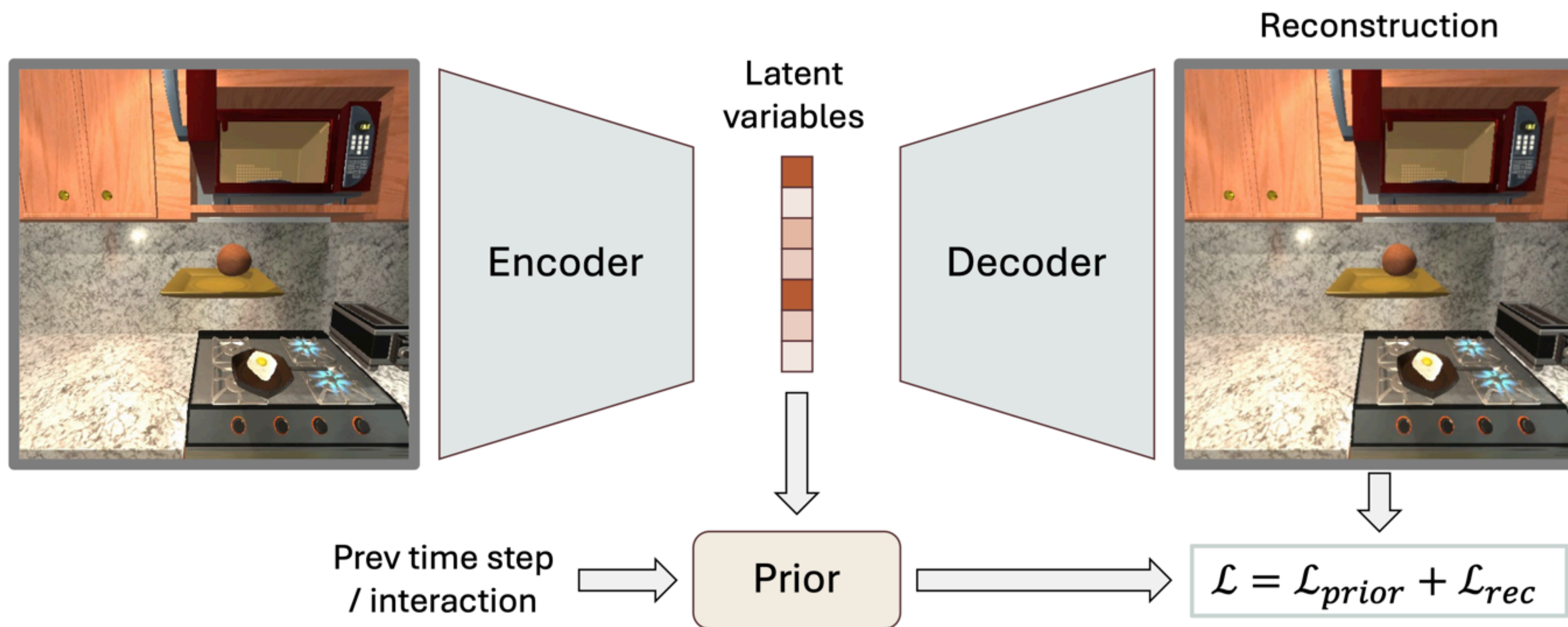
$$\forall C_i^t, \exists C^{t-1}: \frac{\partial^2 \Delta(C_i^t | C^{t-1})}{\partial (C_i^t)^2} \neq 0;$$

B. **(Time Variability)** For any $C^t \in \mathcal{C}$, there exist $K + 1$ different values of C^{t-1} denoted with $c^1, \dots, c^{K+1} \in \mathcal{C}$, for which the vectors $v_1, \dots, v_K \in \mathbb{R}^{K+1}$ with

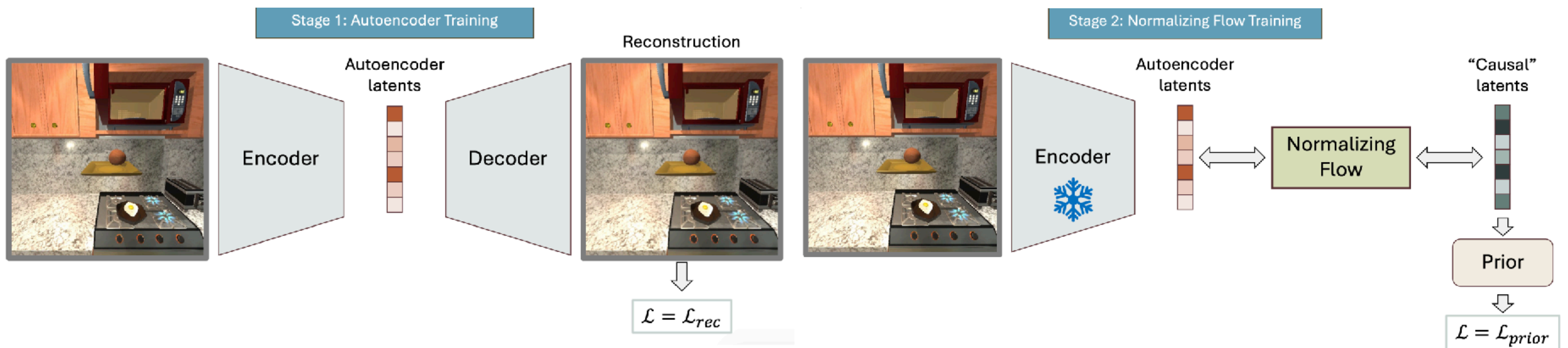
$$v_i = \left[\frac{\partial \Delta(C_i^t | C^{t-1}=c^1)}{\partial C_i^t} \quad \dots \quad \frac{\partial \Delta(C_i^t | C^{t-1}=c^{K+1})}{\partial C_i^t} \right]^T$$

are linearly independent.

OPTIMIZING WITH VARIATIONAL INFERENCE

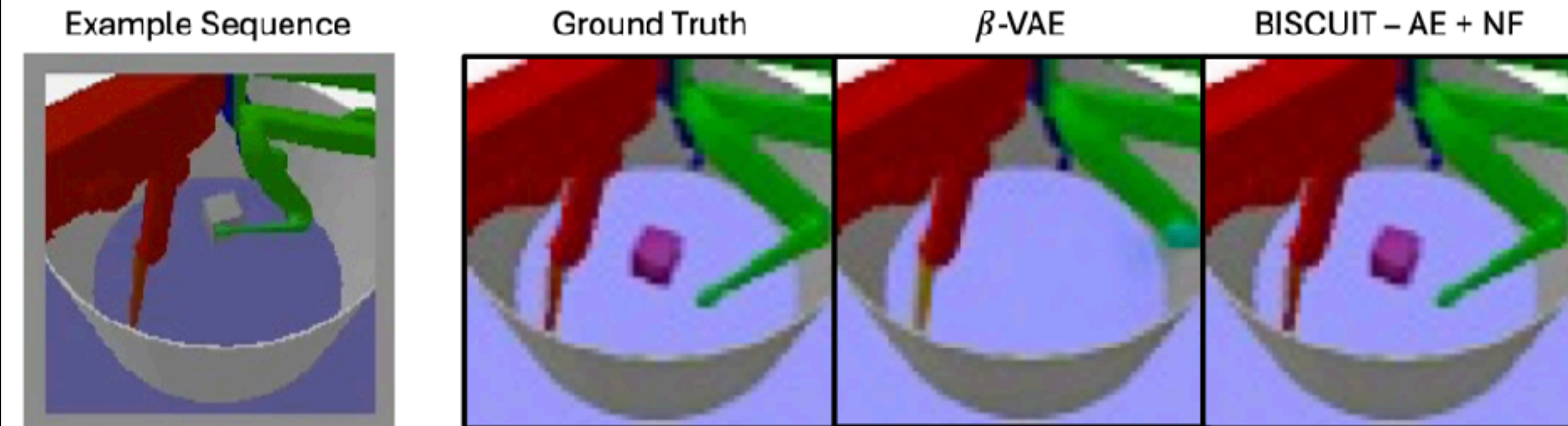


TWO-STAGE LEARNING IN COMPLEX SETTINGS



CAUSALWORLD TRI-FINGER

DISCOVERING INTERACTIONS

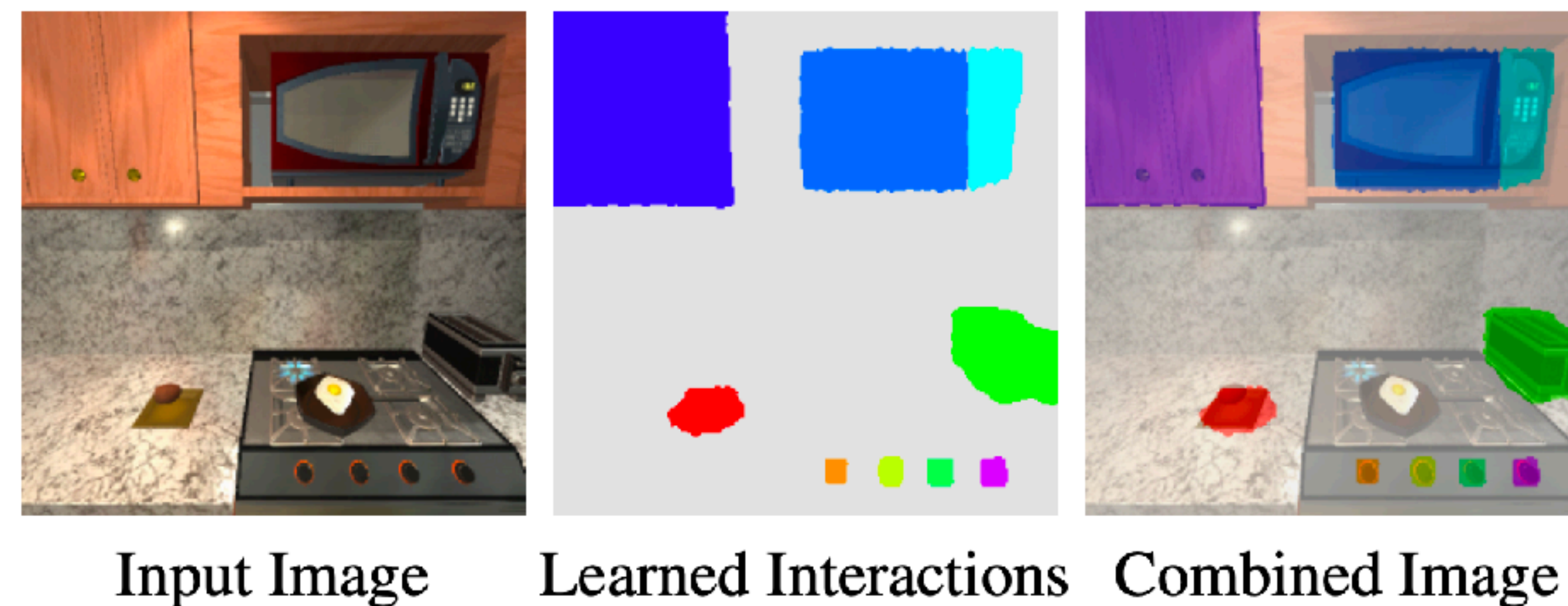


R^2 scores (diag \uparrow /sep \downarrow)

Models	CausalWorld
iVAE (Khemakhem et al., 2020a)	0.28 / 0.00
LEAP (Yao et al., 2022b)	0.30 / 0.00
DMS (Lachapelle et al., 2022b)	0.32 / 0.00
BISCUIT-NF (Ours)	0.97 / 0.01

ITHOR OBJECTS AS CAUSAL VARIABLES

CAUSE-AND-EFFECT
DRIVES SEMANTICS (?)



R^2 scores (diag \uparrow /sep \downarrow)

Models	iTHOR
iVAE (Khemakhem et al., 2020a)	0.48 / 0.35
LEAP (Yao et al., 2022b)	0.63 / 0.45
DMS (Lachapelle et al., 2022b)	0.61 / 0.40
BISCUIT-NF (Ours)	0.96 / 0.15

ELEMENTS OF "IMAGINATION"

HACKING THE SIMULATOR



Input Image 1

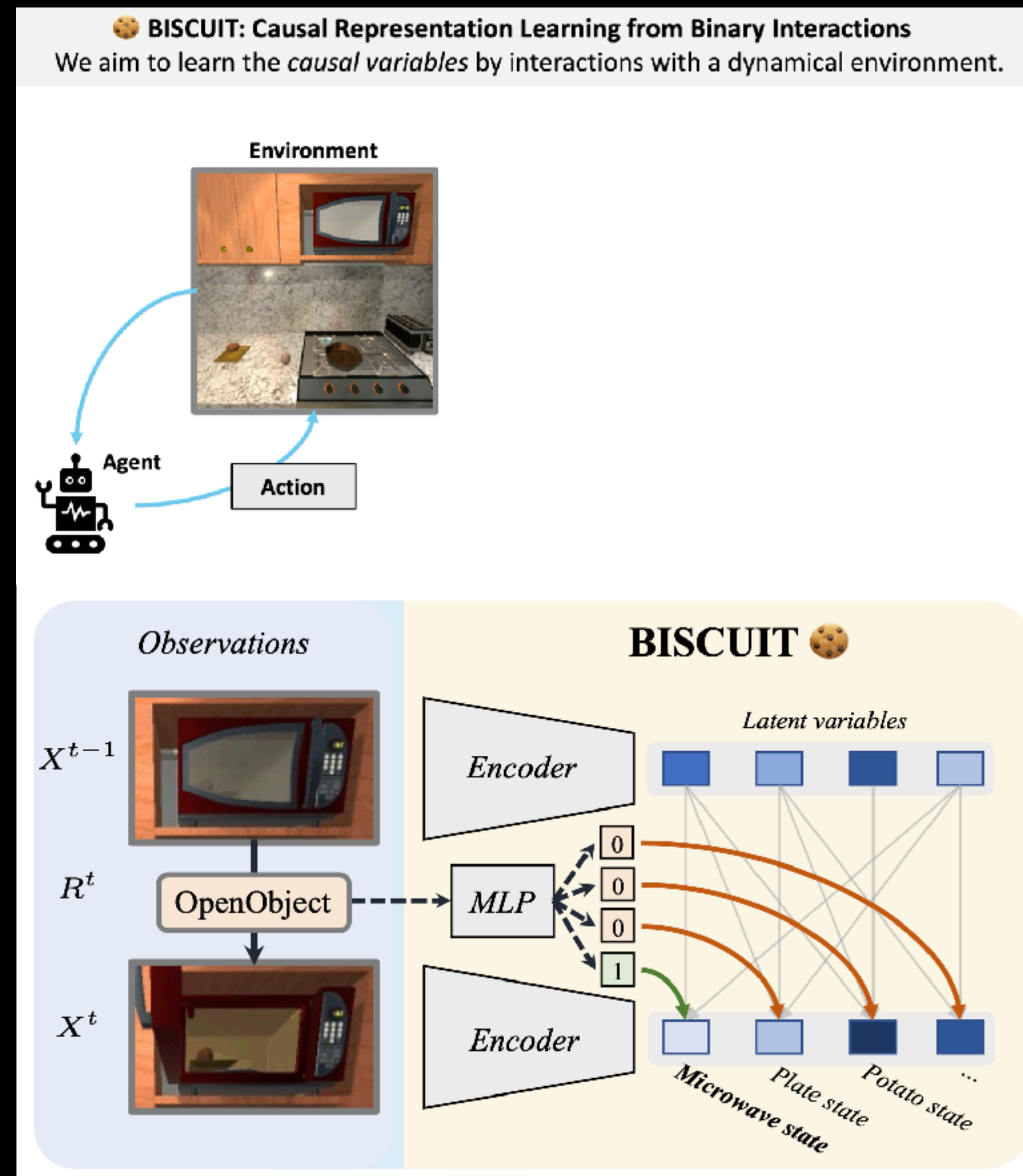
Input Image 2

Generated Output

Scaling-up with foundation vision models
towards autonomous learning?

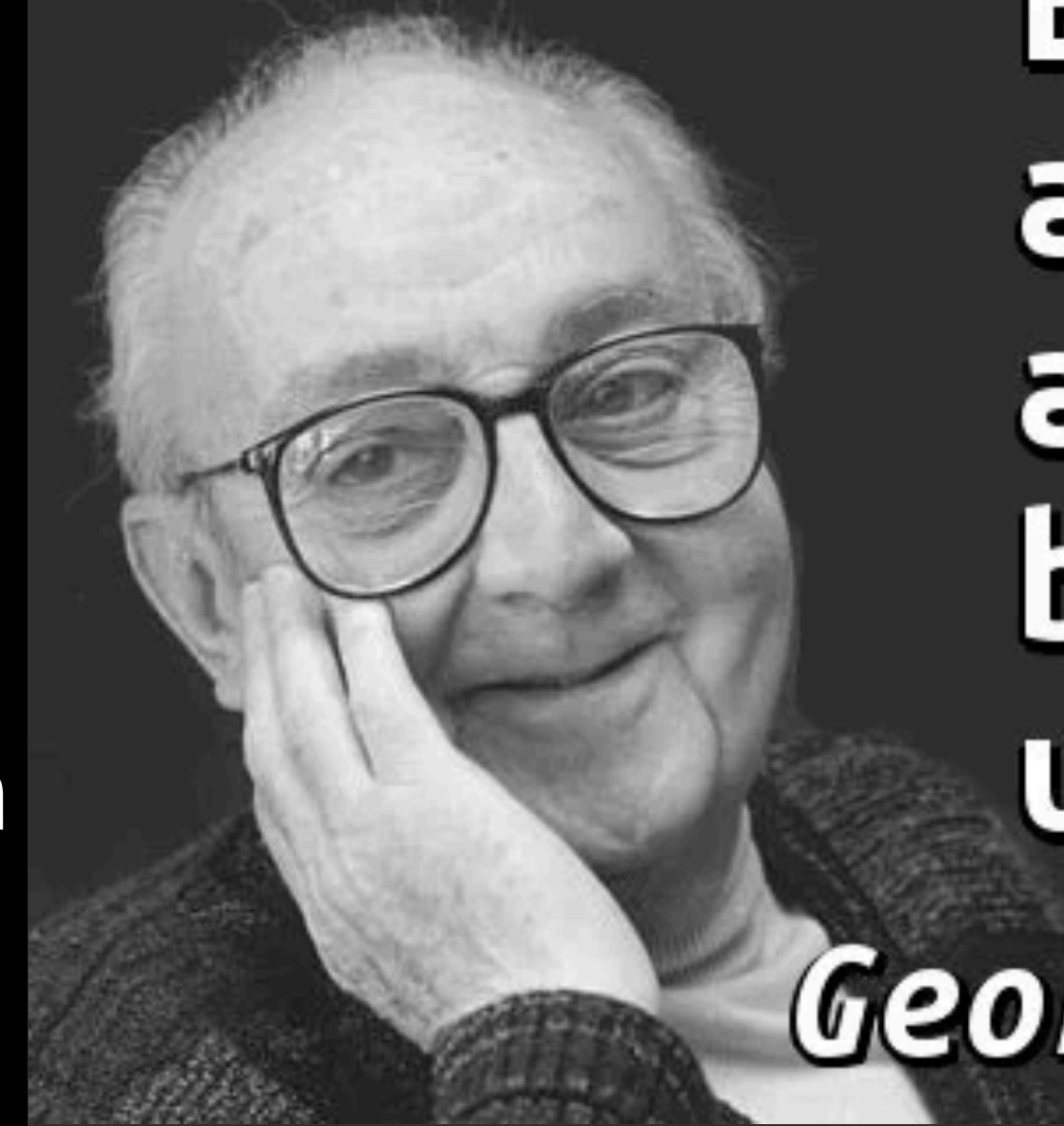
LIMITATIONS

- Sufficient intervention data
- Works with temporal data only
- Assumes binary interactions



IS IT REALLY CAUSAL?

- Patterns are often correlations
- Cause-and-effect is a strong (albeit sometimes biased) framework to learn
- If we go past the chicken-egg problem
- Power of causal representations is in autonomusness and controllability (imho)



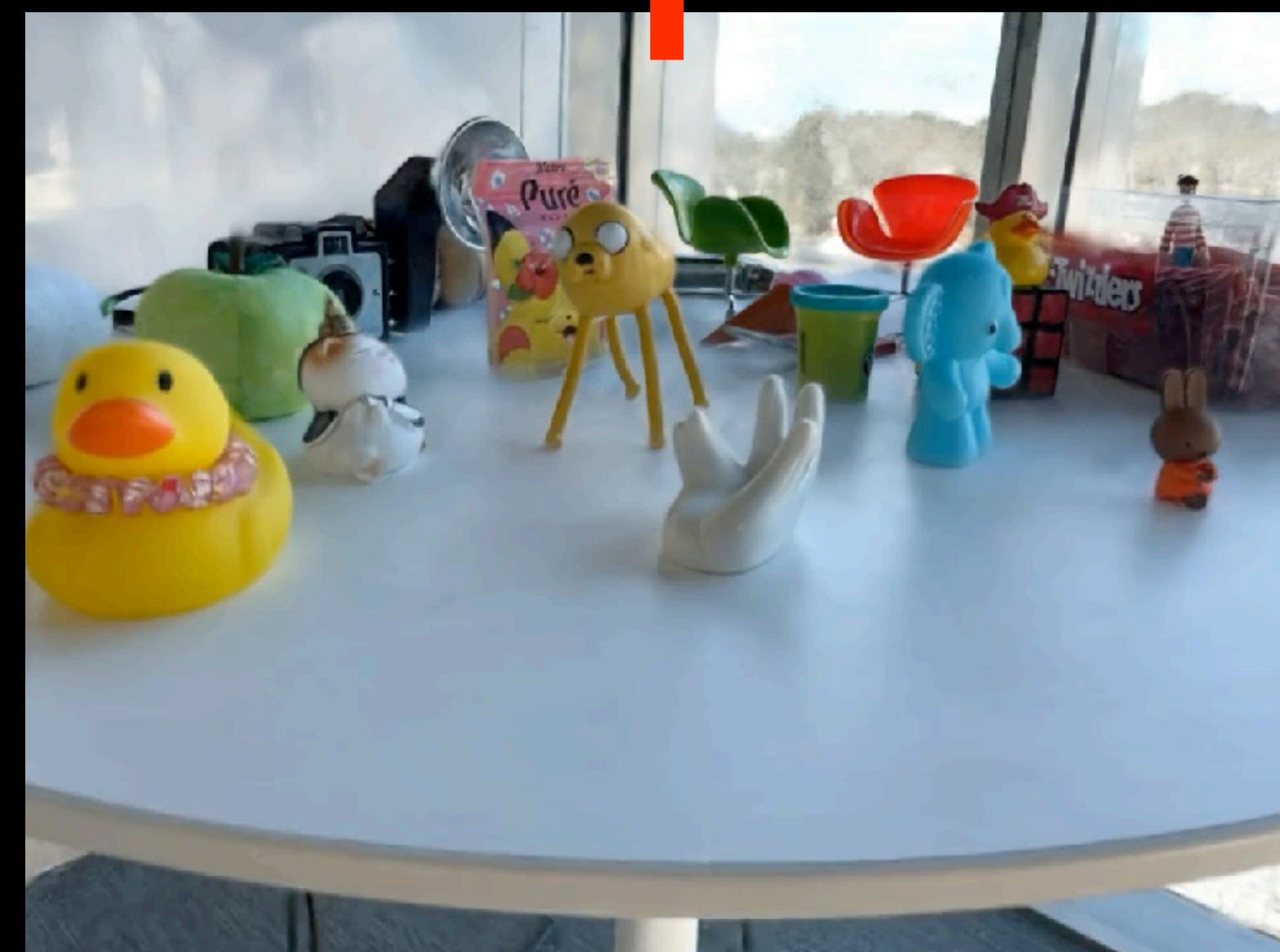
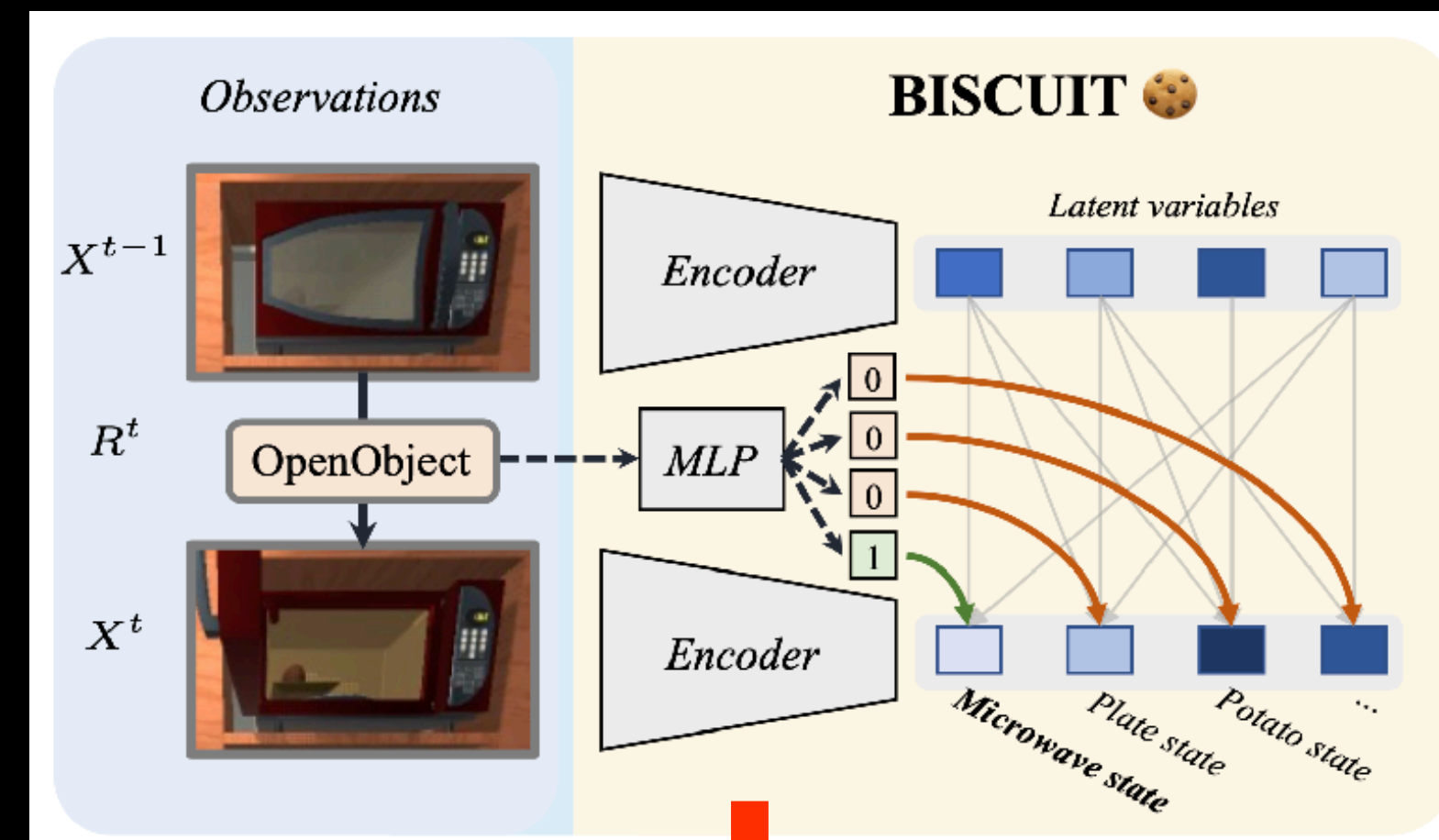
**“Essentially,
all models
are wrong,
but some are
useful.”**

George E. P. Box

BISCUIT++

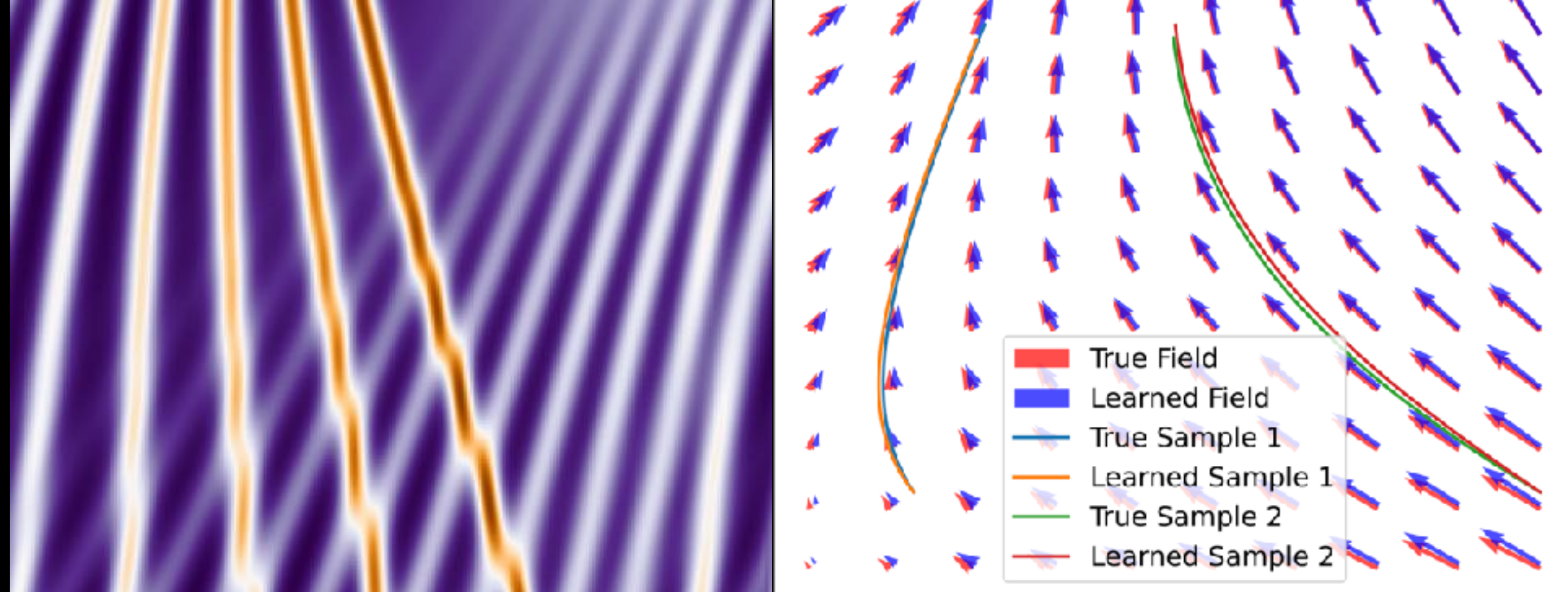
SCALE & ROBOT LEARNING

- Scale up to many environments → reuse semantics
- LLMs for guidance and sample efficiency?
- Ideally, Gaussian Splats for *de novo* interactive environments and scaling-up
- System IIa: First causal principles for novel problem-solving & Causal World Models
- System IIb: Safe & human-robot-aligned planning



LIU ET AL, ICML 2023, ONGOING
AUZINA ET AL, NEURIPS 2023
PERVEZ ET AL, ONGOING

DYNAMICS INDUCTIVE BIASES



Forward:

$$\dot{x} = 5.18 - 0.82y + 0.17xy$$

$$\dot{y} = 0.42 + 0.16xy$$

Backward:

$$\dot{x} = -4.39 - 0.66y + 0.21x^2$$

$$\dot{y} = -0.72 + 0.03y^2$$

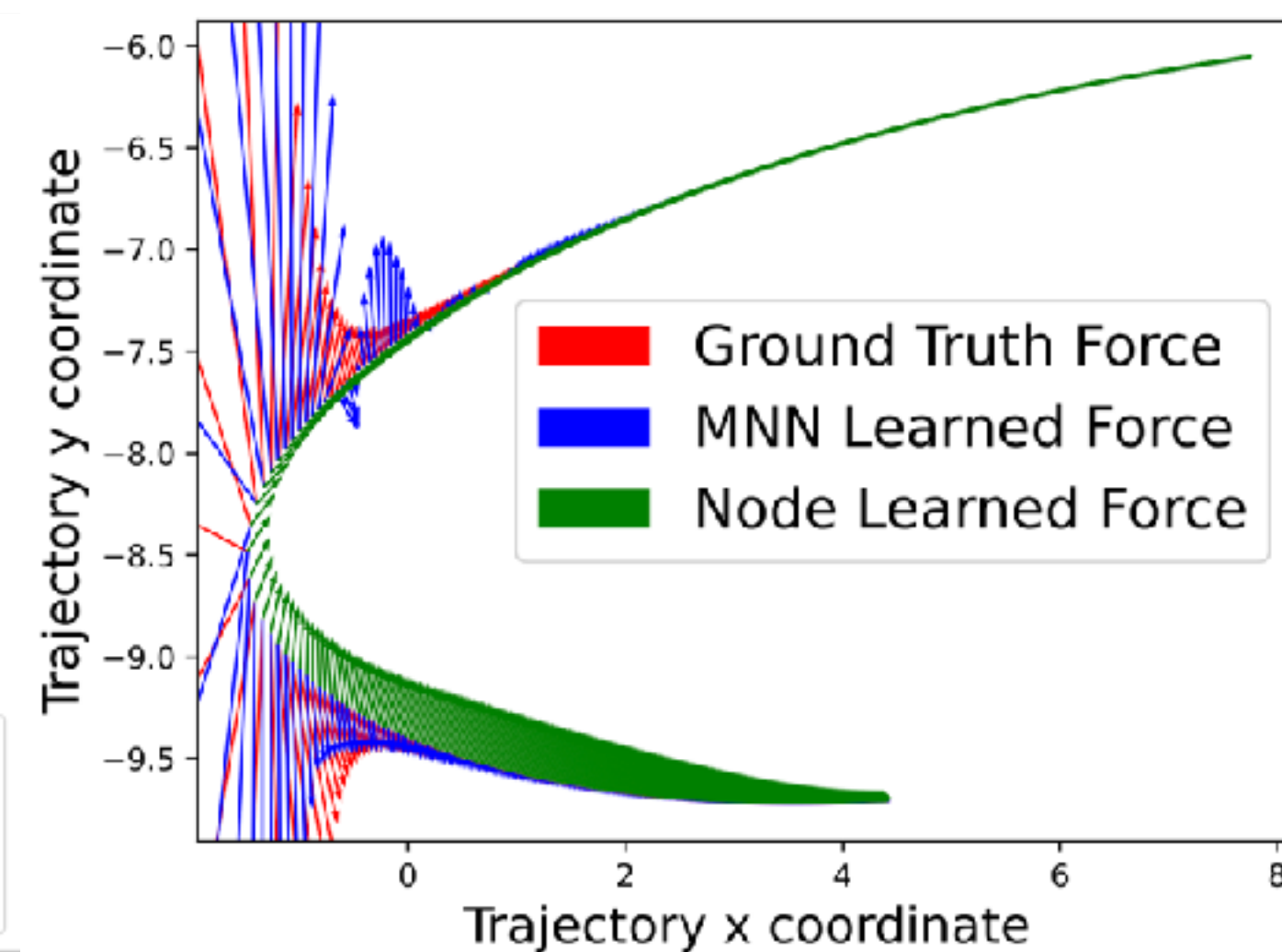
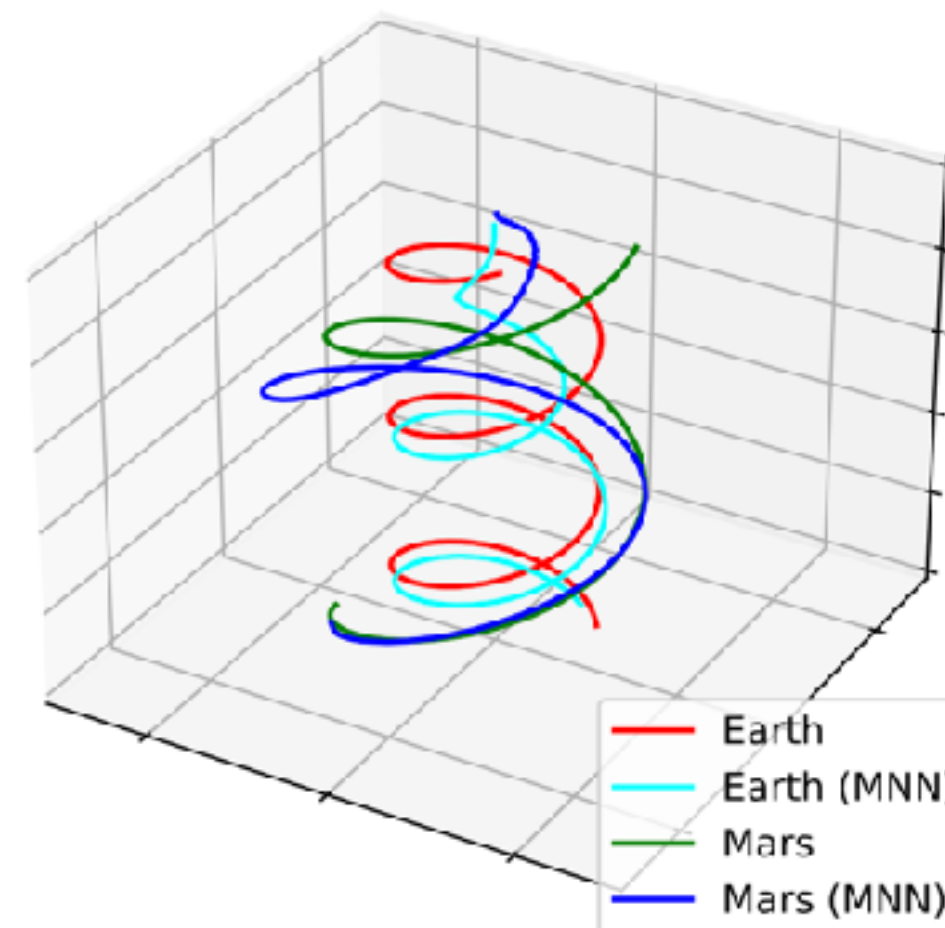
(a) Forward and Backward



$$\dot{x} = 4.73 - 1.04x^2y + 0.28$$

$$\dot{y} = 1.27 - 0.90xy + 0.07y$$

(b) Clockwise

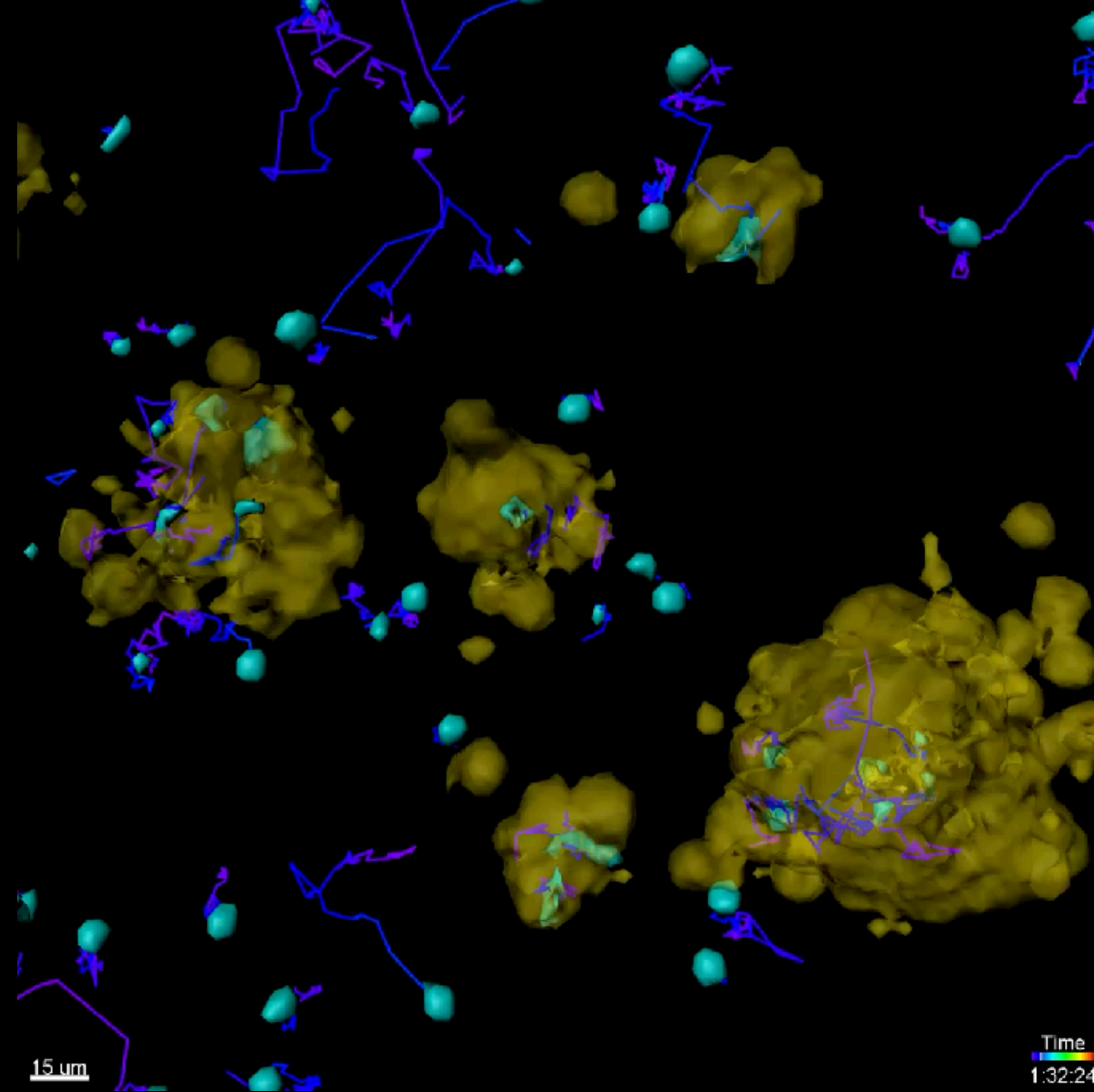
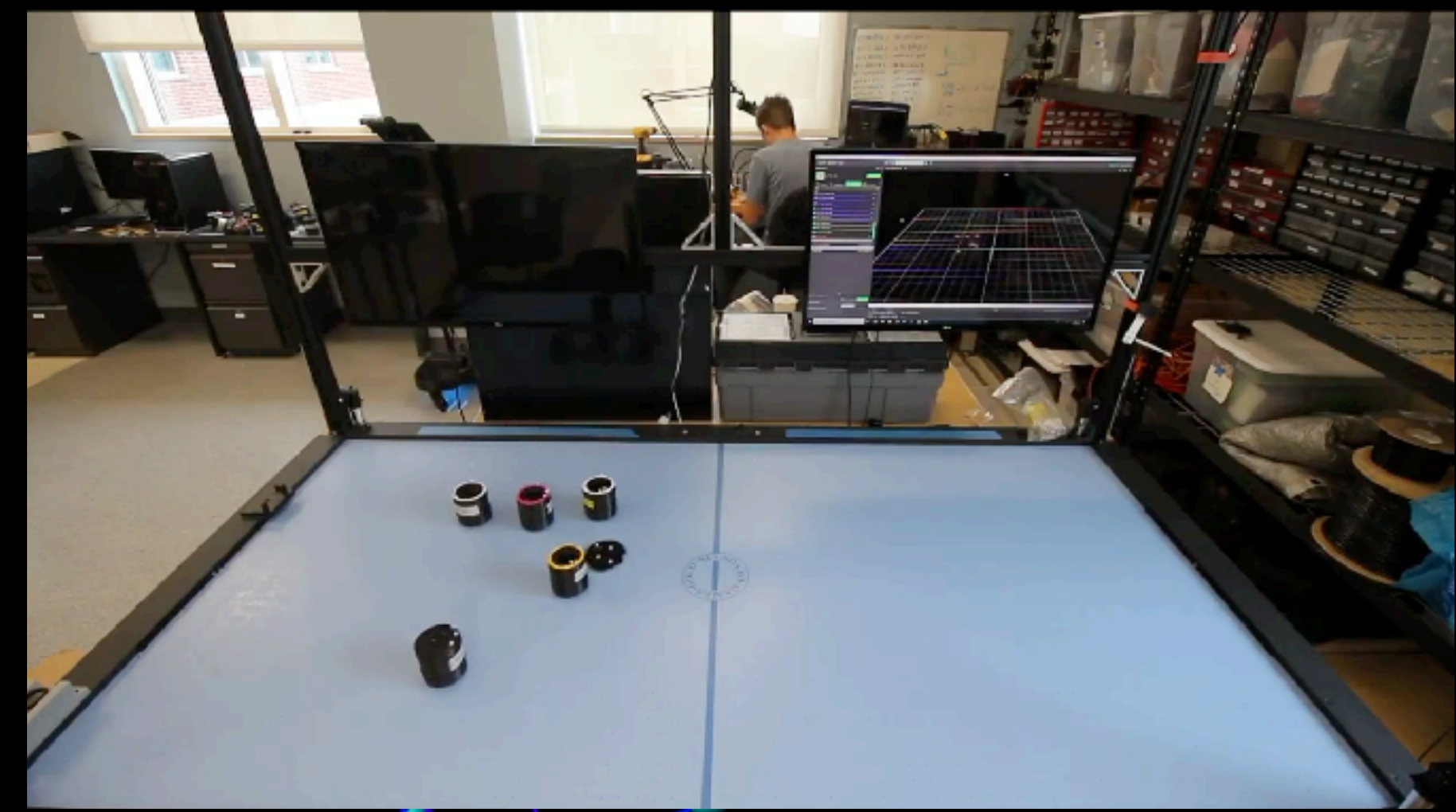


SWITCHING DYNAMICS IN INTERACTING SYSTEMS

- In many settings in perception and sciences, we have systems of multiple objects
- These objects may interact (or not) with higher-order complex & switching temporal dynamics^{1,2}
- Finding dynamical patterns is often critical
- Generalization of temporal clustering

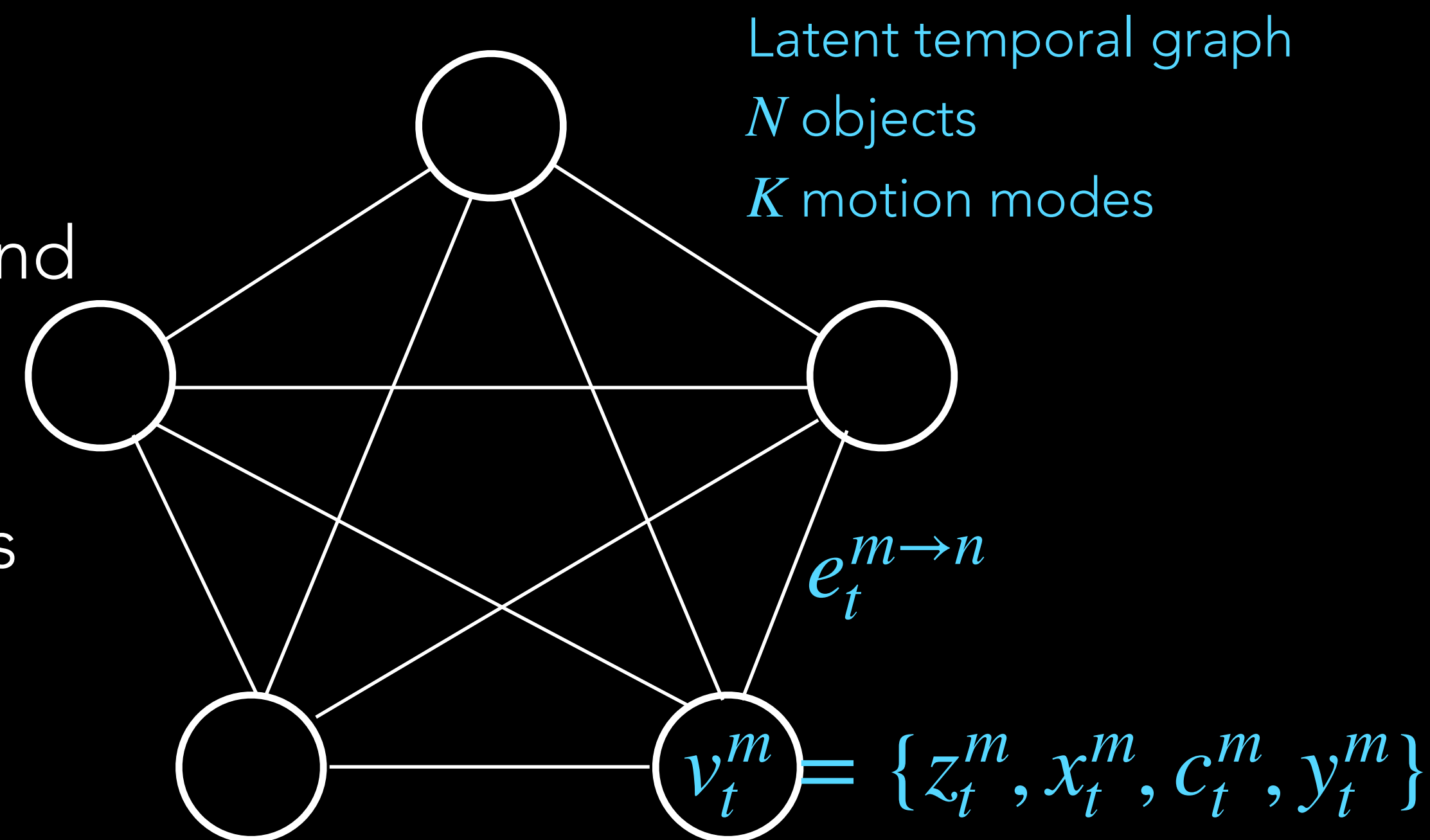
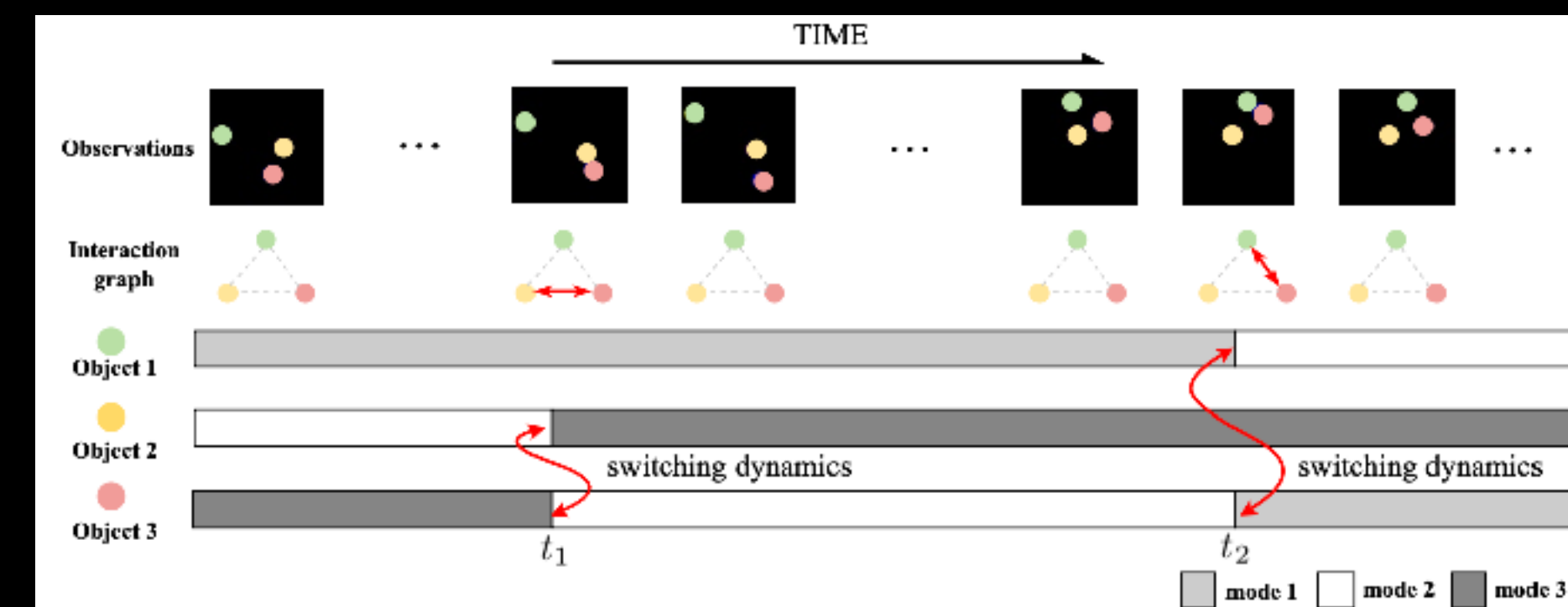
[1] Z Ghahramani, G Hinton, Variational learning for switching state-space models, NeurIPS, 2020

[2] A Ansari, K Benidis, R Kurle, A Turkmen, H So, A Smola, B Wang, T Januschowski, NeurIPS, 2022



GRAPH SWITCHING DYNAMICAL SYSTEMS

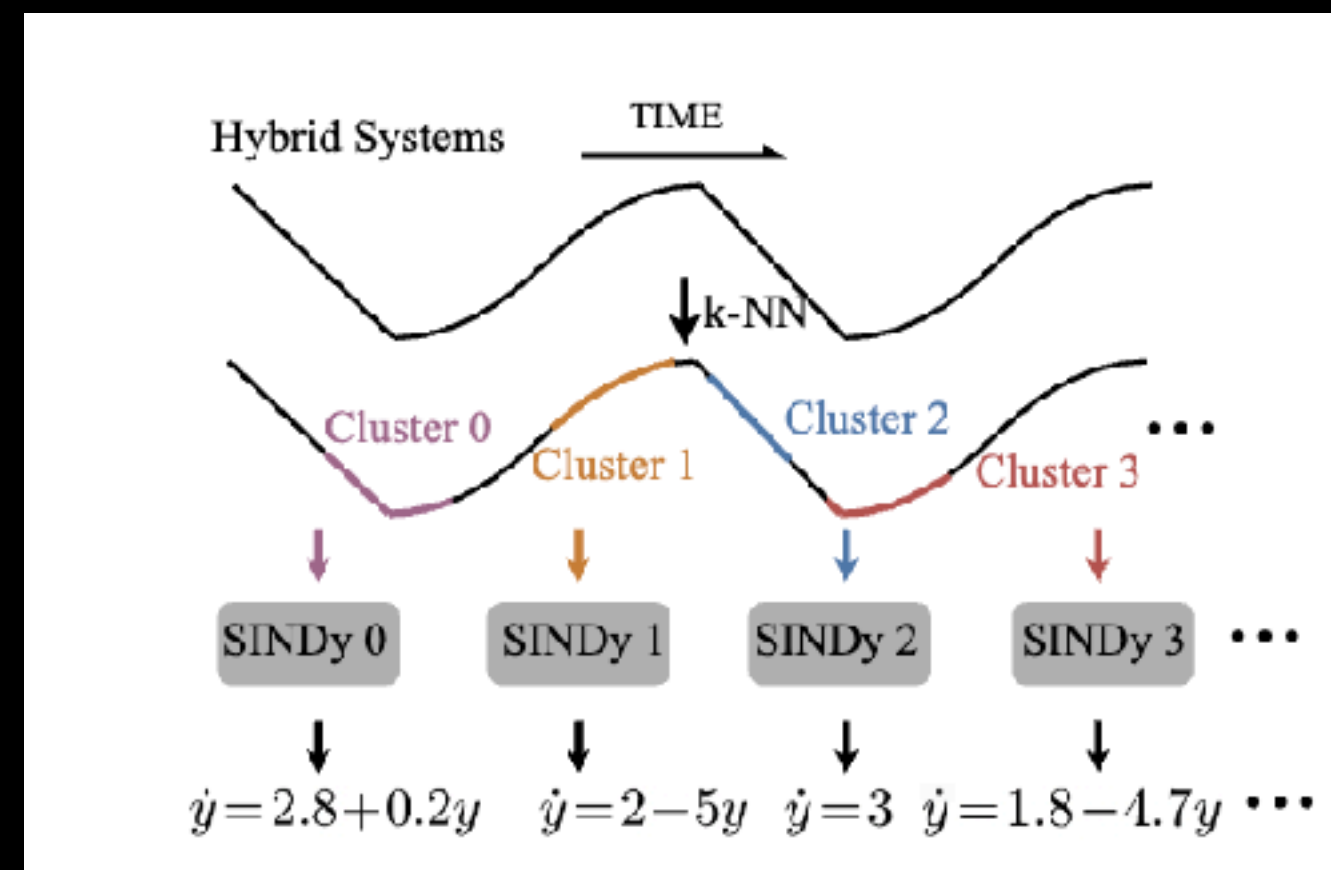
- Switching Dynamical Systems focus on finding out when objects behave differently
- Key idea #1: Scale up by NN function approximation to amortize pairwise transition dynamics between multiple objects and dynamic behaviors
- Key idea #2: Graph NNs and message passing and VI for dynamic interactions between objects
- Divide and Conquer: Breaking complex dynamics into switching between simpler systems



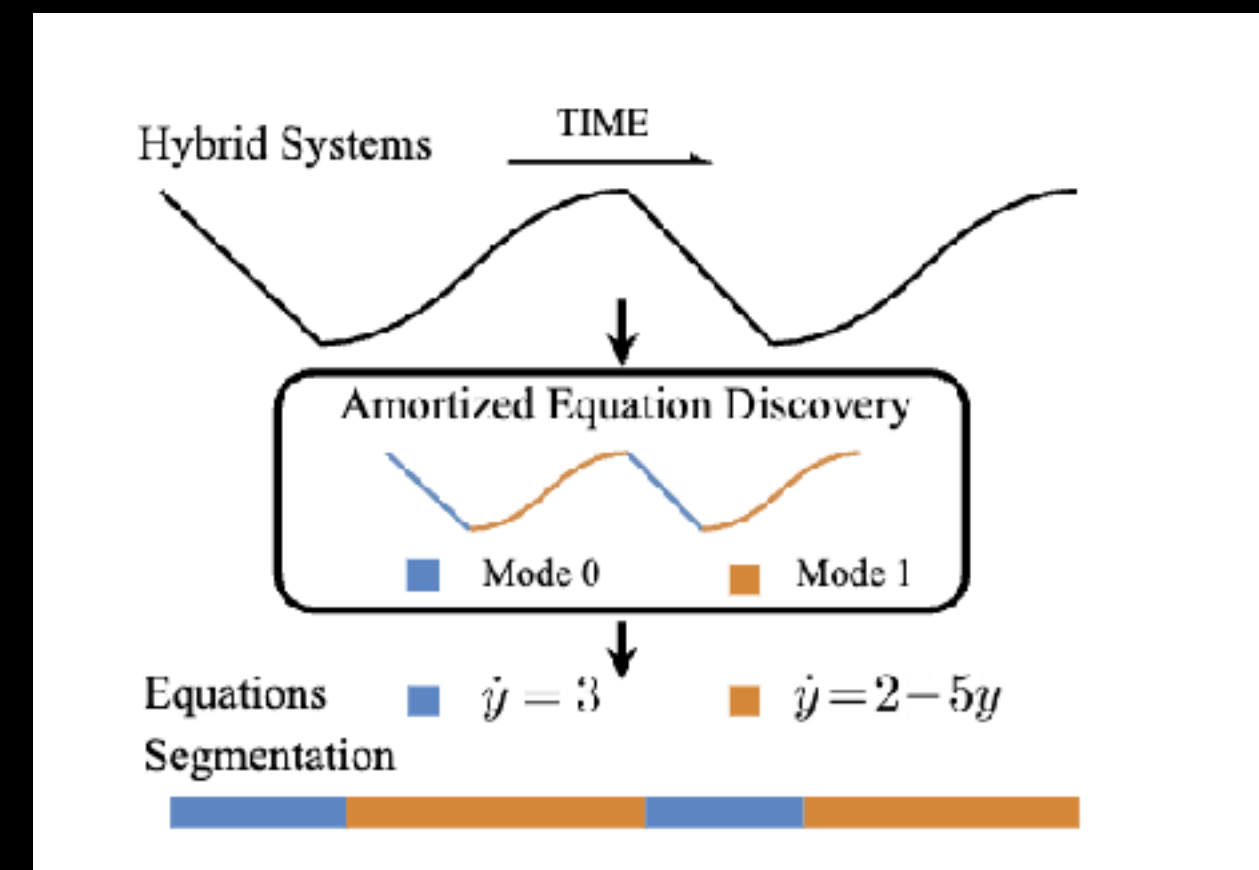
EQUATION DISCOVERY+SWITCHING DYNAMICS

- Hypothesis #1: Symbolic learning critical for extrapolation
- Hypothesis #2: Disentangled representation learning critical for generalization^{1,2}
- Hypothesis #3: Graph learning critical for interacting dynamics

Hybrid-SINDy

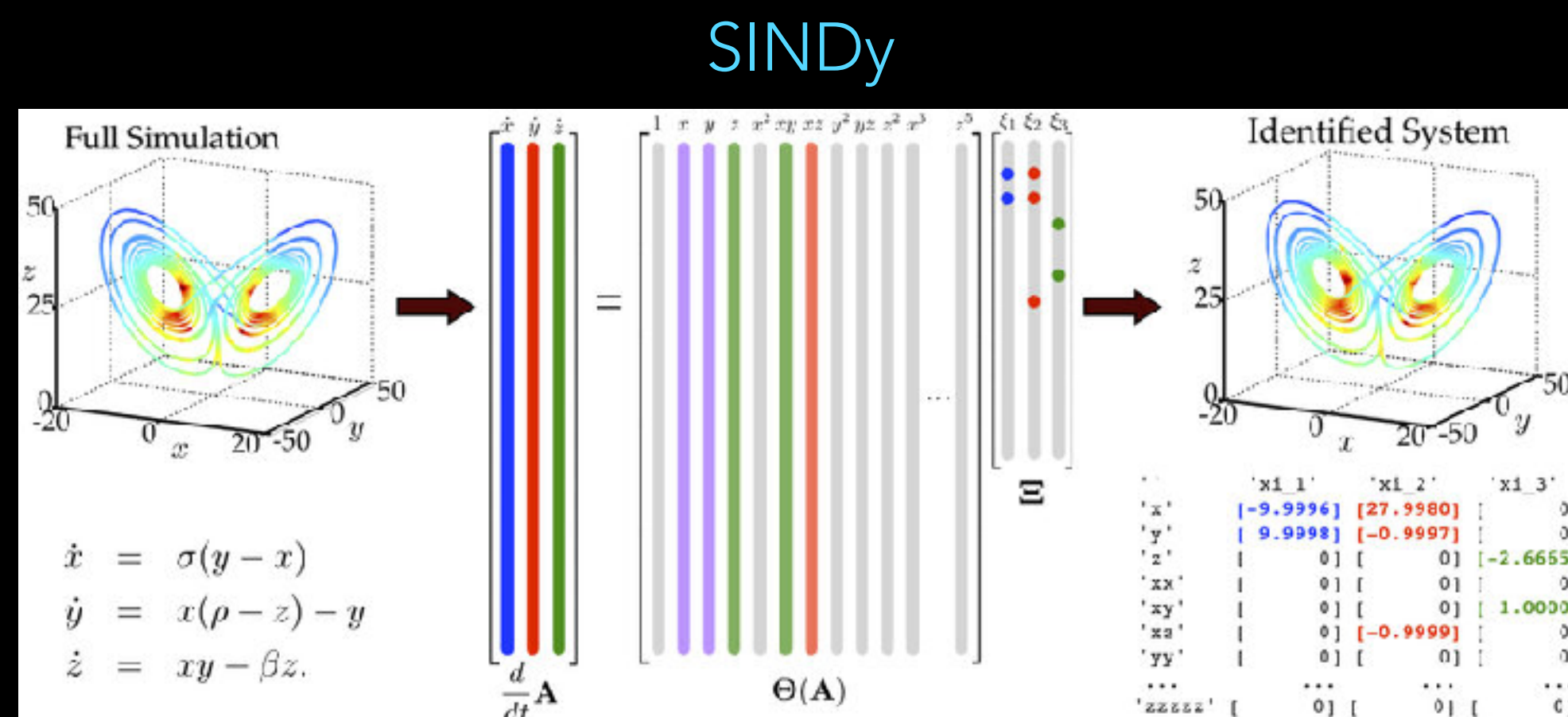


Latent dynamics as governing equations

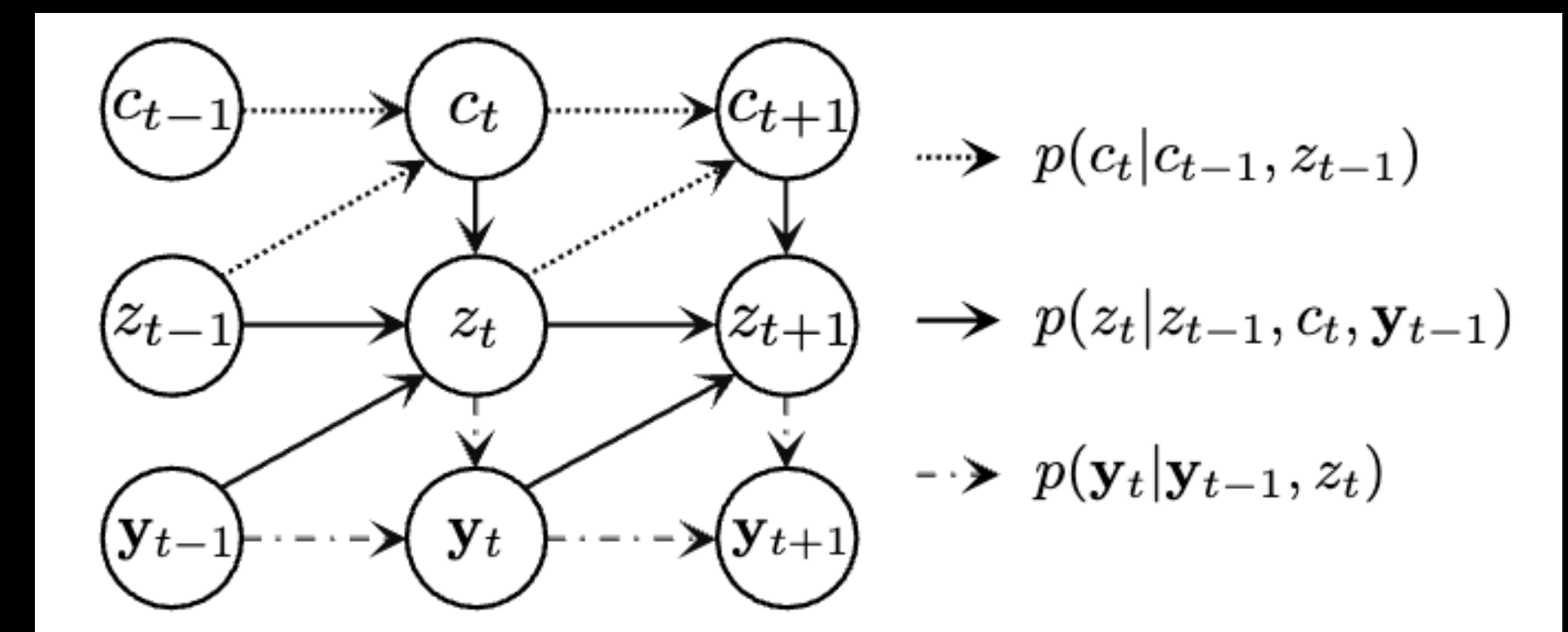


EQUATION DISCOVERY+SWITCHING DYNAMICS

- #H1: Link GRASS dynamics modes to parametric basis functions $\Theta(\mathbf{y}_t)$
- #H2: Learn k -th latent dynamics $\dot{\mathbf{y}}_t^m \approx \Theta(\mathbf{y}_t)w_m$ modulated by w_m in shared NN
- Think of SINDy-governed latent spaces

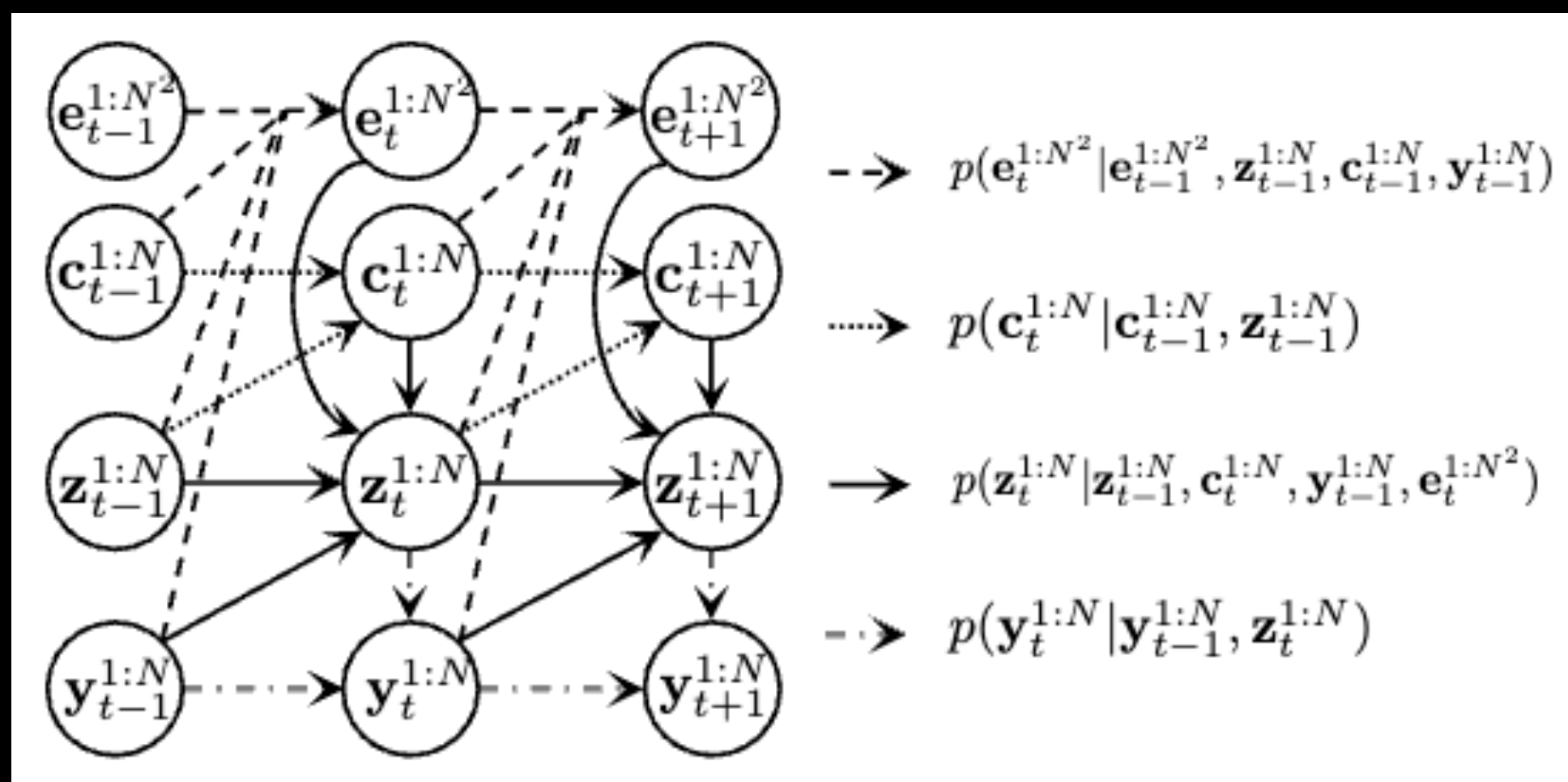


The dynamic mode z_k indexes candidate basis $\Theta_k \cdot w_k$

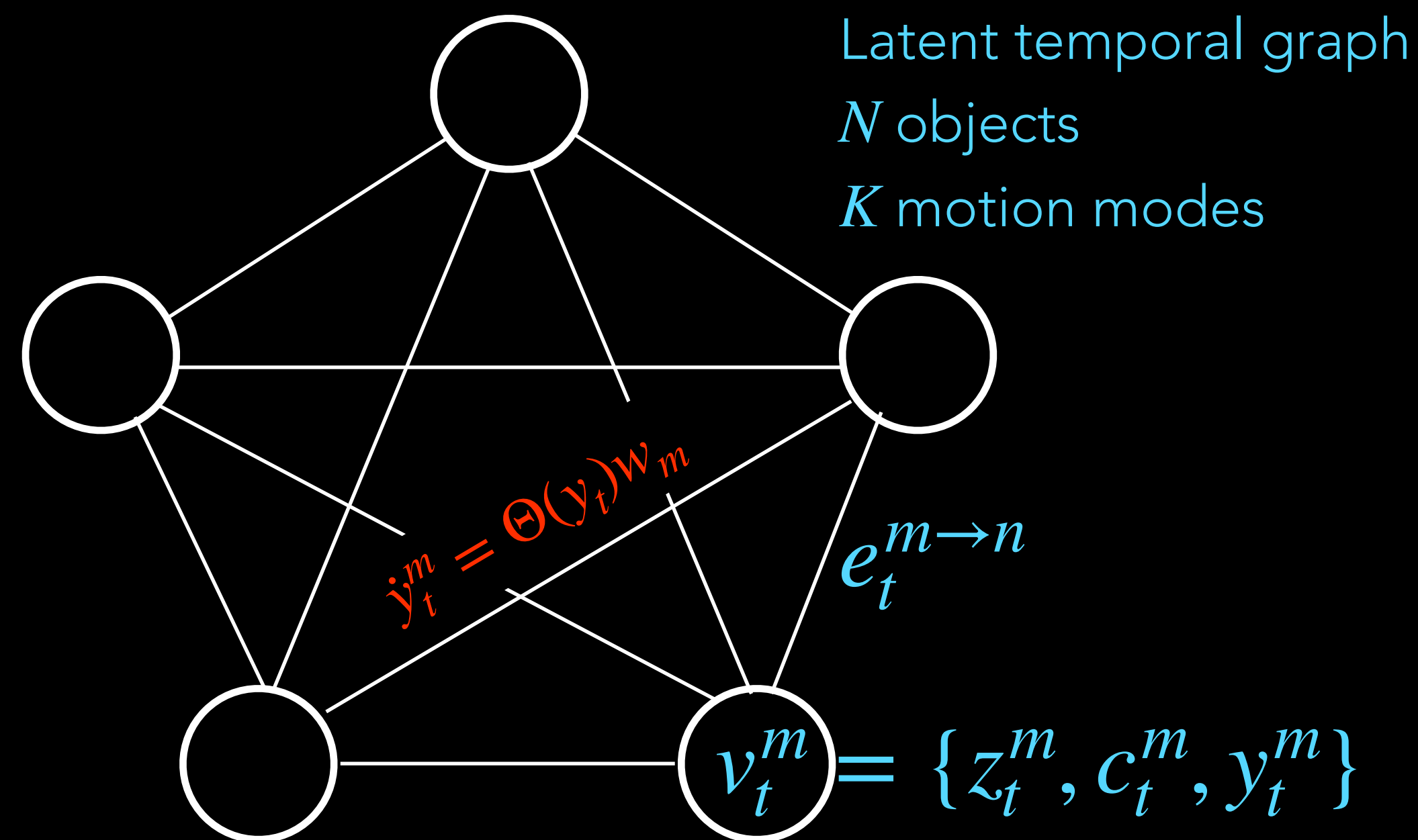


EQUATION DISCOVERY+SWITCHING DYNAMICS

- So far, single-object dynamics
- #H3: Graph message passing for interacting dynamics
- Approximate inference for edges, exact inference for discrete variables



Probabilistic model



RESULTS

EQUATION DISCOVERY+SWITCHING DYNAMICS

Scientific data

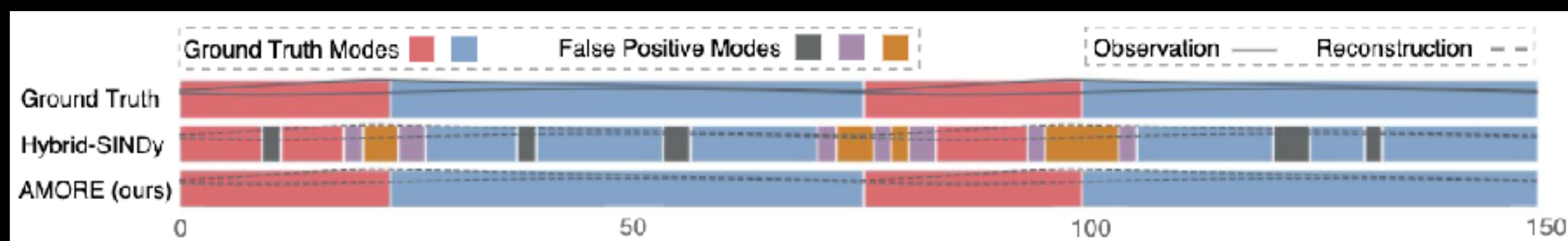


Table 1. Segmentation results on Mass-spring Hopper dataset.

Method	NMI \uparrow	ARI \uparrow	Accuracy \uparrow	F_1 \uparrow
Hybrid-SINDy	0.426	0.383	0.705	0.691
AMORE (ours)	0.934	0.970	0.993	0.994

Table 2. Forecasting results of Location/Velocity on the Mass-spring Hopper dataset.

Method	NMAE \downarrow	NRMSE \downarrow
LLMTime	0.120 / 0.320	0.430 / 0.500
SVI	0.063 / 0.070	0.140 / 0.250
AMORE (ours)	0.009 / 0.037	0.024 / 0.056

Table 7. Forecasting results of in terms of NMAE / NRMSE on ODE-driven Particle dataset.

Method	One-step	Multi-step
LLMTime	0.335 / 0.438	0.370 / 0.473
SVI	0.319 / 0.432	0.346 / 0.465
GRASS	0.151 / 0.224	0.193 / 0.270
AMORE (ours)	0.184 / 0.265	0.217 / 0.302
AMORE-MIO (ours)	0.146 / 0.217	0.186 / 0.259

Table 5. Forecasting results on non-hybrid dynamical systems. Results are shown in $\log_{10}(\text{NRMSE})$ where lower is better.

System	LLMTime	SVI	AMORE (ours)
Coupled linear	-0.39	-1.13	-1.18
Cubic oscillator	-0.45	-1.02	-1.06
Lorenz'63	-0.41	-1.27	-1.23
Hopf bifurcation	-0.32	-0.94	-1.03
Selkov glycolysis	-0.68	-1.55	-1.49
Duffing oscillator	-0.53	-1.12	-1.17

Table 6. Segmentation results on ODE-driven Particle Dataset.

Method	NMI \uparrow	ARI \uparrow	Accuracy \uparrow	F_1 \uparrow
Hybrid-SINDy	0.205	0.192	0.414	0.407
AMORE (ours)	0.418	0.405	0.692	0.684
AMORE-MIO (ours)	0.453	0.442	0.741	0.735

Table 10. Analyses on robustness to different orders of polynomial as candidate basis functions on Mass-spring Hopper dataset.

Polynomial order	2		3		5	
	NMI \uparrow	RER \downarrow	NMI \uparrow	RER \downarrow	NMI \uparrow	RER \downarrow
Hybrid-SINDy	0.426	$7.5e^{-3}$	0.384	$8.1e^{-3}$	0.316	$9.7e^{-3}$
AMORE (ours)	0.934	$2.1e^{-4}$	0.936	$2.3e^{-4}$	0.933	$2.8e^{-4}$

Perception data

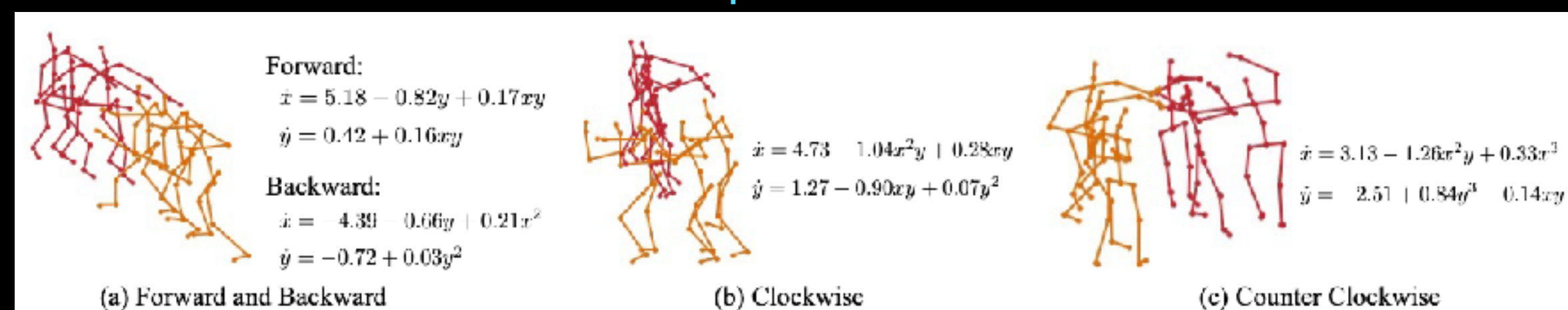


Figure 5. Discovered equations on the Salsa-dancing dataset. Locations (x, y) of the hip joints are used as observations.

Table 8. Segmentation results on the Salsa-dancing dataset.

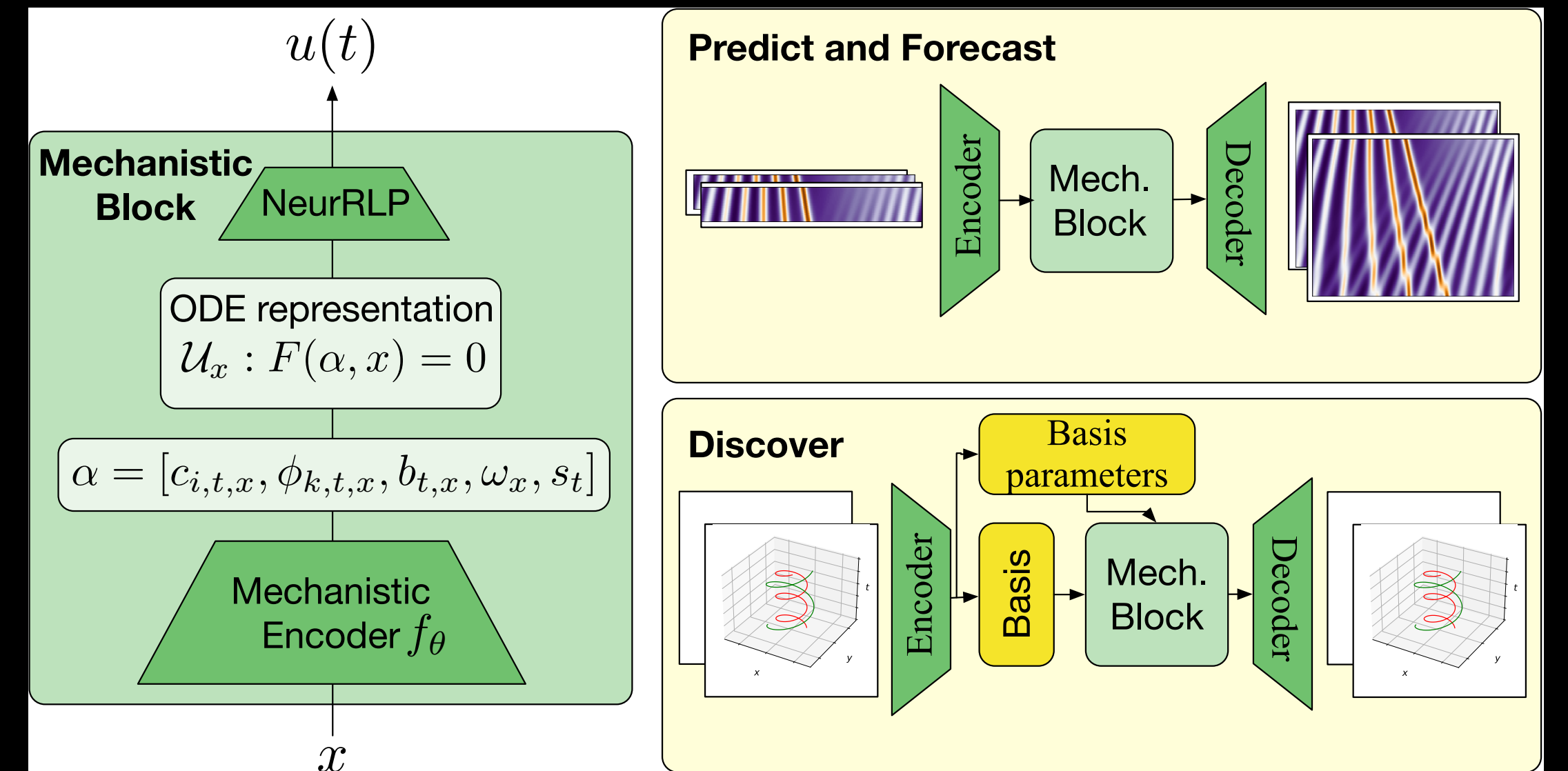
Method	NMI \uparrow	ARI \uparrow	Accuracy \uparrow	F_1 \uparrow
Hybrid-SINDy	0.102	0.097	0.325	0.309
AMORE (ours)	0.167	0.173	0.565	0.518
AMORE-MIO (ours)	0.179	0.182	0.583	0.531

Table 9. Forecasting results in terms of NMAE / NRMSE on the Salsa-dancing dataset.

Method	One-step	Multi-step
LLMTime	0.402 / 0.452	0.449 / 0.480
SVI	0.384 / 0.441	0.423 / 0.465
GRASS	0.285 / 0.344	0.313 / 0.359
AMORE (ours)	0.291 / 0.361	0.334 / 0.373
AMORE-MIO (ours)	0.272 / 0.335	0.301 / 0.352

MECHANISTIC NEURAL NETWORKS

- Neural Networks built on data-driven numerical representations
- Uninterpretable → unfit for scientific exploration and analysis
- Mechanisms would be a great alternative but cannot easily learn from data¹
- Mechanistic NN modules built on governing equations as representations

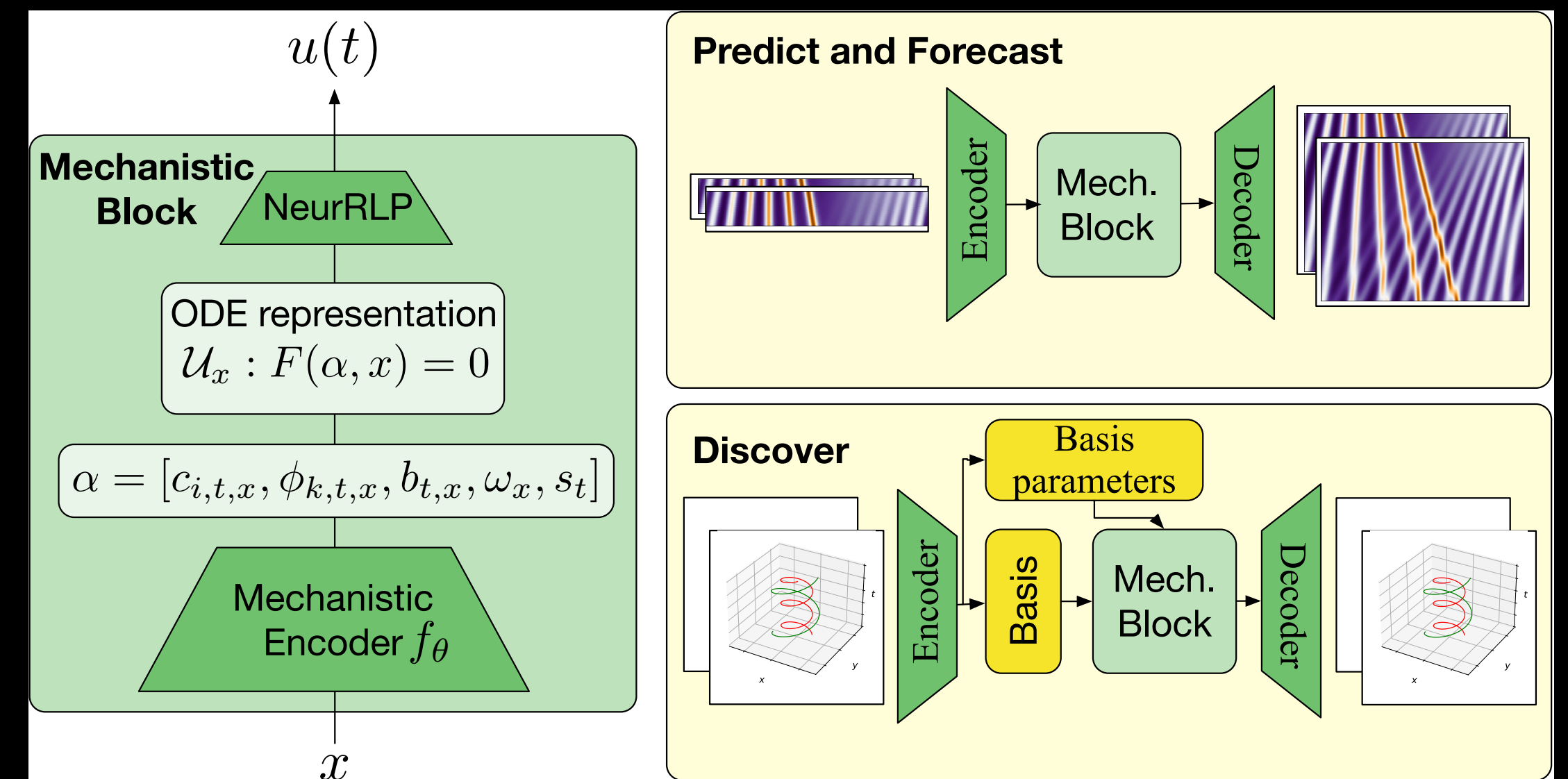


$$F(\alpha, x) = \sum_i^d c_i(t; x)u^{(i)} + \sum_k^r \phi_k(t; x)g_k(t, u, u', \dots) - b(t; x)$$

<https://github.com/alpz/mech-nn>

KEY IDEA

- Define general family of ODEs as governing mechanisms
- Mechanistic NN simultaneously
 - learns the governing ODE explicitly
 - generate new ODEs that explain input
 - solves the ODEs
- Forward pass through the ODE
- Backward pass requires custom, NN-native solver



$$F(\alpha, x) = \sum_i^d c_i(t; x)u^{(i)} + \sum_k^r \phi_k(t; x)g_k(t, u, u', \dots) - b(t; x)$$

THE MODEL

- Traditional ODE solvers suboptimal: Hard to parallelize, no learned step sizes
- Young showed that Linear ODEs can be solved as Linear Programs¹

- Continuous ODE:
$$\sum_i^d c_i(t; x)u^{(i)} + \sum_k^r \phi_k(t; x)g_k(t, u, u', \dots) - b(t; x) = 0$$

- Discretize it:
$$\sum_i^d c_{i,t}u^{(i)} + \sum_k^r \phi_{k,t}g_k(t, u_t, u'_t, \dots) - b_t = 0$$

- Set up the linear program and solve for $u, u^{(i)}, i = 1, 2, \dots$

NEURAL RELAXED LP SOLVER

- Define ODE coefficients etc as LP variables
- But LP solvers are not neural network friendly
 - Solutions not differentiable wrt parameters
 - Specialized solvers cannot parallelize easily
 - Constraint matrices too large for solvers
- Relaxing LP to QP and GPU solve KKT conditions
- Similar error bounds like the Euler solver and much faster
- For nonlinear ODEs, the nonlinear terms pushed to the NN loss function

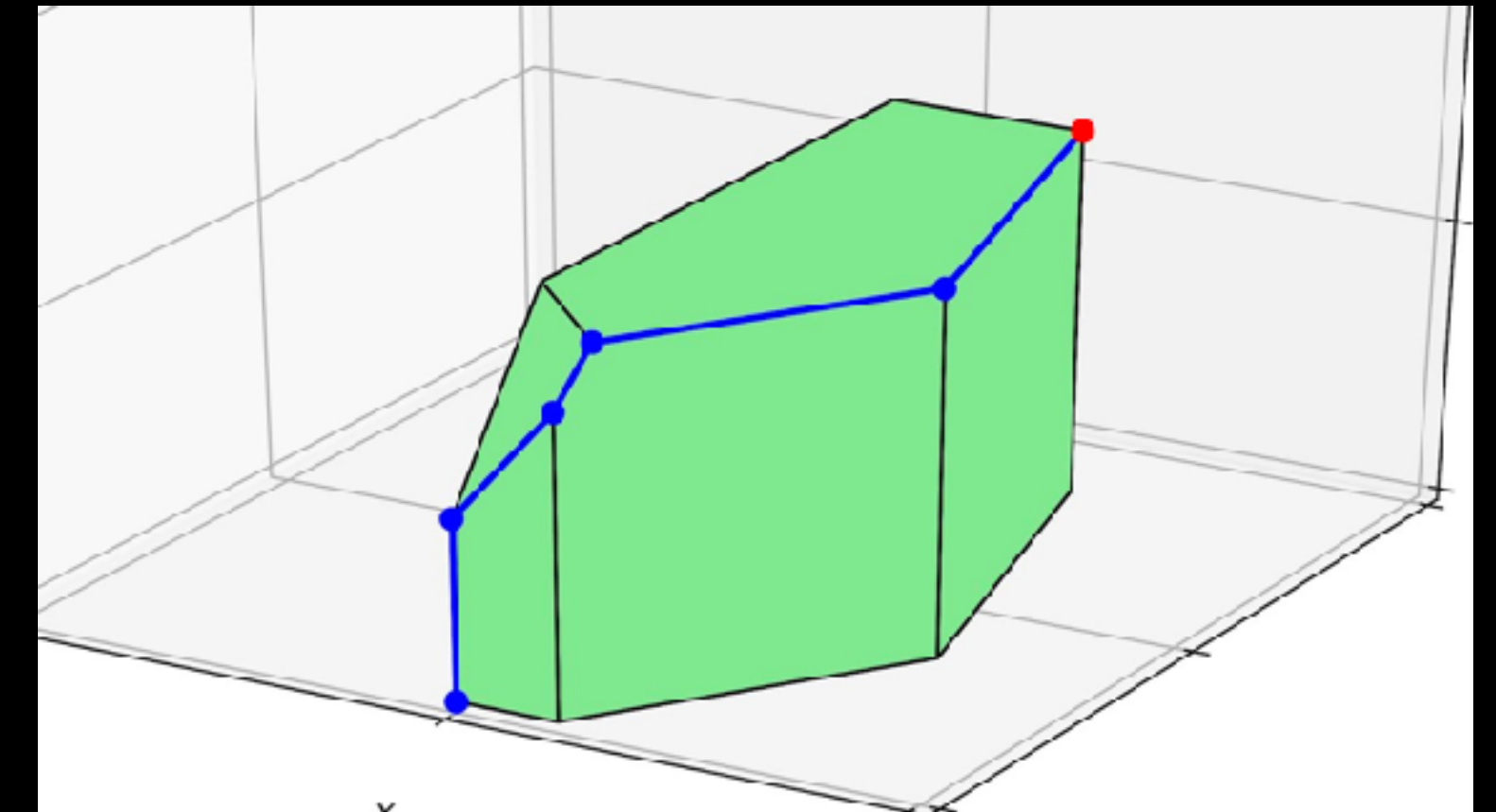


Table 2: Comparing the NeuRLP solver with the RK4 solver with a step size of 0.1 on fitting noisy sinusoidal waves of 300 and 1000 steps. Showing MSE loss and time.

Steps	QP (seconds)	RK4 (seconds)	QP Loss	RK4 Loss
40	1.52	28.06	11.4	29.3
100	1.61	64.57	27.9	35.6
300	1.76	211.52	52	96.8
500	2.12	359.7	128	301
1000	3.68	666.69	292	589

MECHANISTIC NEURAL NETWORKS

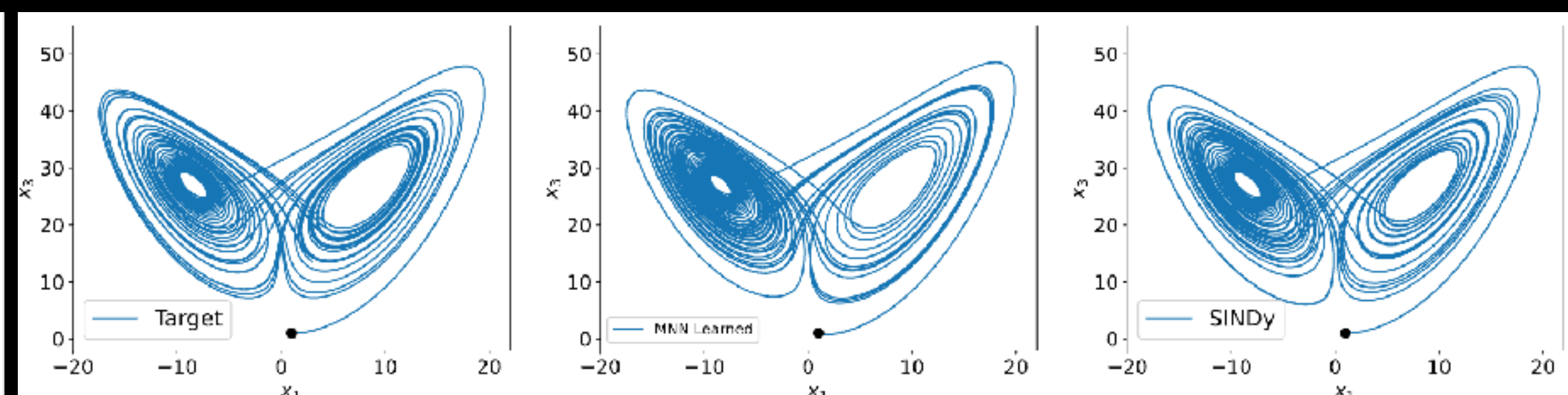
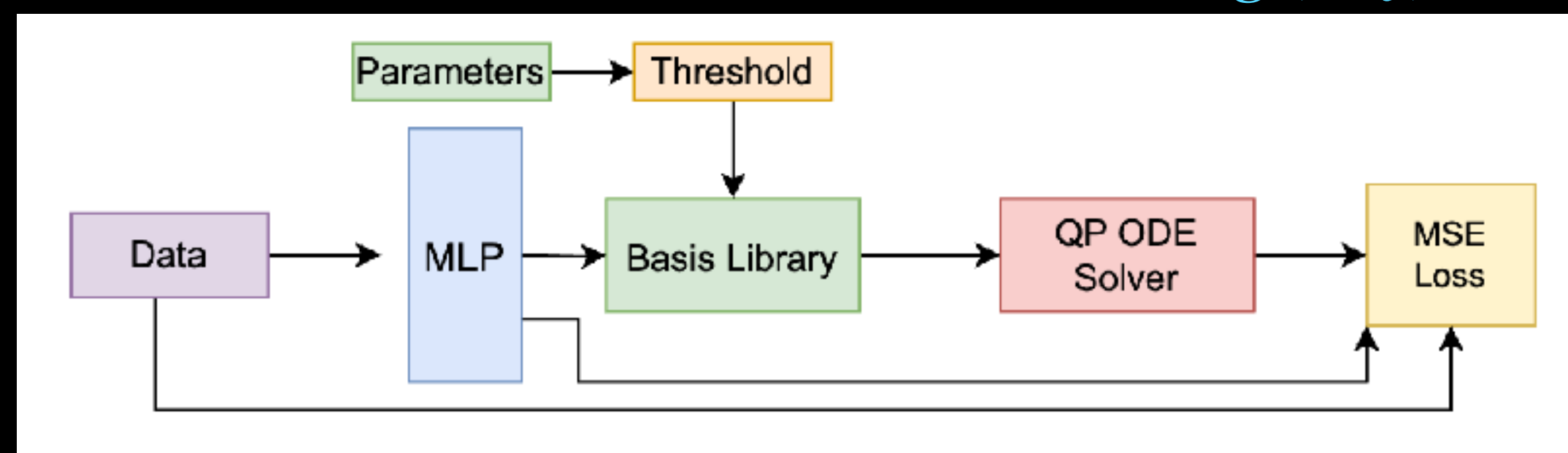
- Weaving in governing equations to an NN impacts lots of scientific applications
- With the same framework, we outperform per task specialized methods

	Neural ODE, UDE Chen et al (2018) Rackauckas et al (2020)	SINDy Brunton et al (2016)	Neural Operators Li et al (2020c)	Mech. NN
Linear discovery	–	✓	–	✓
Nonlinear discovery	–	–	–	✓
Physical parameters	✓	✓	–	✓
Forecasting	✓	–	✓	✓
Interpretability	–	✓	–	✓

MECH NN FOR DISCOVERY

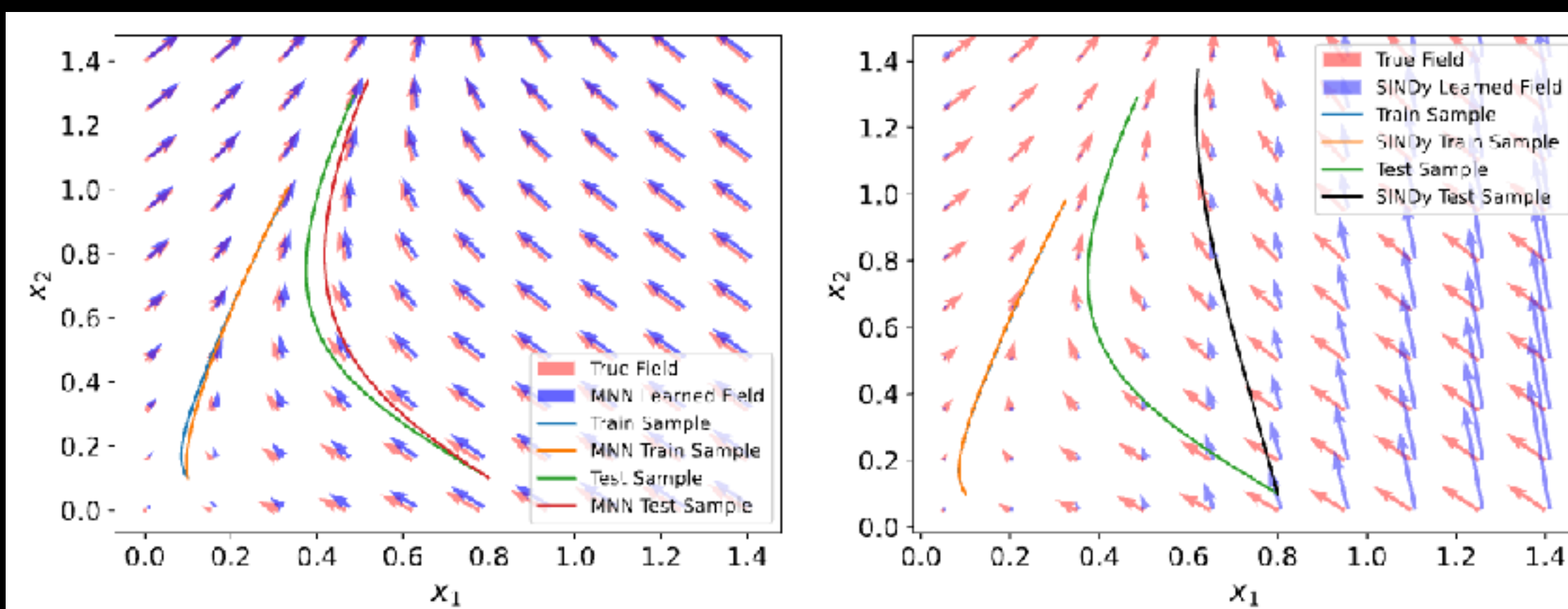
Solve ODEs of the form: $u' = g(\Theta\xi)$

Chaotic Lorenz



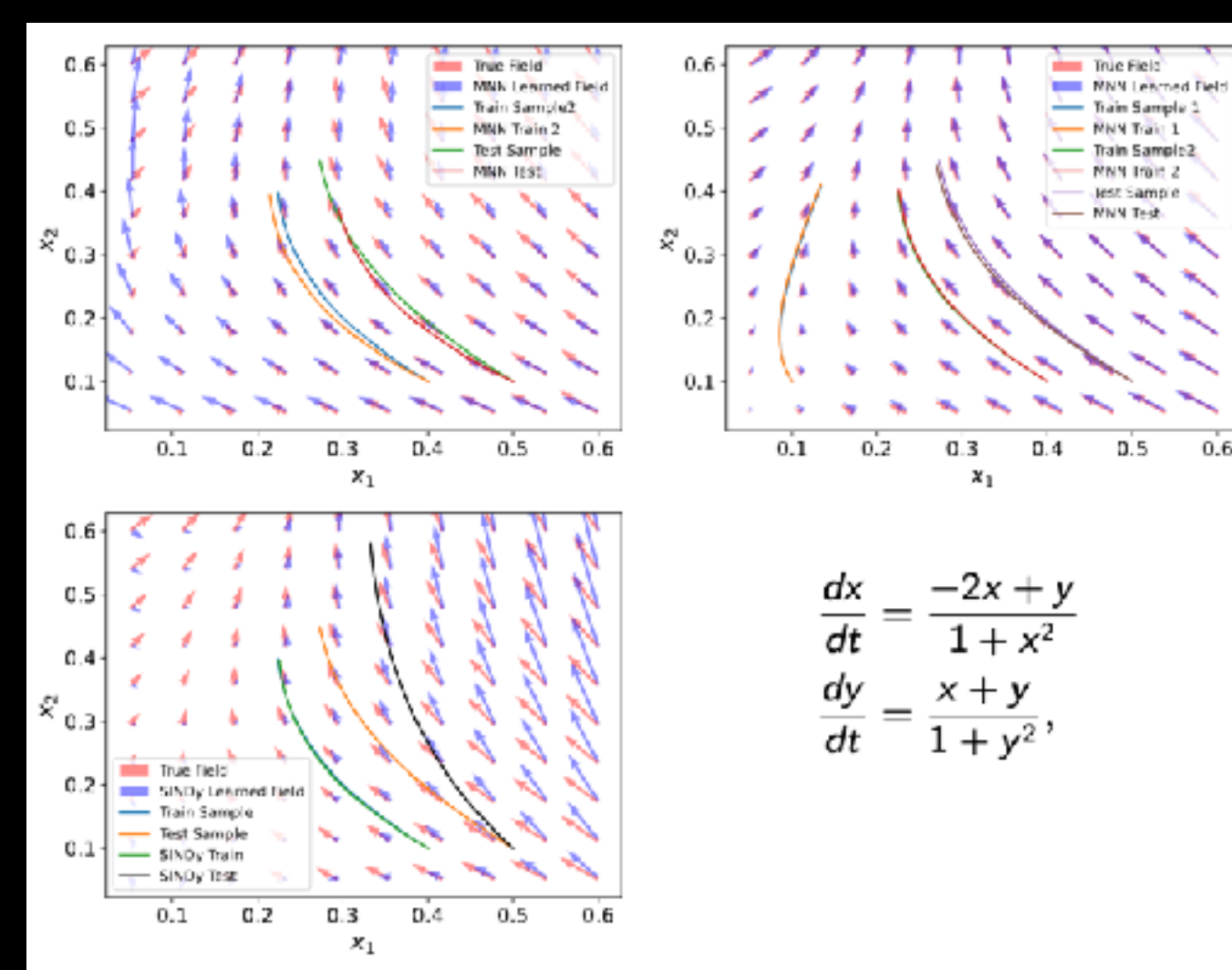
Nonlinear functions

Rational functions



$$\frac{dx}{dt} = \tanh(-2x + y)$$

$$\frac{dy}{dt} = \tanh(x + y)$$



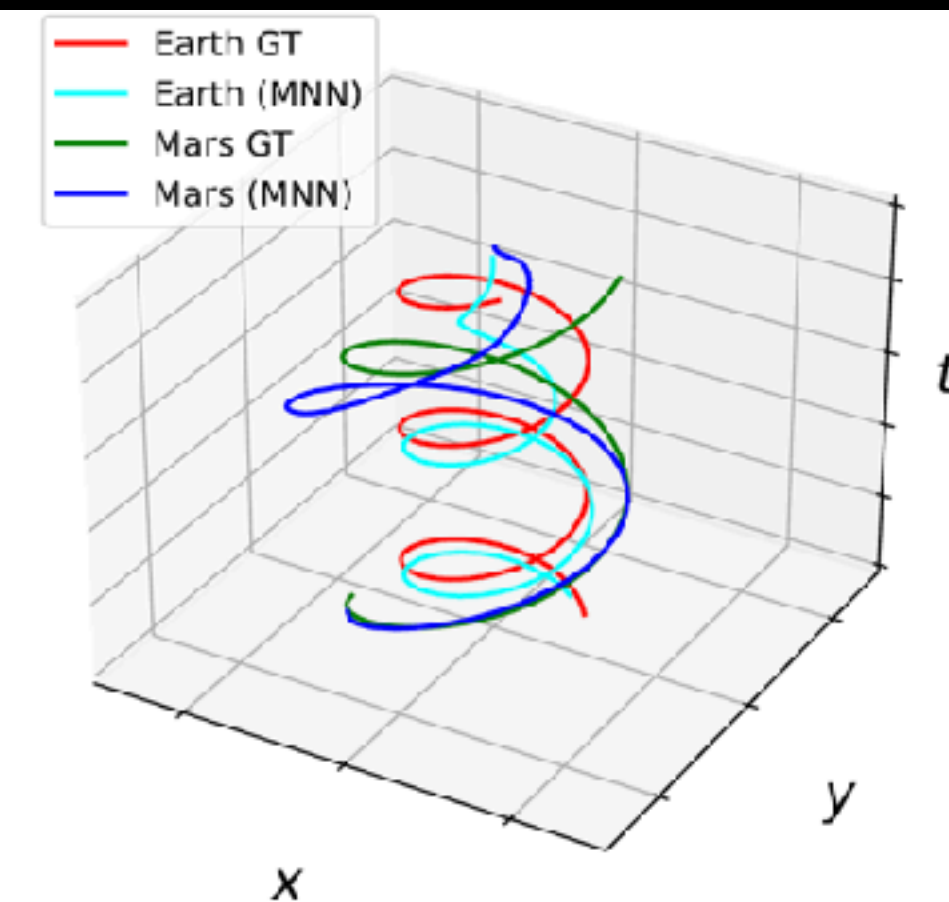
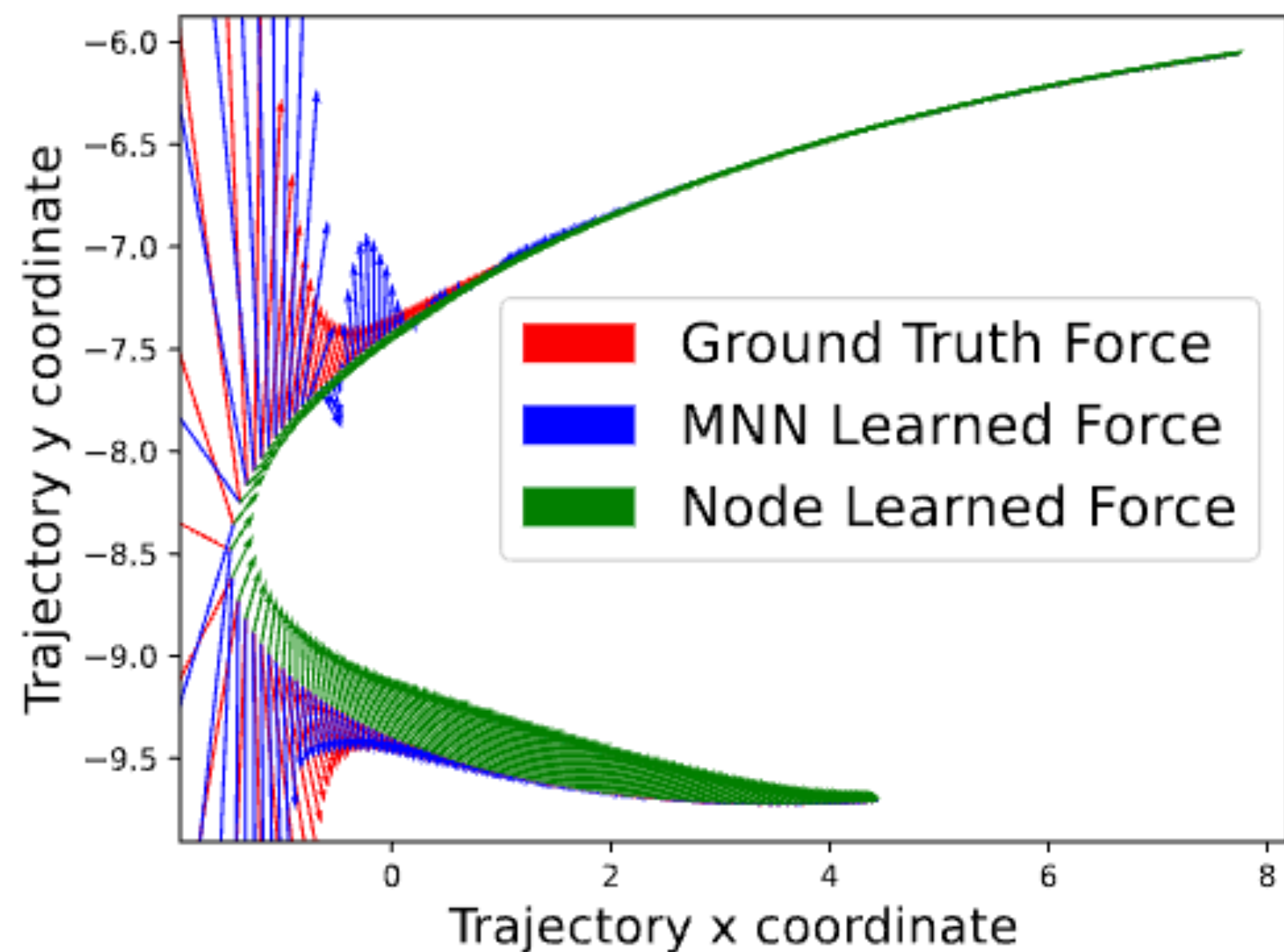
$$\frac{dx}{dt} = \frac{-2x + y}{1 + x^2}$$

$$\frac{dy}{dt} = \frac{x + y}{1 + y^2}$$

Figure 2: Learned ODE vector fields for MNN and SINDy with non-linear tanh function of basis combination and training and test trajectories. Ground truth equation is on the right.

MORE APPLICATIONS

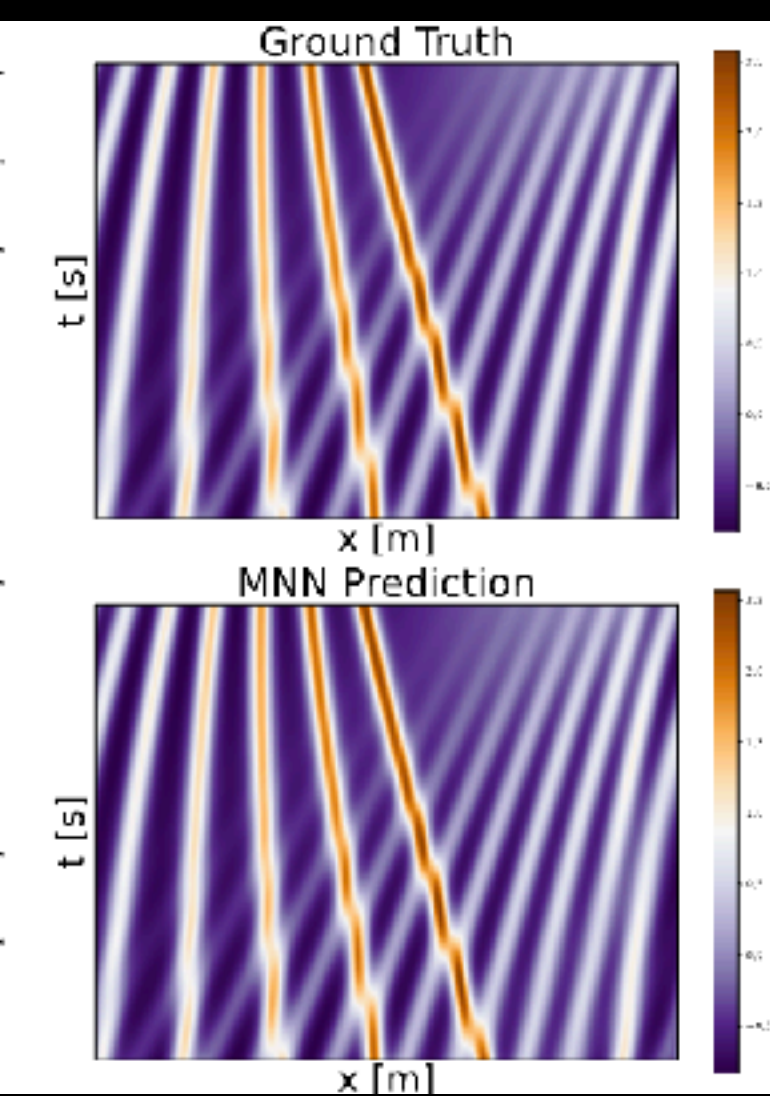
Forecasting
JPL Horizon planetary ephemerides



Method	Eval. MSE
ANODE	0.0470
NODE	0.0485
SONODE	12.200
MNN	0.0034

Method	Force MSE ↓	Cosine sim. ↑	Mass Ratio GT=2
SONODE	879	-0.26	2.11
MNN	345	0.85	2.02

Method	RMSE	
	N=512	N=256
ResNet	0.0223	0.0392
ResNet-LPSDA-1	0.0200	0.0284
ResNet-LPSDA-2	0.0111	0.0185
ResNet-LPSDA-3	0.0155	0.0269
ResNet-LPSDA-4	0.0113	0.0184
FNO	0.0276	0.0407
FNO-LPSDA	0.0055	0.0132
FNO-AR	0.0030	0.0058
FNO-AR-LPSDA	0.0010	0.0037
Mechanistic NN (50 sec)	0.0039	0.0086

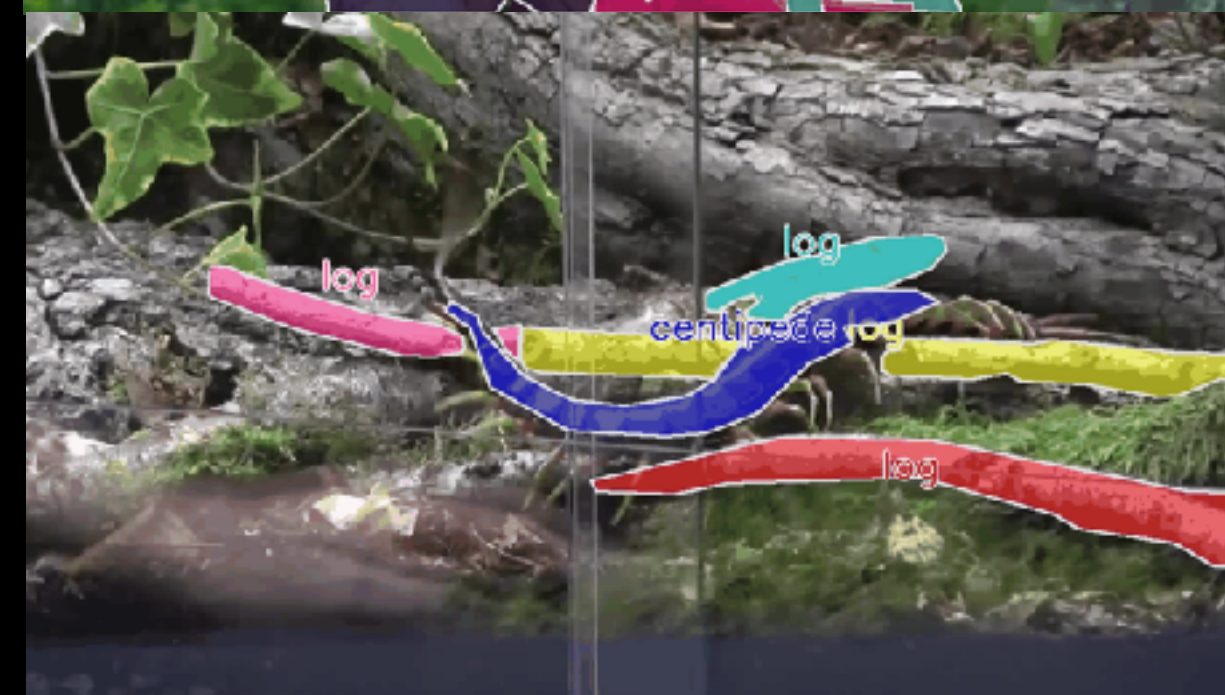
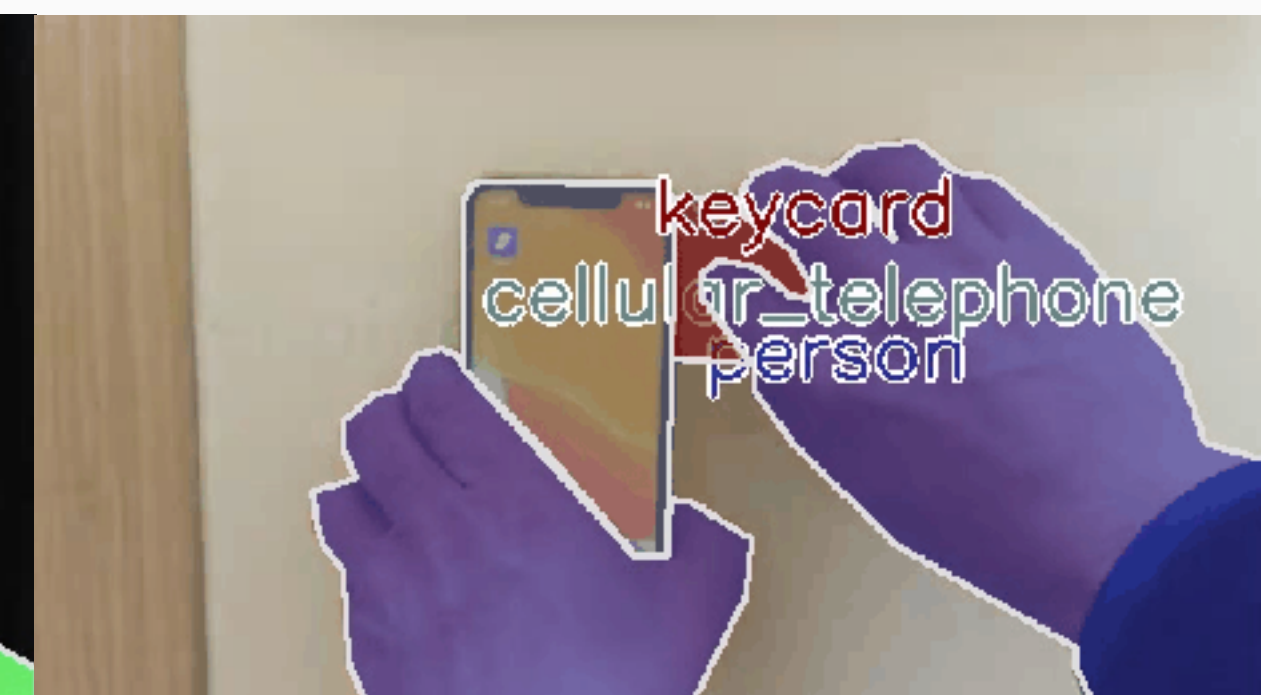


Discovering physical parameters
Mass ratio & force distribution 2-body problem

Neural PDE Solving
1d KdV and 2d Darcy Flow

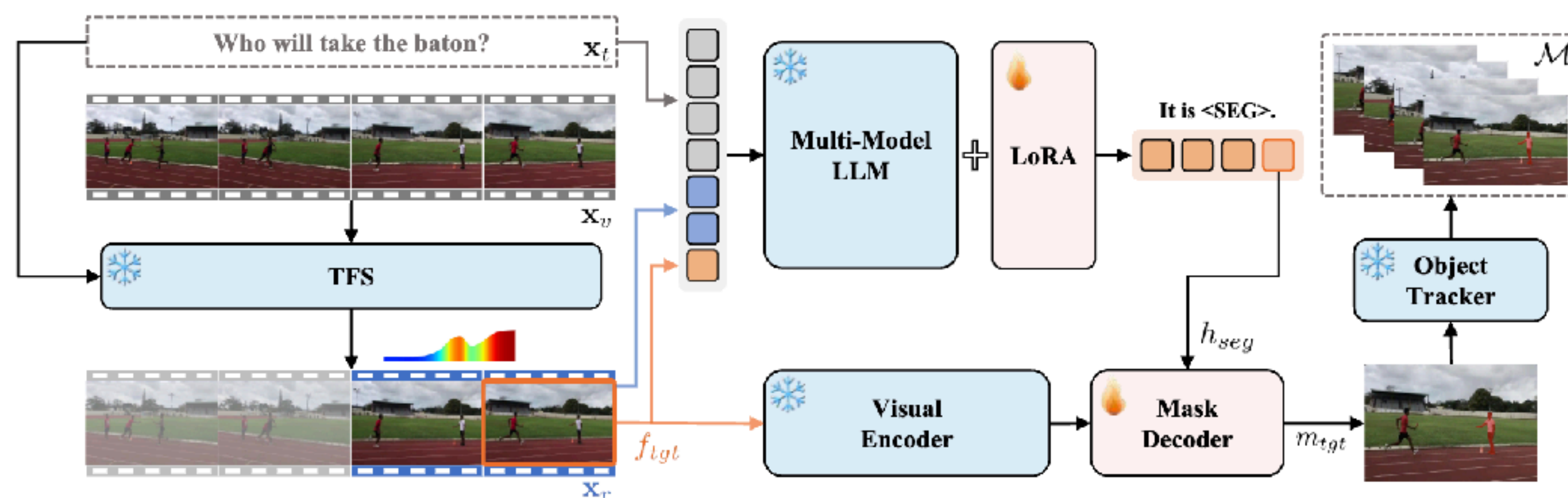
WANG ET AL, CVPR, ICCV, 2022-24

OPEN-WORLD INDUCTIVE BIASES



REASONING VIDEO INSTANCE SEGMENTATION

- Segment, classify, track by 'commonsense reasoning' w.r.t. the pixels and world knowledge
- Key idea: Scale-up sequence length in the input and relay to LLMs for 'reasoning'
- Fantastic if we could pair this with formal reasoning



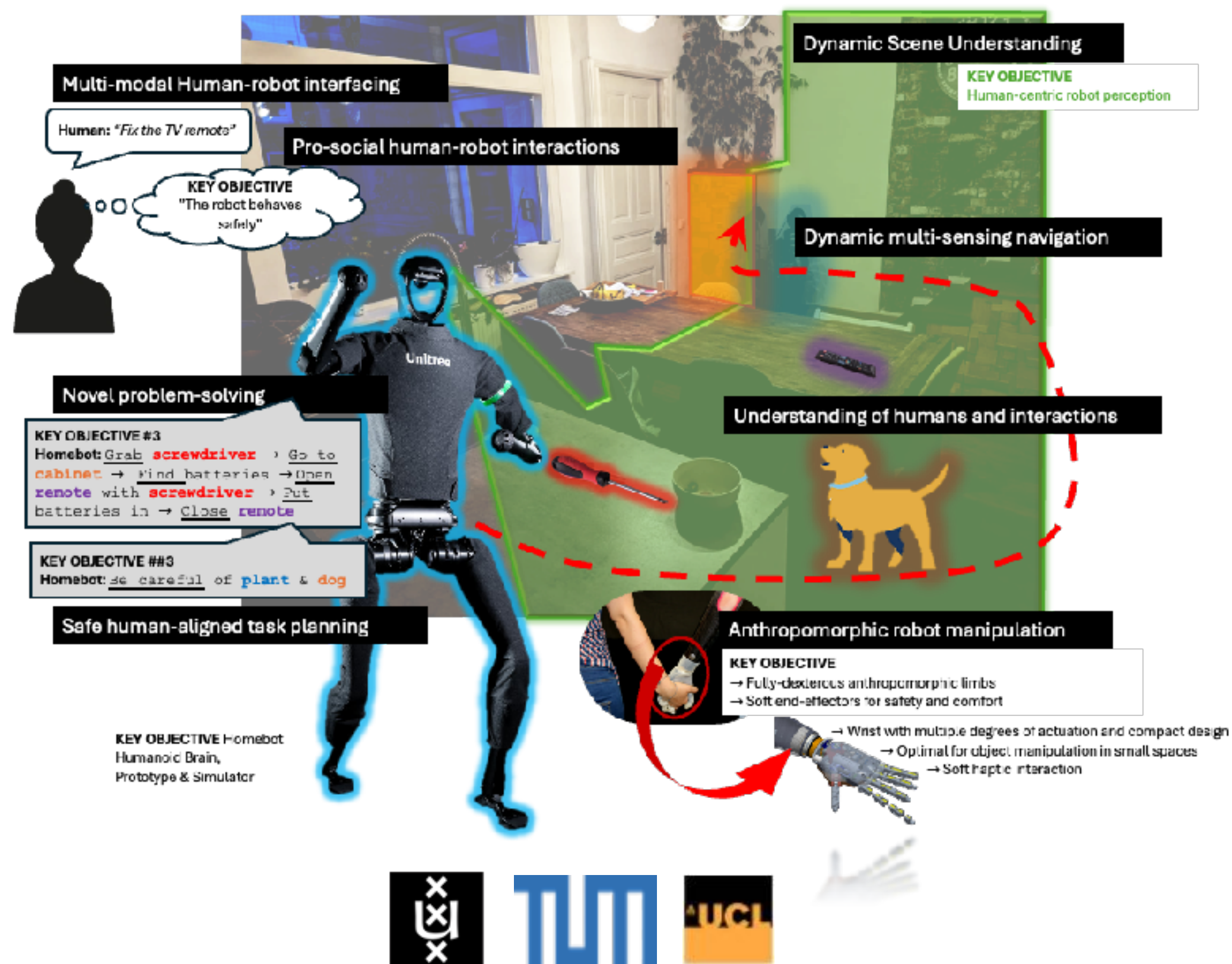
"Which ball should first be hit according to the rules?"
"Which ball is the target of this shot?"
"If this shot goes in, which ball is most likely to be hit next?"

PRO-SOCIAL & HUMAN-CENTRIC ROBOT AI

MY VISION & GOAL

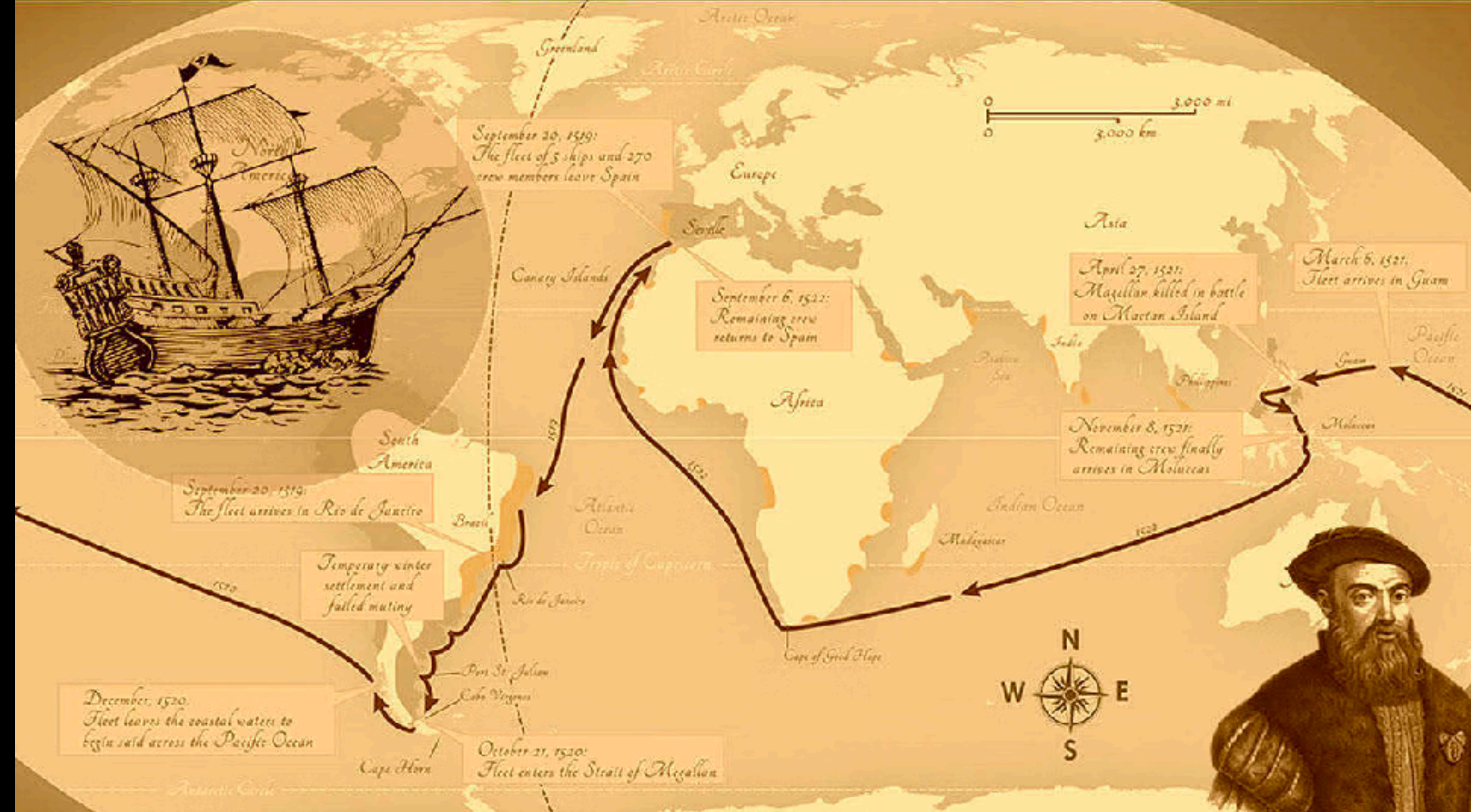
System I Perception and Manipulation
 System II Causal Learning for Robotics
 'System III' Pro-social behavior

Reusable foundation 'world' dynamics from pixels
 Neural+'Symbolic'+Equivariance Learning
 Critical for true extrapolation



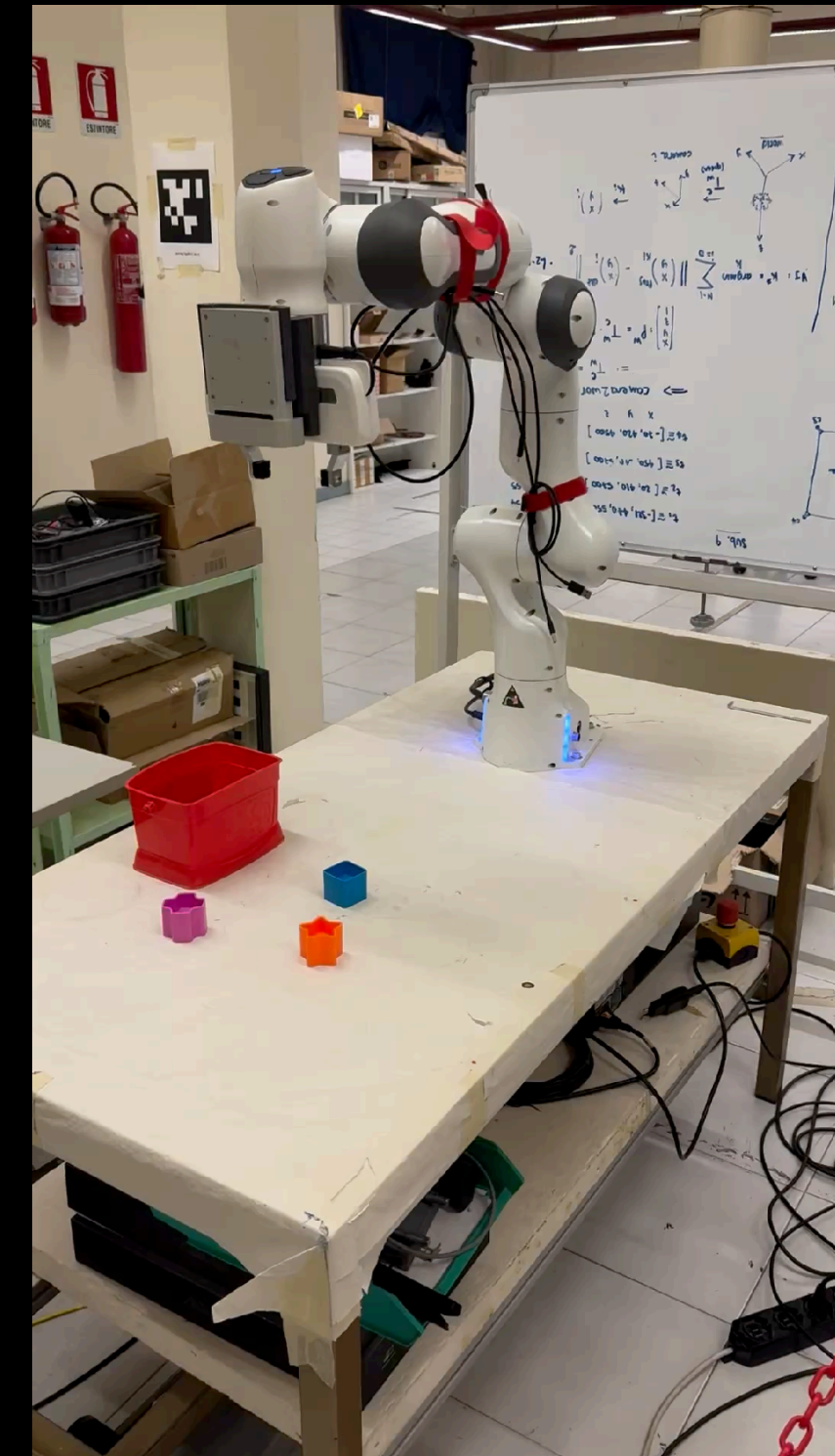
CVPR 2024 Workshop on Causal and Object-centric Representations for Robotics
 Ideally repeated with NeurIPS/ICLR/ICML and CORL/ICRA/IROS

ACADEMIC AI IN THE YEARS OF CHATGPT TO WRAP UP



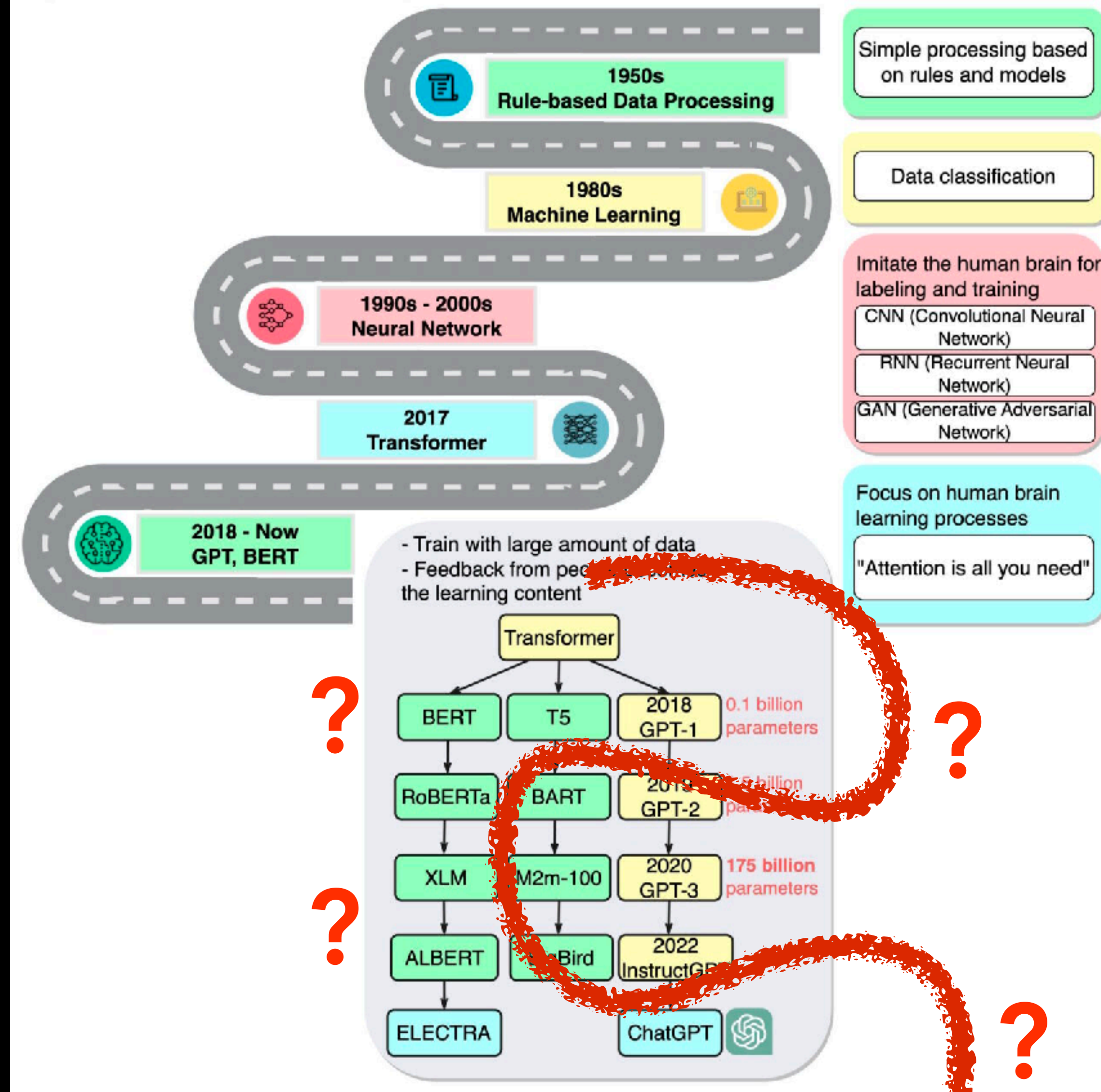
CONCLUSION

- Not yet end-to-end training, but all parts can be made differentiable
- “Physics & causal grounding”: great start toward fully neural robot world models
- And lots of exciting possibilities towards generalization and extrapolation
- We are in good company of Fei Fei Li: <https://github.com/cremebrule/digital-cousins>



CHEERS!

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@egavves



Dynamics ?
Causal Learning
Open-World
Robots & Systems